## SULIT

February 2021

## EAS253 - Theory of Structures

Duration : 2 hours

Please check that this examination paper consists of SEVEN (7) pages of printed material before you begin the examination.

Instructions: This paper contains THREE (3) questions. Anwser ALL questions.
All questions MUST BE answered on a new page.

1. (a). Figure 1 shows a continuous beam with a hinge joint at $B$. Check statical determinacy of the beam. Suggest a way with proof to reduce the degree of statical indeterminacy of the beam by ONE (1), without changing the support conditions.
[7 marks]


Figure 1
(b). Verify with proof if the following statement is true:
"Degree of statical in indeterminacy of the frame shown in Figure 2 is FOUR (4)".


Figure 2
(c). Figure 3 shows a frame which is pin-supported at $A$ and $E$. Joint $C$ is a hinge joint. Vertical uniformly distributed loads of $6 \mathrm{kN} / \mathrm{m}$ and $8 \mathrm{kN} / \mathrm{m}$ act along inclined member AB and horizontal member BD , respectively. Joint $D$ is subjected to a horizontal concentrated load of 45 kN .
(i). Determine the distribution of axial force in inclined member $A B$.
(ii). Determine shear force on section just to the left of joint $D$.
(iii). Draw bending moment diagram for the frame.
(iv). Sketch the qualitative deflected shape.
[20 marks]


Figure 3
2. (a). Figure 4 shows a plane truss of a slanting roof for an airport. Check the statical determinacy of the truss. Support A is pinned and support F is roller. All member connections are pinned. Find the reactions at both supports and identify zero force members, if any. Determine forces in members $\mathrm{BD}, \mathrm{DC}$ and CE by using section method and members DF , DE and EF by using joint method. Classify whether they are in tension or compression.
(b). If one member $D E$ is removed from the truss shown in Figure 4, determine what will happen to the overall stability of the truss. Will there be any changes of the forces in members DF and EF?
(c). If the 100 kN and 80 kN loads in the truss shown in Figure 4 are reduced by $50 \%$, respectively, what will happen to the value of the reactions and the forces in members DC and CE?
[5 marks]
(d). If the length of all the members in the truss shown in Figure 4 are doubled, explain the changes of the forces in members DE and EF.


Figure 4
3. (a). Figure 5 shows a simple beam subjected to a uniformly distributed load of $\mathrm{w} \mathrm{kN} / \mathrm{m}$ acting at the first $L 1 \mathrm{~m}$ from the left support. Flexural rigidity of the beam is $2 E I$. Given $E=210 \mathrm{GPa}$ and $I=125\left(10^{6}\right) \mathrm{mm}^{4}$, calculate the slope and deflection of the beam at a point $b \mathrm{~m}$ from the right support of the beam. The values of $w, L 1$ and L2 are given in Table 1 according to your matriculation number. Use either moment-area method or conjugate-beam method.


Figure 5
(b). If an additional concentrated moment of $M \mathrm{kNm}$ acts at the right support of the beam as shown in Figure 6, calculate the slope and deflection at point $L 2 \mathrm{~m}$ from the right support of the beam. The value $M$ is given in Table 1 according to your matriculation number. Use either momentarea method or conjugate-beam method.


Figure 6

Table 1: Values of $w, M, L 1$ and $L 2$

| Last digit of <br> matriculation <br> number | $w$ <br> $(\mathrm{kN} / \mathrm{m})$ | $M$ <br> $(\mathrm{kNm})$ | Second last digit <br> of matriculation <br> number | $a$ <br> $(\mathrm{~m})$ | $b$ <br> $(\mathrm{~m})$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 3 | 25 | 0 | 3 | 2 |
| 1 | 3.5 | 22.5 | 1 | 3.5 | 2.5 |
| 2 | 4 | 20 | 2 | 4 | 3 |
| 3 | 4.5 | 17.5 | 3 | 4.5 | 3.5 |
| 4 | 5 | 15 | 4 | 5 | 4 |
| 5 | 5.5 | 12.5 | 5 | 4 | 5 |
| 6 | 6 | 10 | 6 | 3.5 | 4.5 |
| 7 | 6.5 | 7.5 | 7 | 3 | 4 |
| 8 | 7 | 5 | 8 | 2.5 | 3.5 |
| 9 | 7.5 | 2.5 | 9 | 2 | 3 |

Note: If your matriculation number is 15628 , use $w=7 \mathrm{kN} / \mathrm{m}, M=5 \mathrm{kNm}$, $L 1=3 \mathrm{~m}$ and $L 2=4 \mathrm{~m}$.

