## UNIVERSITI SAINS MALAYSIA

## Second Semester Examination Academic Session 2004/2005

March 2005

## **CPT314 - Automata Theory & Formal Languages**

Duration: 3 hours

## **INSTRUCTIONS TO CANDIDATES:**

- Please ensure that this examination paper contains FIVE questions in FIVE printed pages before you start the examination.
- Answer ALL questions.
- This is an 'Open book' examination.

ENGLISH VERSION OF THE QUESTION PAPER

- 1. Answer both 1(a) and 1(b) below.
  - (a) Let  $V_1 = \{a, b, c, d\}$ ,  $V_2 = \{a, d, e, f\}$ ,  $V_3 = \{0, 1\}$ , and  $V_4 = \{b, d, e, g\}$ . Solve the following expressions based on the given sets:
    - (i)  $V_1 \cap V_3$
    - (ii)  $2^{\nu_1} \cap 2^{\nu_2}$
    - (iii)  $2^{\nu_1 \cap \nu_2}$
    - (iv)  $|V_1 \cup V_4|$
    - (v)  $|\{V_3, \{V_3\}\}|$

(50/100)

- (b) Let  $\Sigma = \{0, 1\}$ . Give regular expressions generating the following languages:
  - (i)  $P = \{w \mid w \text{ has exactly a single } 1\}$
  - (ii)  $Q = \{w \mid w \text{ has at least one } 1\}$
  - (iii)  $R = \{w \mid w \text{ is a string of even length}\}$
  - (iv)  $S = \{w \mid w \text{ starts and ends with the same symbol}\}$
  - (v)  $T = \{w \mid \text{the length of } w \text{ is at most } 5\}$

(50/100)

- 1. Let L be the language consisting of all words over the symbols 0 and 1 that have a '0' in the third-to-last place.
  - (a) Give **two** strings that belong to L and two strings that do not belong to L.

(10/100)

(b) Construct a non-deterministic finite state automaton N that accepts the strings belonging to L.

(20/100)

(c) Convert NFA N into DFA M.

(30/100)

(20/100)

(e) Try to minimize DFA M into a smaller DFA M' (if any). What can you say about M and M'?

(20/100)

3. Consider the grammar  $G = (\{S,A,B\}, \{a,b,c\}, P, S)$ , where P is given by

 $S \rightarrow aABb$ 

 $A \rightarrow bAb \mid c$ 

 $B \rightarrow aB \mid b$ 

(a) Give a leftmost and rightmost derivation of the string abcbabb in G.

(10/100)

(b) Give two strings that are not in G.

(10/100)

(c) What is the shortest string in G? Give its length.

(10/100)

(d) Give the equivalent PDA M and draw its transition diagram.

(50/100)

(e) Simulate M for the string abcbabb.

(20/100)

4. Let  $\Sigma = \{0, ..., 9, +, -, *, /, ^, )$ , ( $\}$ . The language of all strings over the alphabet  $\Sigma$  represents syntactically correct arithmetic expressions on integers involving the following operators.

Operators	Precedence	Associativity	
<del>_</del>	3		Negation
^	2	Right	Exponentiation
*	1	Left	Multiplication
1	1	Left	Division
+	0	Left	Addition
_	0	Left	Subtraction

In the table above, the precedence of operators is listed from highest (3) to lowest (0) precedence. We say that operator  $\mathbf{p}$  has precedence over operator  $\mathbf{q}$  if an expression is of the form:

expr1 p expr2 q expr3 is interpreted only as (expr1 p expr2) q expr3.

In arithmetic expressions, (well balanced) parentheses are used to modify the order of precedence and associativity of operators.

In arithmetic expression, except for 0 (zero), integers cannot start with zero. For example, 002 is not an integer.

Samples of well formed arithmetic expressions:

Samples of not well formed arithmetic expressions:

(a) Add parentheses to the following expressions to make clear the precedence of the operators.

e.g: 
$$2*4+22+452+-1 \rightarrow ((2*4)+22)+452)+(-1)$$

- (i)  $20+-20+68^2/23-23 \rightarrow$
- (ii)  $2+-2*3^3^4*8+2^4^3+2*5 \rightarrow$  (20/100)
- (b) Find a grammar G that can generate all arithmetic expressions described above.

(40/100)

(c) Convert the grammar G into a PDA M that can recognise all well formed arithmetic expressions.

(40/100)

- 5. Let  $L = \{0^{2^n} \mid n \ge 0\}$ .
  - (a) Design a Turing machine T for the language L.

(50/100)

(b) Draw the state diagram of T.

(30/100)

(c) Show the ID's of the Turing machine T if the input tape contains the string "0".

(20/100)