## SULIT

Second Semester Examination
2021/2022 Academic Session
July/August 2022

## EAS254 - Structural Analysis

Duration : 3 hours

Please ensure that this examination paper contains SEVEN (7) printed pages including appendix before you begin the examination.

Instructions: This paper contains FIVE (5) questions. Answer ALL questions.

All questions MUST BE answered on a new page.

1. Figure 1 shows a frame subjected to a concentrated moment of $M$ at point $B$, a uniformly distributed load of $w$ acting vertically along span BC and a point load of $P$ at mid-span of span AB. Use the virtual work method to determine the slope at $A$ and displacement at $C$ along the inclined plane $B C$ ( $x$-axis). Take $E=200 \mathrm{GPa}$ and $I=100 \times 10^{6} \mathrm{~mm}^{4}$. Ignore the axial work. The values of all applied loads are given in Table 1.
[20 marks]


Figure 1

Table 1

| Last digit of <br> index <br> number | $P$ <br> $(\mathrm{kN})$ | $w$ <br> $(\mathrm{kN} / \mathrm{m})$ | Second last digit <br> of <br> index number | $M$ <br> $(\mathrm{kNm})$ |
| :---: | :---: | :---: | :---: | :---: |
| 0 | 25 | 7.5 | 0 | 20 |
| 1 | 30 | 8 | 1 | 22.5 |
| 2 | 35 | 8.5 | 2 | 25 |
| 3 | 40 | 9 | 3 | 27.5 |
| 4 | 45 | 9.5 | 4 | 30 |
| 5 | 42.5 | 10 | 5 | 32.5 |
| 6 | 37.5 | 10.5 | 6 | 35 |
| 7 | 32.5 | 11 | 7 | 37.5 |
| 8 | 27.5 | 11.5 | 8 | 40 |
| 9 | 22.5 | 12 | 9 | 40.5 |

Note: If your index number is 50038, use $P=27.5 \mathrm{kN}, w=11.5 \mathrm{kN} / \mathrm{m}$ and $\mathrm{M}=27.5$ kNm.
2. Figure 2 shows a beam carrying a point load of 100 kN at spans $A B, B C$ and DE acting at $30^{\circ}$ and $150^{\circ}$ with certain distance. Meanwhile, span BC carrying a uniform distributed load of $10 \mathrm{kN} / \mathrm{m}$ and span CD carrying a distributed load varying from $10 \mathrm{kN} / \mathrm{m}$ at C to $0 \mathrm{kN} / \mathrm{m}$ at D . Supports A and E are fixed, whereas supports $B, C$ and $D$ are pinned. $E l$ is constant for the beam.
(a) Compute the internal moments at the joint of the beam by using Moment Distribution Method. Fixed end moment is given in the Appendix.
[15 marks]
(b) Draw the bending moment diagram and the qualitative deflected shape for the beam.
[5 marks]


Figure 2
3. Figure 3 shows a frame carrying a point load of 40 kN and 100 kN at the midspan of $A B$ and $B C$ and an additional $20 \mathrm{kN} / \mathrm{m}$ of uniform distributed load at span AB. Meanwhile, span DE carrying a distributed load varying from 20 $\mathrm{kN} / \mathrm{m}$ at midspan $D E$ to $0 \mathrm{kN} / \mathrm{m}$ at D and E . A point load of 10 kN is loaded at overhang portion for span DG. Supports A, C and F are fixed and support E is pinned. $E l$ is constant for the frame.

Compute the internal moments at the joint of the frame by using Slope Deflection Method. Fixed end moment is given in the Appendix.
[20 marks]


Figure 3
4. Figure 4 shows a single overhanging concrete beam that supports a trapezoidal load with a minimum and maximum of $15 \mathrm{kN} / \mathrm{m}$ and $30 \mathrm{kN} / \mathrm{m}$, respectively, along with span $A B$. In addition, the beam supports a uniformly distributed load of $15 \mathrm{kN} / \mathrm{m}$ along with span BC and a concentrated load of 20 kN at C . The beam is fixed at $A$ and supported by a roller at B . El of the beam is constant. Answer the following questions using the method of least work.
(a) Using a vertical reaction force at $B$ as a redundant force, determine the reactions at supports $A$ and $B$.
[17 marks]
(b) If a roller is placed at point C , state the analysis procedure to determine the reaction force at supports $\mathrm{A}, \mathrm{B}$, and C .
[3 marks]


Figure 4
5. Figure 5 shows a rigid-jointed frame is loaded with the working loads. Determine the value of $M_{p}$ if the collapse load factor is 1.5 . Consider all possible mechanisms.
[20 marks]


Figure 5

## APPENDIX



