



UNIVERSITI SAINS MALAYSIA

First Semester Examination  
2017/2018 Academic Session

January 2018

**ESA321 – Aerospace Structure**  
**[Struktur Aeroangkasa]**

Duration : 3 hours  
Masa : 3 jam

Please ensure that this paper contains **FOURTEEN (14)** printed pages, included **THREE (3)** pages appendix and **FIVE (5)** questions before you begin examination.

*Sila pastikan bahawa kertas soalan ini mengandungi **EMPAT BELAS (14)** mukasurat bercetak termasuk **TIGA (3)** mukasurat lampiran dan **LIMA (5)** soalan sebelum anda memulakan peperiksaan.*

**Instructions** : Answer **ALL** questions.

**[Arahan** : Jawab **SEMUA** soalan].

1. **Appendix/Lampiran** **[3 pages/mukasurat]**

Student may answer the questions either in **English** or **Bahasa Malaysia**.  
*[Pelajar boleh menjawab soalan dalam **Bahasa Inggeris** atau **Bahasa Malaysia**].*

Each questions must begin from a new page.  
*[Setiap soalan mestilah dimulakan pada mukasurat yang baru].*

In the event of any discrepancies, the English version shall be used.  
*[Sekiranya terdapat sebarang percanggahan pada soalan peperiksaan, versi Bahasa Inggeris hendaklah diguna pakai].*

Each student is allowed to bring an A4-sized sheet of self-prepared two-page summary note.

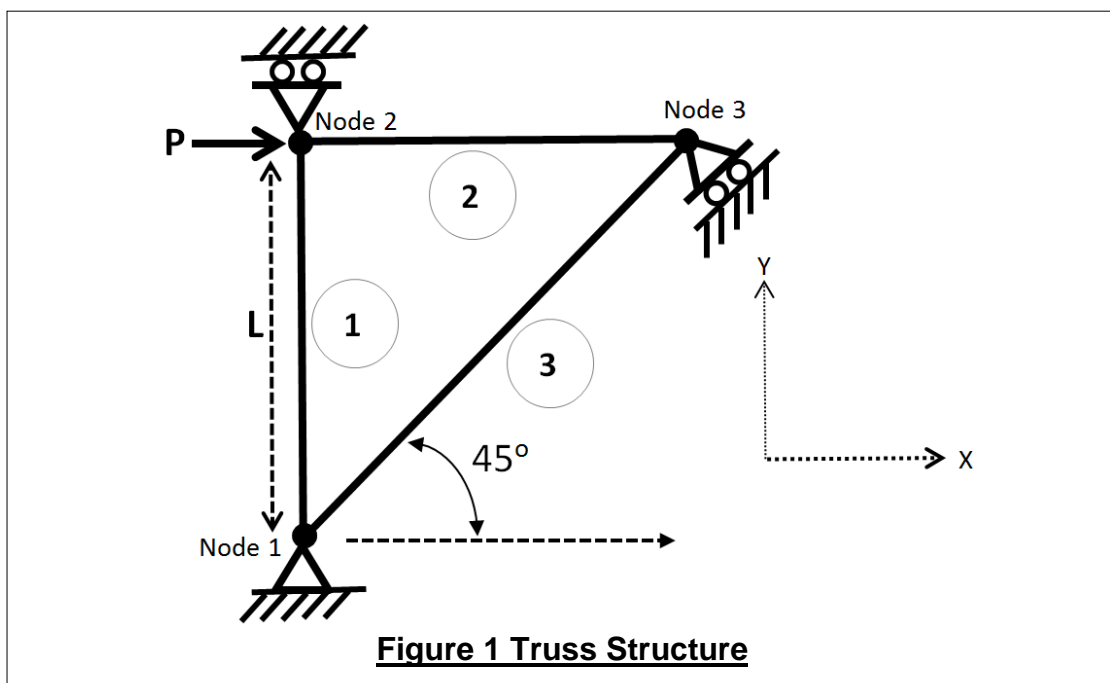
*[Setiap pelajar dibenarkan untuk membawa sehelai nota ringkasan bersaiz A4 yang mempunyai dua mukasurat yang ditulis sendiri].*

1. [a] Describe the general procedure for performing structural analysis using finite element method software. (3 marks)
- [b] List **5 advantages** of finite element method. (1 marks)
- [c] A structure is made of three trusses is shown in figure 1. It is loaded horizontally with force,  $P$  with a magnitude of 1,000 Newton at node 2. Node 1 is fixed at the anchor point. Node 2 is fixed vertically while node 3 is free to displace. The properties of the truss are given in **Table 1**. Find the answers of the following questions :
- (i) Global stiffness matrix of element 1
  - (ii) Global stiffness matrix of element 3
  - (iii) Global assembly matrix of the truss structure
  - (iv) Displacement of node 3 in horizontal direction

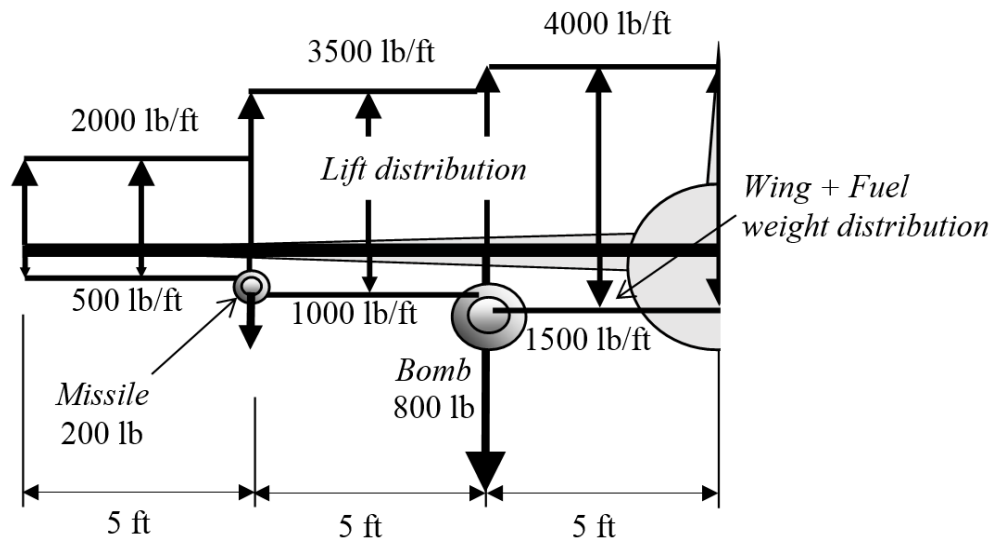
(16 marks)

Table 1 Truss properties

Parameter		Value	Unit
Elastic modulus	$E$	210,000	Pa
Cross sectional area	$A$	1	$m^2$
Length	$L$	10	m



2. Using **Figure 2** shown below, draw the shear load and bending moment diagrams of the half-wing while the aircraft is in flight.



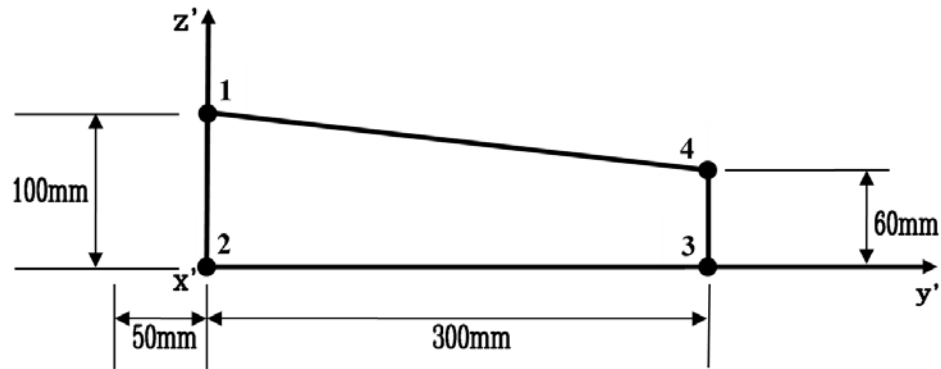
**Figure 2**

**(20 marks)**

-4-

3. Bending moments of  $M_y = -50 \text{ Nm}$  and  $M_z = -10 \text{ Nm}$  are applied on the idealized thin-walled 4 booms wing beam section shown in **Figure 3**.

Determine the axial stresses in all booms.

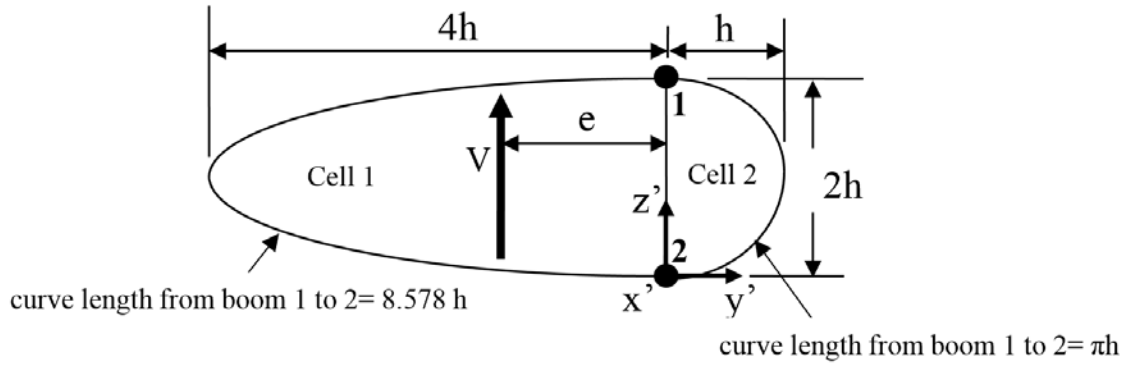


Area of booms 1, 2 & 3 =  $3000 \text{ mm}^2$   
Area of booms 4 =  $2000 \text{ mm}^2$

**Figure 3**

**(20 marks)**

4. Determine  $e$ , the shear center of the idealized thin-walled 2-boom beam section shown in **Figure 4**.



Original thickness of all walls =  $t$   
 Area of booms 1 & 2 =  $A$   
 Area of cell 1 =  $6.283 h^2$   
 Area of cell 2 =  $\frac{\pi h^2}{2}$

**Figure 4**

**(20 marks)**

5. Figure 5 shows a fuselage structure.

- Fuselage skins between the stringers are considered flat
- Structure is made of aluminum:

$$E = 10 \times 10^6 \text{ psi}; \quad \nu = 0.3; \quad \sigma_{\text{yield}} = 63 \text{ ksi}; \quad \sigma_{\text{ult}} = 74 \text{ ksi}$$

- Skin thickness,  $t_{\text{sk}}$  0.05 in
- Stringer thickness,  $t_{\text{st}}$  0.04 in

[a] Determine whether the skin and stringer can fail in buckling (including local buckling), given

- Maximum compressive load  $N_x$  1200 lb/in
- Frame/former spacing,  $L$  24 in
- Stringer spacing,  $W$  3 in

(5 marks)

[b] Optimize the skin-stringer (stiffened-panel/panel-strut) structure design by finding the appropriate frame and stringer spacings,  $L$  and  $W$  such that if buckling failure occurs, the skins, stringers and stiffened-panel structure should fail simultaneously (i.e. local and general/global buckling occurs at the same critical stress).

Design requirements:

- All stringer dimensions are fixed.
- Ratio  $L/W \gg 3$

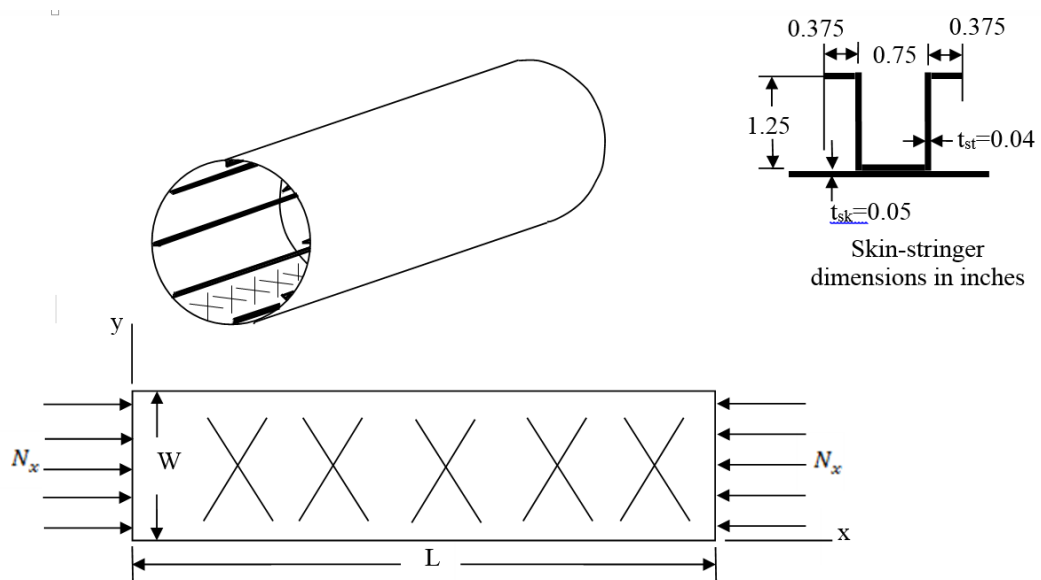


Figure 5

(15 marks)

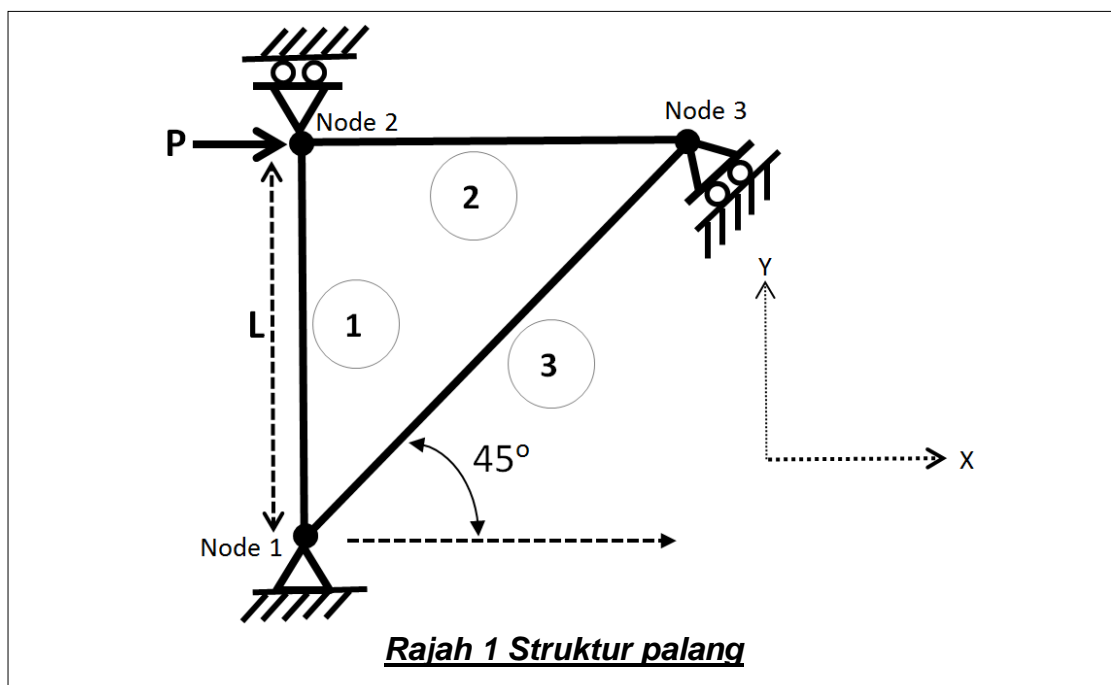
...7/-

SULIT

1. [a] Perihal tatacara am untuk melakukan analisa struktur dengan menggunakan perisian kaedah unsur terhingga. **(3 markah)**
- [b] Senaraikan **5 kelebihan** kaedah elemen terhingga. **(1 markah)**
- [c] Satu struktur yang terdiri daripada 3 palang yang serupa seperti yang ditunjukkan dalam **Rajah 1**. Beban  $P$  dikenakan pada nod 1 dengan magnitud daya berjumlah 1,000 Newton. Nod 1 ditambatkan pada penambat. Nod 2 ditambatkan secara menegak manakala nod 3 tidak ditambatkan. Sifat palang tersebut diberikan dalam **Jadual 1**. Cari jawapan kepada soalan berikut :
- (i) Matrik kekakuan global elemen 1
  - (ii) Matrik kekakuan global elemen 3
  - (iii) Matrik himpunan global struktur tersebut
  - (iv) Sesaran pada nod 3 dalam arah mendatar
- (16 markah)**

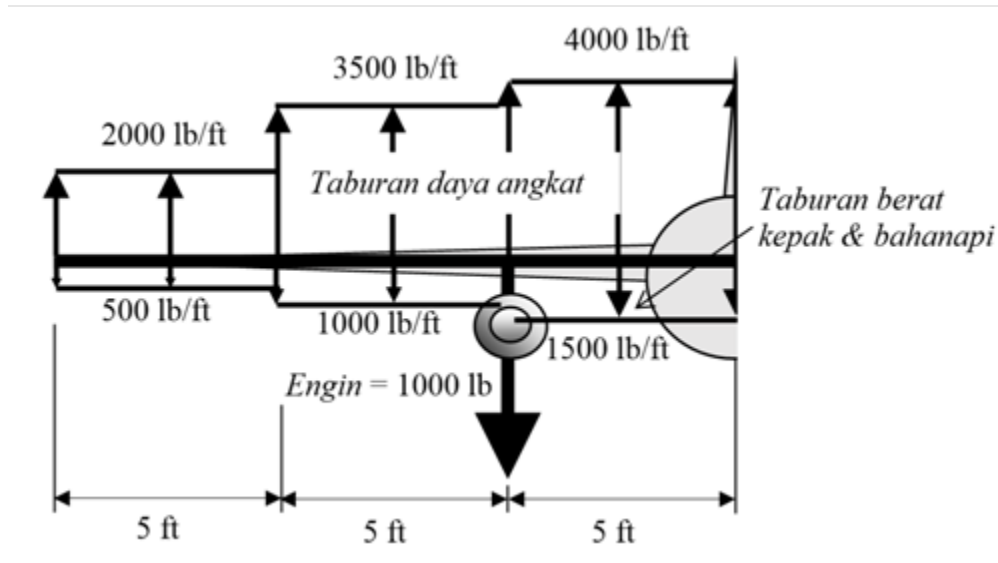
**Jadual 1 Sifat Palang**

Parameter		Nilai	Unit
Modulus kenyal	$E$	<b>210,000</b>	<b>Pa</b>
Luas keratan rentas	$A$	<b>1</b>	<b>m<sup>2</sup></b>
Panjang	$L$	<b>10</b>	<b>m</b>



3/-

2. Dengan menggunakan **Rajah 2** di bawah, lukiskan rajah beban ricih dan momen lentur kepak-separuh semasa pesawat yang sedang dalam penerbangan



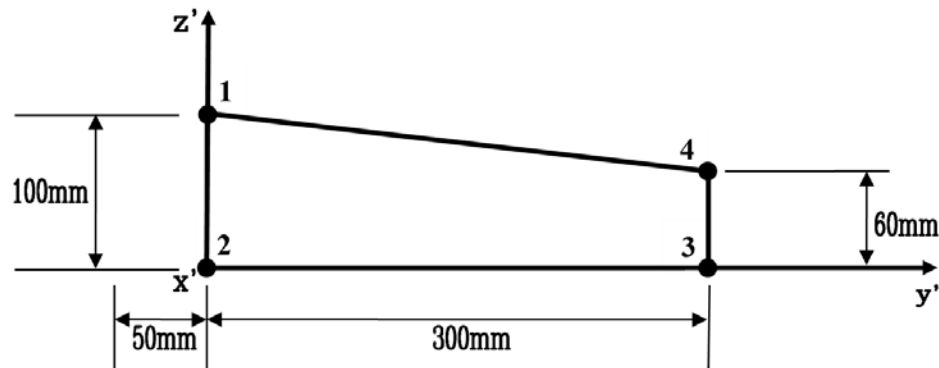
**Rajah 2**

**(20 markah)**



3. Momen lentur  $M_y = -50 \text{ kNm}$  dan  $M_z = 10 \text{ kNm}$  dikenakan ke atas keratan-rentas rasuk dinding-nipis 4 gelegar yang ditunjukkan di **Rajah 3**.

Tentukan tegasan paksi pada setiap gelegar.

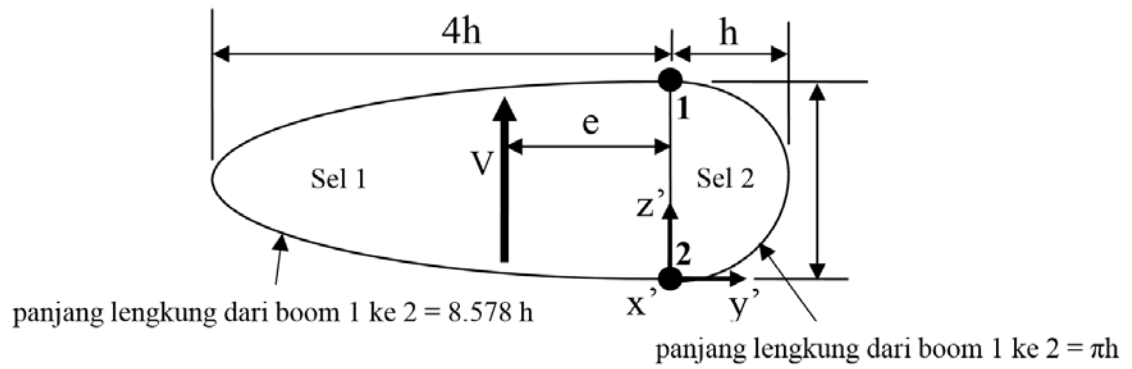


Keluasan gelegar 1, 2 & 3 =  $3000 \text{ mm}^2$   
Keluasan gelegar 4 =  $2000 \text{ mm}^2$

**Rajah 3**

**(20 markah)**

4. Tentukan  $e$ , pusat ricih rasuk 2-gelegar ideal yang ditunjukkan di **Rajah 4**.



Tebal asal semua dinding =  $t$   
 Keluasan gelegar 1 & 2 =  $A$   
 Keluasan sel 1 =  $6.283 h^2$   
 Keluasan sel 2 =  $\frac{\pi h^2}{2}$

**Rajah 4**

**(20 markah)**

5. **Rajah 5** menunjukkan struktur fuselaj.

- Kulit fuselaj di antara gelegar dianggap rata.
- Struktur dibuat dari aluminum:

$$E = 10 \times 10^6 \text{ psi}; \nu = 0.3; \sigma_{\text{yield}} = 63 \text{ ksi}; \sigma_{\text{ult}} = 74 \text{ ksi}$$

- Tebal kulit,  $t_{sk}$  0.05 in
- Tebal gelegar,  $t_{st}$  0.04 in

[a] Tentukan jika kulit dan gelegar boleh gagal secara lengkakan (termasuk lengkakan lokal), jika

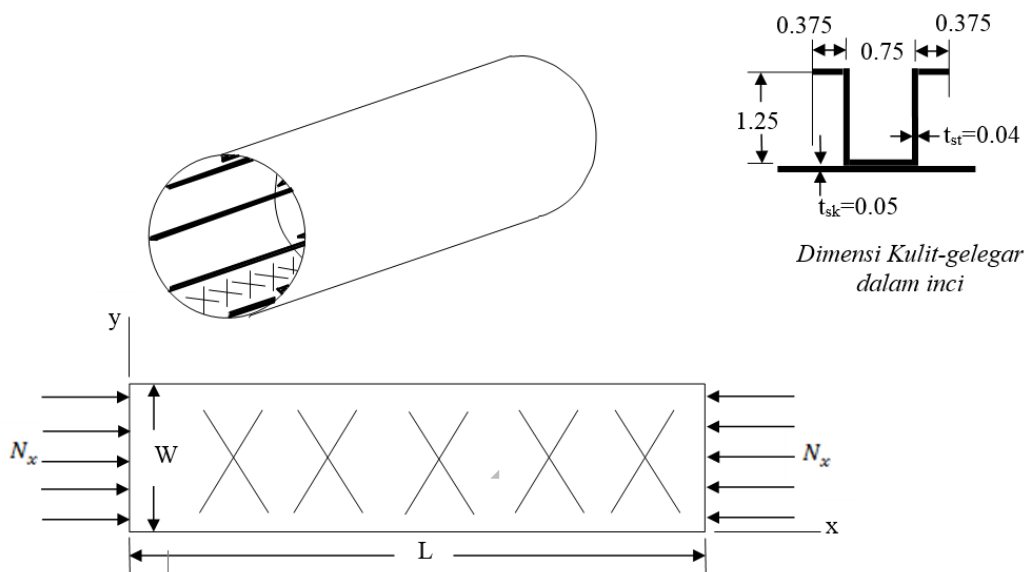
- Beban mampat maksimum,  $N_x$  1200 lb/in
- Jarak antara rusuk/bingkai,  $L$  24 in
- Jarak antara gelegar,  $W$  3 in

**(5 markah)**

[b] Optimumkan rekabentuk struktur kulit-gelegar dengan mencari jarak sesuai,  $L$  (antara rusuk ke rusuk) dan  $W$  (antara gelegar ke gelegar) di mana andai jika berlaku kegagalan secara lengkakan kulit, gelegar dan struktur kulit-gelegar, hendaklah gagal serentak (iaitu kegagalan lokal dan global berlaku pada tegasan kritikal yang sama).

Keperluan rekabentuk :

- Semua dimensi gelegar tidak berubah
- Nisbah  $L/W \gg 3$



**Rajah 5**

**(15 markah)**

### Equation for truss element stiffness in global coordinate system

$$k = \frac{EA}{L} \begin{matrix} & \begin{matrix} u_j & v_i & u_j & v_j \end{matrix} \\ \begin{matrix} l^2 & lm & -l^2 & -lm \\ lm & m^2 & -lm & -m^2 \\ -l^2 & -lm & l^2 & lm \\ -lm & -m^2 & lm & m^2 \end{matrix} \end{matrix}$$

Where

$$l = \cos\theta = \frac{X_j - X_i}{L}$$

and

$$m = \sin\theta = \frac{Y_j - Y_i}{L}$$

$$\sigma_x = \frac{P}{A} + \frac{-(M_z I_y + M_y I_{yz})y + (M_y I_z + M_z I_{yz})z}{I_y I_z - I_{yz}^2}$$

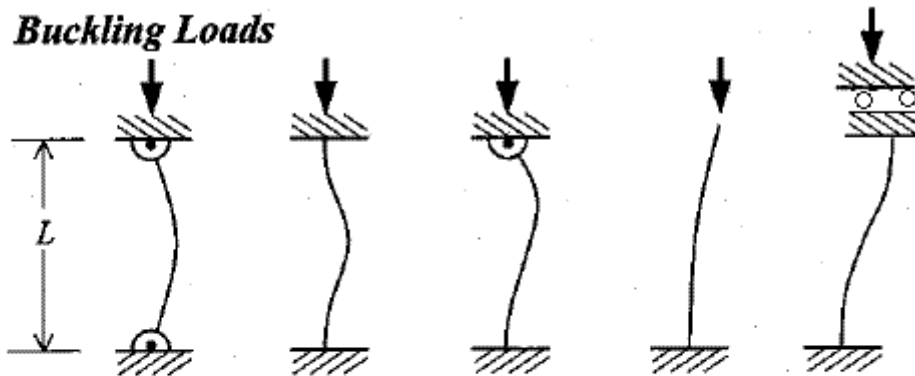
$$\Delta q = - \left[ \frac{(V_y I_y - V_z I_{yz})Q_z + (V_z I_z - V_y I_{yz})Q_y}{I_y I_z - I_{yz}^2} \right] \quad \theta = \frac{q}{2AG} \oint \frac{ds}{t}$$

$$P_{cr} = \frac{\pi^2 EI}{L_e^2}$$

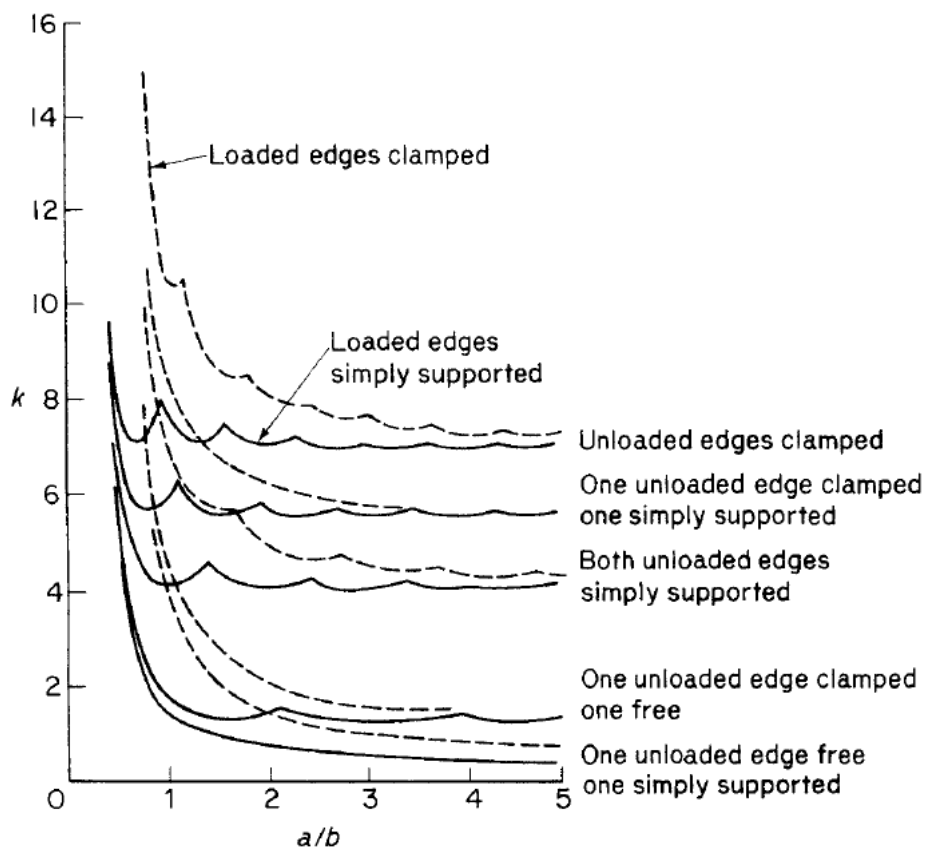
$$\sigma_{cr} = \frac{\pi^2 E}{(L_e / r)^2}$$

$$\sigma_{cr} = k \frac{\pi^2 E}{12(1-\nu^2)} \left( \frac{t}{b} \right)^2$$

**Buckling Loads**



Buckling Load	$\frac{\pi^2 EI}{L^2}$	$\frac{4\pi^2 EI}{L^2}$	$\frac{2.045\pi^2 EI}{L^2}$	$\frac{\pi^2 EI}{4L^2}$	$\frac{\pi^2 EI}{L^2}$
Effective Length $L_e$	$L$	$0.5L$	$0.699L$	$2L$	$L$



Equation for truss element stiffness in global coordinate system

$$k = \frac{EA}{L} \begin{bmatrix} l^2 & lm & -l^2 & -lm \\ lm & m^2 & -lm & -m^2 \\ -l^2 & -lm & l^2 & lm \\ -lm & -m^2 & lm & m^2 \end{bmatrix} \begin{matrix} u_i \\ v_i \\ u_j \\ v_j \end{matrix}$$

Where

$$l = \cos\theta = \frac{X_j - X_i}{L}$$

and

$$m = \sin\theta = \frac{Y_j - Y_i}{L}$$

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