

**DEVELOPMENT AND APPLICATION OF  
YIELDING STEEL PLATE DAMPER TO IMPROVE  
SEISMIC PERFORMANCE OF STRUCTURES**

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**UNIVERSITI SAINS OF MALAYSIA**

**2017**

**DEVELOPMENT AND APPLICATION OF YIELDING STEEL PLATE  
DAMPER TO IMPROVE SEISMIC PERFORMANCE OF STRUCTURES**

**by**

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**Thesis submitted in fulfillment of the  
requirements for the degree of  
Doctor of Philosophy**

**April 2017**

## ACKNOWLEDGEMENTS

First, I would like to thank almighty God for the grace and mercy, which enable me to complete my studies. The author wishes to express his sincere gratitude to his supervisor, associate Professor Taksiah A. Majid and Professor Bambang Budiono for their support and time dedicated during preparation my thesis. Their inputs, help, encouragement, and guidance ensure this thesis to be completed.

I would like to thank the structural laboratory staff of Bandung Institute of Technology and in particular to Mr. Burhan and Mr. Rahmat for their preparation, installation, and testing of the steel damper specimens, and to graduate student Mr. Lukman Murdiansyah for his monitoring during fabrication, installation, and testing.

I also wish to express my sincere appreciation to my wife Sofia Rita, my sons Christopher Teruna, Jonathan Teruna, and Joshua Kenny Teruna for their patience, supports and encouragements.

Last but not the least, I would like to appreciate the Ministry of Higher Education and University of Sumatera Utara for funding my research through Grant No. 4267/UNS.1.R/KEU/2013.

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