# FSI SIMULATIONS OF AN AEROELASTIC SYSTEM WITH AERODYNAMIC NONLINEARITY

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### FSI SIMULATION OF AN AEROELASTIC SYSTEM WITH AERODYNAMIC NONLINEARITY

by

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#### LIST OF ABBREVIATIONS

2D Two dimensional

3D Three dimesional

AC Aerodynamic Center

AOA Angle of Attack

CFD Computational Fluid Dynamic

CSD Computational Structural Dynamics

DES Detached Eddy Simulation

DOF Degree Of Freedom

EA Elastic Axis

FEA Finite Element Analysis

FEM Finite Element Method

FSI Fluid Structure Interaction

LAO Large Amplitude Oscillation

LCO Limit Cycle Oscillation

LES Large Eddy Simulation

LEV Leading Edge Vortex

LSB Laminar Separation Bubble

PISO Pressure Implicit with Splitting of Operator

RANS Reynold Average Navier-Stokes

RMS Root Mean Square

RSM Reynold Stress Model

SAO Small Amplitude Oscillation

SIMPLE Semi Implicit Method for Pressure Linked Equations

SIMPLEC Semi Implicit Method for Pressure Linked Equations Consistent

SST Shear Stress Transport

UDF User Defined Function

URANS Unsteady Reynold Average Navier-Stokes

VLM Vortex Lattice Method

# FSI SIMULASI SISTEM AEROELASTIK DENGAN KETIDAKSAMAAN AERODINAMIK

#### **ABSTRAK**

Tesis ini membentangkan kajian sistem aeroelastik sebuah model NACA0012 rigid yang dipasang secara elastik dengan ketidaksamaan aerodinamik. Tingkah laku aeroelastik dari sayap dua dimensi berayun diperiksa dengan cara simulasi numerik. Simulasi NACA0012 dipelajari secara numerik melalui simulasi aeroelastic dua dimensi menggunakan ANSYS Fluent 16.1 untuk menilai tindak balas getaran aeroelastic pada paksi elastik yang berlainan dengan ketidaksamaan aerodinamik dan mendapati fenomena ketidaksamaan aerodinamik terhasil daripada pemisahan lapisan sempadan, pemisahan dan aliran lampiran semula di sekitar aerofoil. Simulasi menggunakan model RANS (SST) k-ω dengan pembetulan nombor Reynolds yang rendah untuk menangkap aliran fizikal di sekitar aerofoil. Interaksi struktur bendalir dinamik (FSI) dicapai melalui gabungan persamaan struktur gerakan dengan penyelesai bendalir dalaman melalui utiliti fungsi (UDF) yang ditentukan oleh Fluent. Simulasi numerik dijalankan pada tiga kedudukan paksi elastik (EA) yang berbeza, 0% (titik depan), 18.6% dan 35% dari titik depan. Simulasi dijalankan pada julat kelajuan angin dari 4 m/s hingga 14 m/s. Hasilnya menunjukkan dua amplitud ayunan yang berlainan daripada tindak balas dinamik yang dihasilkan oleh sistem aeroelastik, di EA dari 0% (titik depan) dan 18.6% menghasilkan ayunan amplitud kecil (SAO) sementara pada paksi elastik 35% menghasilkan ayunan besar amplitud (LAO). Pengesahan simulasi numerik menunjukkan kecenderungan yang sama dengan hasil eksperimen dan didapati menghasilkan amplitud had ayunan kitaran (LCO) yang boleh dibandingkan. Dari aspek aliran aerodinamik, pemisahan lapisan sempadan laminar didapati memainkan peranan penting untuk ayunan yang mengekalkan ayunan dalam

ayunan amplitud kecil. Fenomena aliran pusaran, pemisahan aliran dan fenomena pengaliran lampiran semula dijumpai menyebabkan amplitud yang besar dan pusaran aliran yang terbalik di titik belakang aerofoil menyebabkan sayap bergerak dan mengekalkan kitaran ayunan.

# FSI SIMULATION OF AN AEROELASTIC SYSTEM WITH AERODYNAMIC NONLINEARITY

#### **ABSTRACT**

This thesis presents a study of aeroelastic system of an elastically mounted rigid NACA0012 airfoil with aerodynamics nonlinearity. The aeroelastic behavior of a two dimensional wing oscillating is examined by means of numerical simulations. The simulation of NACA0012 is studied numerically through unsteady two-dimensional aeroelastic simulation using ANSYS Fluent 16.1 to evaluate the aeroelastic response of stall flutter at different elastic axis with aerodynamic nonlinearities and found that the aerodynamic nonlinearities are from boundary layer separation, the separation and reattachment of flow around the airfoil. The simulation employed RANS (SST) k-ω model with low Reynolds number correction to capture the physical flow around the airfoil. The dynamics fluid structure interaction (FSI) were achieved by coupling the structural equation of motion with an in-house fluid solver through defined function (UDF) utility in Fluent. Numerical simulations were ran through at three different elastic axis (EA) positions, 0% (leading edge), 18.6% and 35% from the leading edge. The simulations were ran through at free stream velocity range from 4m/s to 14m/s. The results showed two different oscillation amplitudes from the dynamic responses generated by the aeroelastic system of the airfoil, at EA of 0% (leading edge) and 18.6% produced small amplitude oscillation (SAO) while at 35% elastic axis produced large amplitude oscillations (LAO). The validation of numerical simulation showed trends which are similar to experiment results and are found to produce a reasonably comparable limit cycle oscillation (LCO) amplitudes. From the aerodynamic flow aspect, laminar boundary layer separation was found to play an important role for the oscillation sustaining the pitching oscillation in small amplitude oscillation. Leading

edge vortex, flow separation and reattachment flow phenomena was found which caused large amplitude oscillation and reversed flow vortices at the trailing edge of the airfoil caused the wing to pitch down and maintaining the oscillation cycle.

#### **CHAPTER ONE**

#### INTRODUCTION

#### 1.1 Aeroelasticity

"Aeroelasticity" is a term used to represent the field of study concerned with the interaction between the deformation of an elastic structure in an airstream and the resulting aerodynamic force. Aeroelasticity can be categorized into two major categories, static and dynamic. Static aeroelasticity consists of the interaction between elastic and aerodynamic forces whereas the dynamic side involves the interaction of aerodynamic, elastic, and inertial forces. Aeroelastic phenomena can include several types of oscillations resulted from classical bending torsion flutter, stall flutter, buffeting and Limit Cycle Oscillations (LCO). Flutter is an example of an unstable self-excited vibration, and can arise under conditions of steady-state airflow. In the design of aircraft and aerospace components, design for aeroelastic performance is of fundamental importance, where if flutter vibration amplitude cannot be controlled, catastrophic structural failure can result. The classical airfoil flutter is a fundamental flow induced instability mechanism described as self-excited plunging and pitching oscillations of an airfoil subjected to airflow. One of the first fundamental studies considering the classical airfoil flutter was published by Theodorsen (Theodorsen, 1934) who obtained a closed-form solution of the flutter instability in the frequency domain with the experimental validation. Flutter of airplane wings or aircraft engine turbomachinery blades is a critical issue determining the reliability of the aircraft. The flutter phenomenon is the results of the fluid structural interaction and is usually involved with complicated phenomena such as the shock wave boundary layer interaction, flow separation, nonlinear limited cycle oscillation, etc. Accurate

prediction of the flutter is very challenging due to the complex physical phenomena and the required large amount of computation. The current study is an effort to develop the methodologies needed to achieve prediction of aircraft flutter. The best way to explain aeroelastic phenomena and interaction between forces mentioned is by observing at Collar's aeroelastic triangle (Collar, 1946) shown in Figure 1.1 In Figure 1.1, main disciplines of stability and control, structural dynamics and static aeroelasticity each caused from the interaction of two of the three forces. However, all three forces are required to interact for dynamic aeroelastic effects to happen.

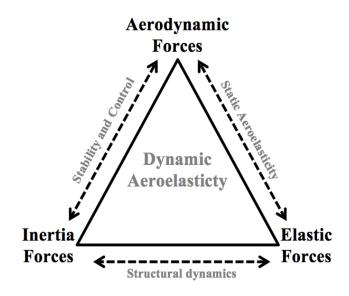


Figure 1.1: Collar's Aeroelastic Triangle

The presence of nonlinearity in aeroelastic system is known to affect the dynamic responses of the system which sometimes causes oscillation that cannot be predicted by linear theory (Razak, 2012). One of the types of oscillation is Limit Cycle Oscillation or LCO which requires at least one nonlinear element in a given system to occur. The sources of nonlinearity can be from structural or aerodynamic nonlinearities (Razak and Dimitriadis, 2013).

Computational fluid dynamics (CFD) and finite element method (FEM) provide the basic tools for predicting flutter, buffeting and limit cycle oscillation, hence computational aeroelasticity is expected to play a vital role in numerical modelling of combined solid-fluid interaction in the context of aerospace component and structure design (Schuster et al., 2003). In this project, Fluid structure interaction simulation analysis predicts the flow characteristics of the airfoil, including turbulence and flow separation.

#### 1.1.1 Stall Flutter

Phenomenon of stall flutter arises when there is flow separation and reattachment to the surface of the wing in a cyclic manner. The separation can be categorized as partial separation or fully separation on the wing surface. Another aeroelastic phenomenon that can occur from the flow separation is galloping. The Occurrence of galloping can be observed when there is only flow separation over the bluff bodies. Dynamic stall is a process of alternation between stalled and attached flow, this phenomenon has been the subject of numerous experimental and theoretical investigations. (Ericson and Reding, 1971; McCroskey William, 1981; Spentzos et al., 2005)

The coupling of the vibration characteristics of a flexible structure with dynamic stall caused stall flutter to take place. The stall flutter phenomenon has been observed in helicopter rotor blades, wind turbine blades, low stiffness wing operating at high angles of attack and wind tunnel models.

#### 1.2 Conceptual Theory

#### 1.2.1 Dynamic

In this section the terminology that will be used to define airfoil, airfoil motions and unsteady aerodynamics in the rest of this thesis are presented. The terminology concerns geometric, aerodynamic and kinematic characteristics.

#### 1.2.2 Reduced Frequency

In the field of aeroelasticity, reduced frequency describes the unsteadiness of the flow and is symbolized by the symbol k. Reduced frequency is a degree of flow unsteadiness due to body motion. Reduced frequency is given by

$$k = \frac{\omega b}{v} \tag{1.1}$$

Where,  $\omega$  is the oscillation frequency, b is the airfoil's chord length and v is the free stream airspeed. The value of reduced frequency represents the unsteadiness of the flow which ranges from 0 to 1 as given in Table 1.1.

Table 1.1: Classification of flow unsteadiness

Range	Classification
k = 0	Steady
0 < k < 0.05	quasi-steady
0.05 < k < 0.2	Unsteady
k > 0.2	Highly unsteady

Reduced frequency values between 0 and 0.05 specifies quasi-steady flow where wake effects are unimportant. For 0.05 to 0.2 the flow is quasi-unsteady and added mass is negligible but wake effects are critical. The fully unsteady flow regime is characterized by reduced frequency values exceeding 0.2, the resulting flow is dominated by acceleration effects.

#### 1.2.3 Equation of motion

Equation of motion for one degree of freedom can be obtained by applying summation of forces and moment acting on the airfoil body.

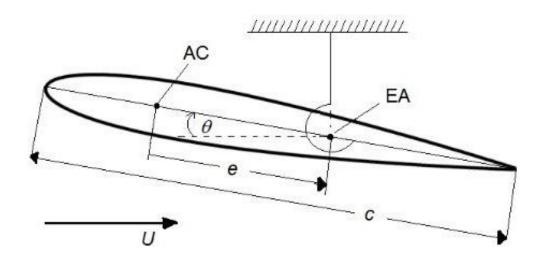


Figure 1.2: Schematic of a spring-supported symmetric airfoil.

From the Figure 1.2, AC is the aerodynamic center, EA is the elastic axis which the spring-supported symmetric airfoil is located, c is the chord length and e is the distance between aerodynamic center and elastic axis. In the case where the motion is restricted to pitching only, the equation of motion is given as:

$$I_{EA}\ddot{\theta} + D_{\theta}\dot{\theta} + K_{\theta}\theta = M_{EA} \tag{1.2}$$

Where,  $M_{EA}$  is the moment at the elastic axis,  $I_{EA}$  is the moment of inertia measured at the elastic axis,  $D_{\theta}$  and  $K_{\theta}$  are structural damping and structural stiffness respectively.

#### 1.2.4 Limit Cycle Oscillation

Aeroelastic phenomenon are the dynamical phenomenon resulting from the mutual interaction of aerodynamic forces, elastic forces and elastic forces. Limit Cycle Oscillations (LCO) is one of the vibration phenomenon which requires at least one nonlinear element in a given system to occur (Razak and Dimitriadis, 2013). For an aeroelastic system, the nonlinearity can be from structural, aerodynamic or both. Flutter causes the system to vibrate and when nonlinearity elements is introduced, LCO phenomenon happens to sustain the vibration without any decay in the system. The nature of the transient oscillations is dependent on the initial conditions or perturbation given to the system.

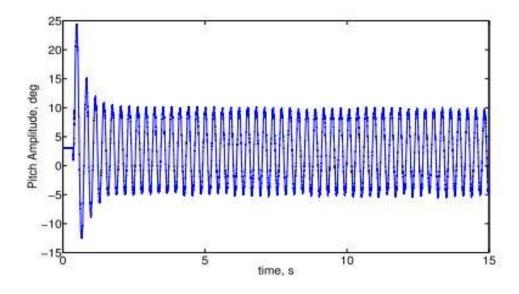


Figure 1.3: Limit cycle oscillations time response (Abdul Razak et al., 2012).