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UNIVERSITI SAINS MALAYSIA

First Semester Examination  
2013/2014 Academic Session

December 2013/January 2014

**ESA461/2 – Flight Stability and Control II**  
***[Kawalan dan Kestabilan Pesawat II]***

Duration : 2 hours  
*Masa : 2 jam*

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Please check that this paper contains **THIRTEEN (13)** printed pages, **THREE (3)** pages appendix and **FIVE(5)** questions before you begin the examination.

*[Sila pastikan bahawa kertas soalan ini mengandungi **TIGA BELAS (13)** mukasurat bercetak, **TIGA (3)** mukasurat lampiran dan **LIMA (5)** soalan sebelum anda memulakan peperiksaan].*

**Instructions** : **Part A** : Choose **ONE (1)** question **ONLY**. **Part B**: Answer **ALL** questions.

**Arahan** : **BAHAGIAN A** : Pilih **SATU (1)** soalan **SAHAJA**.

**BAHAGIAN B** : Jawab **SEMUA** soalan

1. **Appendix A/Lampiran A[FORMULA]:** [1 page/mukasurat]

2. **Appendix B/Lampiran B** [2 pages/mukasurat]

Answer all questions in **English** OR **Bahasa Malaysia**.

*[Menjawab semua soalan dalam **Bahasa Inggeris ATAU Bahasa Malaysia**].*

Answer to each question must begin from a new page.

*[Jawapan untuk setiap soalan mestilah dimulakan pada mukasurat yang baru].*

In the event of any discrepancies, the English version shall be used.

*[Sekiranya terdapat sebarang percanggahan pada soalan peperiksaan, versi Bahasa Inggeris hendaklah diguna pakai].*

**PART A:** Choose **ONE (1)** question **ONLY**  
**BAHAGIAN A :** Pilih **SATU (1)** soalan **SAHAJA**

1. [a] Briefly explain about directional stability and state the conditions required for an aircraft to remain stable in this motion. (6 marks)

- [b] Vertical tail is one of the most influential components in directional stability. Its contribution to the aircraft's directional stability can be calculated from the following equation

$$C_{n\dot{\beta}_v} = V_v \eta_v C_{L_{\alpha v}} \left( 1 + \frac{d\sigma}{d\beta} \right)$$

Where,

$$\eta_v \left( 1 + \frac{d\sigma}{d\beta} \right) = 0.724 + 3.06 \frac{S_v/S}{1 + \cos \Lambda_{c/4w}} + 0.4 \frac{z_w}{d} + 0.009AR_w$$

Let say a model of an airplane is tested in a wind tunnel with vertical tail off. Contributions of various components give  $C_{n\dot{\beta}} = -0.001 \text{ deg}^{-1}$ . If the vertical tail is to be positioned at a point on the aft end of the fuselage giving a tail length of  $4.8 \text{ m}$ , estimate the required vertical tail area to give an overall  $C_{n\dot{\beta}} = 0.001 \text{ deg}^{-1}$ ? Given  $C_{L_{\alpha v}} = 0.0454$ ,  $\Lambda_{c/4w} = 0$ ,  $S = 18 \text{ m}^2$ ,  $b = 10.6 \text{ m}$  and the wing is set at the middle of the fuselage.

(14 marks)

- [c] Explain why deflecting the ailerons produce a yawing moment.

(5 marks)

- [a] Terangkan dengan ringkas tentang kestabilan berarah dan nyatakan keadaan yang diperlukan untuk sebuah kapalterbang kekal stabil dalam pergerakan ini.

(6 markah)

- [b] Ekor menegak merupakan salah satu komponen yang berpengaruh dalam kestabilan berarah. Sumbangannya kepada kestabilan berarah pesawat boleh dikira dengan menggunakan formula berikut

$$C_{n_{\beta v}} = V_v \eta_v C_{L_{\alpha v}} \left( 1 + \frac{d\sigma}{d\beta} \right)$$

Di mana

$$\eta_v \left( 1 + \frac{d\sigma}{d\beta} \right) = 0.724 + 3.06 \frac{S_v/S}{1 + \cos \Lambda_{c/4w}} + 0.4 \frac{z_w}{d} + 0.009 AR_w$$

Katakan sebuah model pesawat tanpa ekor menegak diuji dalam sebuah terowong angin. Sumbangan pelbagai komponen pesawat tersebut memberikan  $C_{n_{\beta}} = -0.001 \text{ deg}^{-1}$ . Jika ekor menegak diletakkan pada bahagian belakang pesawat iaitu di hujung fuislaj dengan panjang ekor adalah 4.8 m, anggarkan luas permukaan ekor menegak yang diperlukan untuk memberi kestabilan keseluruhan  $C_{n_{\beta}} = 0.001 \text{ deg}^{-1}$ . Diberi  $C_{L_{\alpha v}} = 0.0454$ ,  $\Lambda_{c/4w} = 0$ ,  $S = 18 \text{ m}^2$ ,  $b = 10.6 \text{ m}$  dan pesawat diletakkan pada pertengahan fuislaj.

(14 markah)

- [c] Terangkan mengapa dengan memesonkan aileron menghasilkan momen rewang.

(5 markah)

2. [ a ] Briefly explain about asymmetric power and state the conditions required for an aircraft to remain stable in this motion. (4 marks)
- [b] For the twin engine airplane shown in **Figure 1**, determine the rudder size to control the airplane if one engine needs to be shut down. Use the following flight information and **Figure 2** to solve this problem.

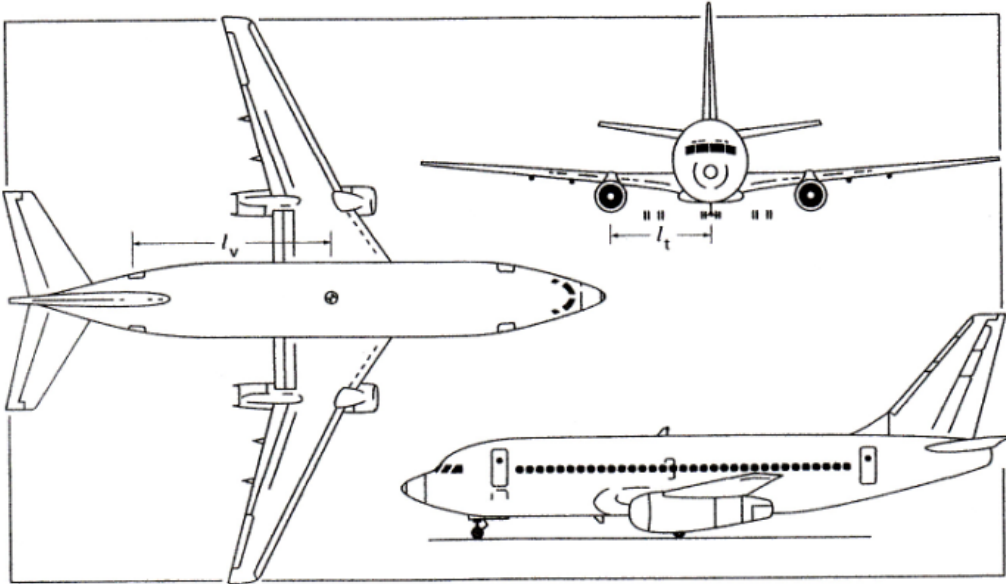


Figure 1

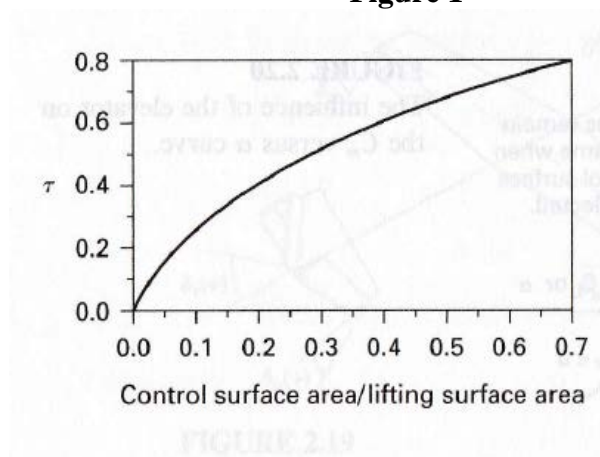
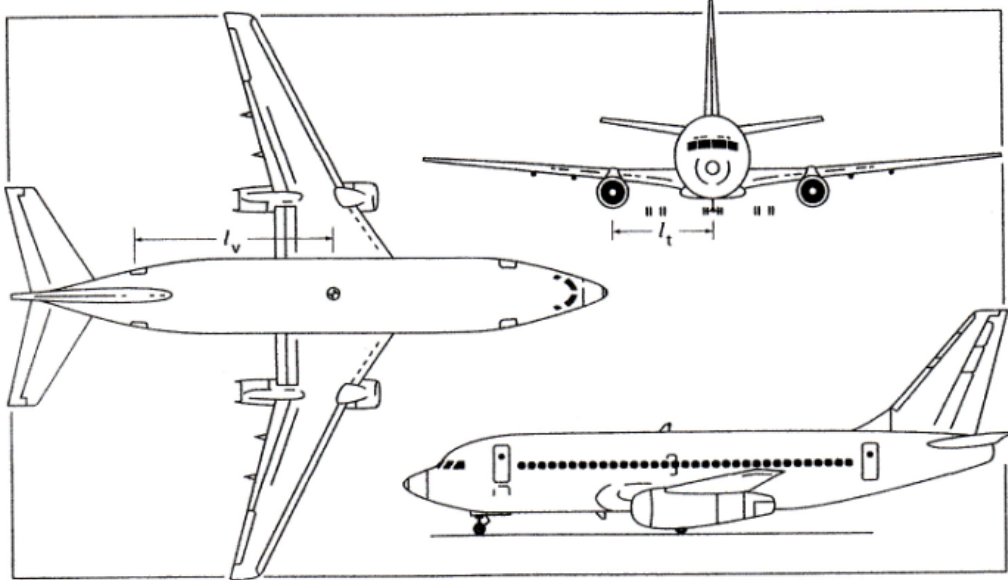


Figure 2

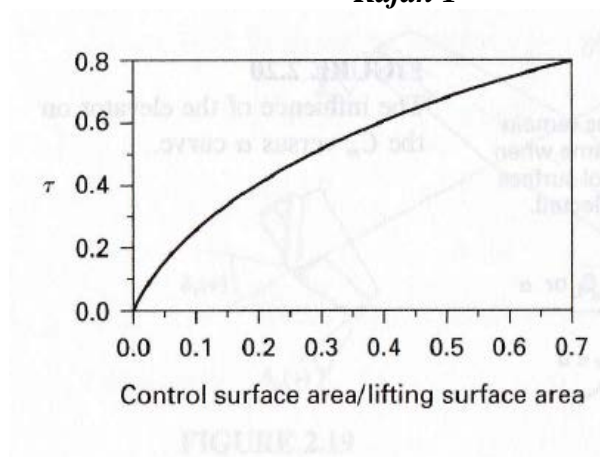
Wing:  $S = 980 \text{ ft}^2$ ,  $b = 93 \text{ ft}$   
 Vertical tail:  $S_v = 330 \text{ ft}^2$ ,  $AR_v = 4.3$ ,  $l_v = 37 \text{ ft}$ ,  $\eta_v = 1.0$ ,  $C_{l_{rv}} = 0.1/\text{deg}$   
 Rudder:  $\delta_r = \pm 15^\circ$   
 Propulsion:  $T = 14\,000 \text{ lb}$  each  $y_T = 16 \text{ ft}$   
 Flight condition:  $V = 250 \text{ ft/s}$ ,  $\rho = 0.002378 \text{ slug/ft}^3$

(21 marks)

- [a] Terangkan dengan ringkas tentang kuasa asimetri dan nyatakan keadaan yang diperlukan untuk sebuah kapal terbang kekal stabil dalam pergerakan ini. (4 markah)
- [b] Untuk kapal terbang dengan enjin berkembar seperti dalam **Rajah 1**, tentukan saiz kemudi untuk mengawal kapal terbang jika salah satu daripada enjin tersebut perlu dimatikan. Gunakan informasi penerbangan berikut dengan **Rajah 2** untuk menyelesaikan masalah ini.



Rajah 1



Rajah 2

Sayap:  $S = 980 \text{ ft}^2$ ,  $b = 93 \text{ ft}$   
 Ekor Tegak:  $S_v = 330 \text{ ft}^2$ ,  $AR_v = 4.3$ ,  $l_v = 37 \text{ ft}$ ,  $\eta_v = 1.0$ ,  $C_{l_{\alpha v}} = 0.1/\text{deg}$   
 Kemudi:  $\delta_r = \pm 15^\circ$   
 Pendorongan:  $T = 14\,000 \text{ lb}$  each  $y_T = 16 \text{ ft}$   
 Keadaan penerbangan:  $V = 250 \text{ ft/s}$ ,  $\rho = 0.002378 \text{ slug/ft}^3$

(21 markah)

**PART B:** Answer **ALL** questions.

**BAHAGIAN B :** Jawab **SEMUA** soalan.

3. [a] The stability coefficient  $C_{l_r}$  is the change in roll moment due to the yawing rate. What cause this effect and how does the vertical tail contribute to the  $C_{l_r}$ ? A simple discussion with appropriate sketches is required for this problem. **(4 marks)**
- [b] The stability coefficient  $C_{l_{\delta_r}}$  is the change in roll moment coefficient due to rudder deflection. Again, explain how this effect occurs. **(1 marks)**
- [c] Using the geometric data given below and in **Figure 3**, estimate  $C_{l_p}$  and  $C_{n_r}$ . The roll moment coefficient due to rolling rate,  $C_{l_p}$  and yaw moment coefficient due to yawing rate,  $C_{n_r}$  can be formulated from the following equations respectively.

$$C_{l_p} = -\frac{C_{L_{\alpha}}}{12} \frac{1 + 3\lambda}{1 + \lambda}$$

$$C_{n_r} = -2\eta_v V_v \left(\frac{l_v}{b}\right) C_{L_{\alpha v}}$$

**(20 marks)**

Wing:  $S = 232 \text{ ft}^2$ ,  $b = 36 \text{ ft}$ ,  $C_{L_{\alpha w}} = 0.1/\text{deg}$

Vertical tail:  $S_v = 37.4 \text{ ft}^2$ ,  $l_v = 18.5 \text{ ft}$ ,  $C_{L_{\alpha v}} = 0.1/\text{deg}$ ,  $\eta_v = 1$

Wing:  $C_{L_{\alpha_w}} = 0.1/\text{deg}$   $C_{mac_w} = -0.02/\text{deg}$   
 $\alpha_{Lo} = -1.0^\circ$

Tail:  $C_{L_{\alpha_w}} = 0.1/\text{deg}$   $C_{mac_w} = 0.00$   
 $\alpha_{Lo} = 0^\circ$

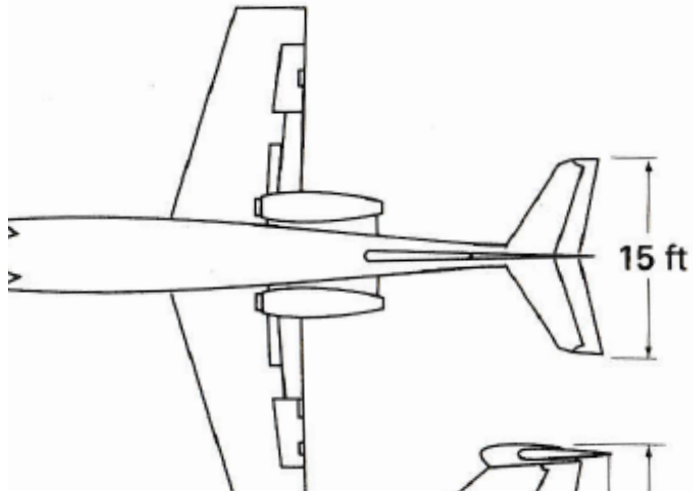


Figure 3

- [a] Kestabilan pekali  $C_{l_r}$  adalah perubahan dalam masa roll disebabkan oleh kadar rewang. Apa yang menyebabkan kesan ini dan bagaimana ekor menegak menyumbang kepada pekali  $C_{l_r}$ ? Satu perbincangan ringkas dengan lakaran yang sesuai diperlukan untuk masalah ini. (4 markah)
- [b] Pekali kestabilan  $C_{l_{\dot{\alpha}}}$  adalah perubahan pekali momen roll yang disebabkan oleh kemudi pesongan. Sekali lagi, menjelaskan bagaimana kesan ini berlaku. (1 markah)
- [c] Menggunakan data geometri yang diberikan di bawah dan di dalam **Rajah 3**, anggaran  $C_{l_p}$  and  $C_{n_r}$ . Pekali momen roll yang disebabkan oleh kadar roll,  $C_{l_p}$  dan pekali momen rewang yang disebabkan oleh kadar rewang,  $C_{n_r}$  boleh dirumuskan daripada persamaan berikut.

$$C_{l_p} = -\frac{C_{l_{\dot{\alpha}}}}{12} \frac{1 + 3\lambda}{1 + \lambda}$$

$$C_{n_r} = -2\eta_v V_v \left(\frac{l_v}{b}\right) C_{l_{\dot{\alpha}}}$$

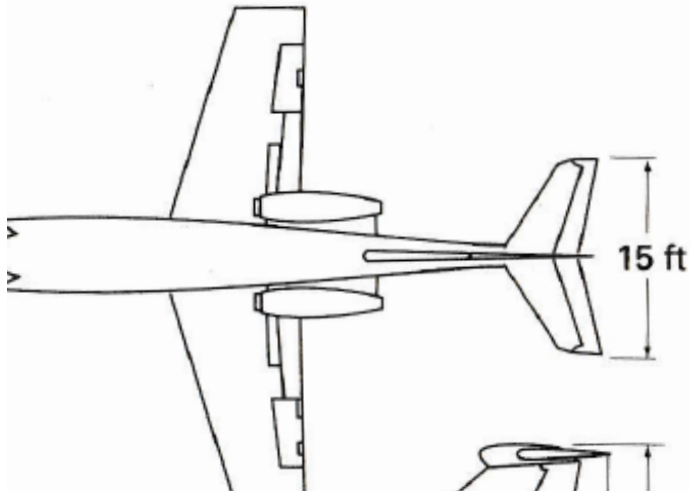
(20 markah)

Sayap:  $S = 232 \text{ ft}^2$ ,  $b = 36 \text{ ft}$ ,  $C_{l_{\dot{\alpha}}} = 0.1/\text{deg}$   
 Ekor Tegak:  $S_v = 37.4 \text{ ft}^2$ ,  $l_v = 18.5 \text{ ft}$ ,  $C_{l_{\dot{\alpha}}} = 0.1/\text{deg}$ ,  $\eta_v = 1$



Wing:  $C_{L\alpha_w} = 0.1/\text{deg}$   $C_{mac_w} = -0.02/\text{deg}$   
 $\alpha_{Lo} = -1.0^\circ$

Tail:  $C_{L\alpha_w} = 0.1/\text{deg}$   $C_{mac_w} = 0.00$   
 $\alpha_{Lo} = 0^\circ$



*Rajah 3*

4. Assuming the cruciform finned model in Figure 4 is mounted in a wind tunnel so that it is constrained to a pure yawing motion. The model is displaced from its trim position by  $10^\circ$  and then released. Neglect the fuselage and  $\beta$  contribution and assume  $S = \pi D^2/4$ .

[a] Find the time for the motion to damp to half its initial amplitude.

(15 marks)

[b] What is the period of the motion.

(10 marks)

$D = \text{Characteristic length} = 5.0$

Tail surfaces are flat plates:  $I_z = 5.0 \times 10^{-2} \text{ kgm}^2$ ,  $S = \pi D^2/4$

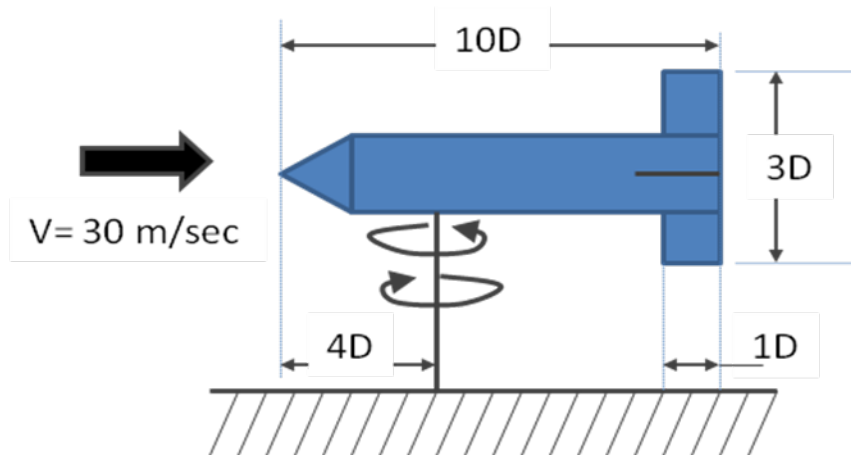


Figure 4

Dengan andaian model bersirip bentuk 'Cruci' seperti di **Rajah 4** yang dipasang di dalam terowong angin supaya ianya berlaku pergerakan rewang asli. Model yang disasarkan dari kedudukan cantas dengan  $10^\circ$  dan kemudian dibebaskan. Abaikan fuslaj dan  $\beta$  sumbangan dan anggapkan  $S = \pi D^2/4$ .

[a] Tentukan masa bagi pergerakan menjadi rendam untuk setengah amplitude awal.

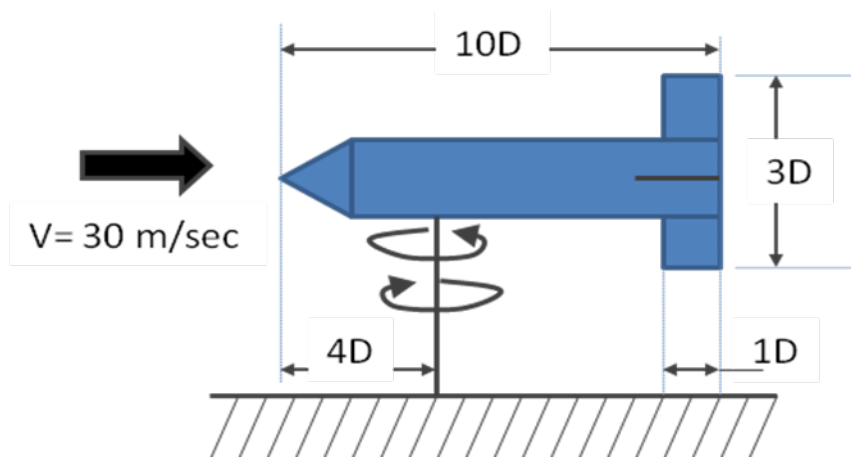
(15 markah)

[b] Apakah tempoh pergerakan.

(10 markah)

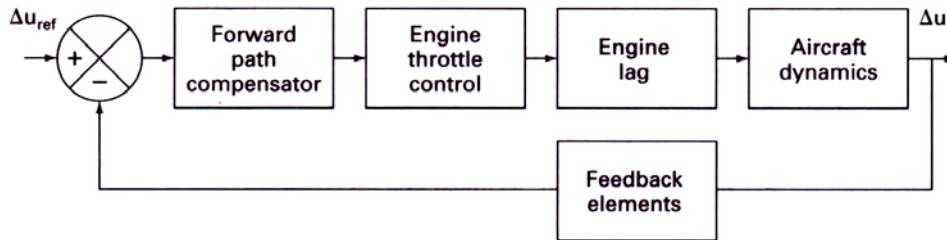
$D = \text{Panjang Kriteria} = 5.0$

Permukaan ekor adalah permukaan rata:  $I_z = 5.0 \times 10^{-2} \text{kgm}^2$ ,  $S = \pi D^2/4$



**Rajah 4**

5. Examine the performance characteristics of a speed control autopilot similar to the one shown in **Figure 5** for the STOL transport included in **Appendix A**. The transfer functions for the throttle servo, engine lag, forward path compensation, and the feedback elements follow:



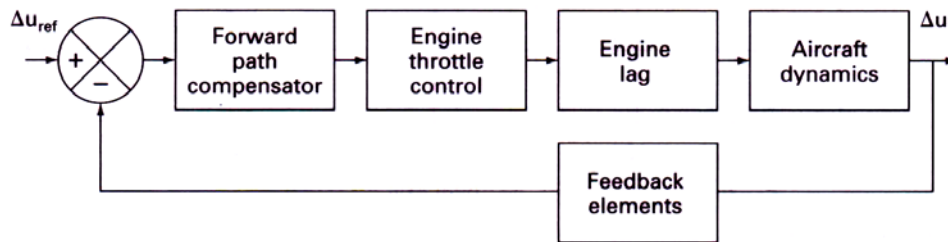
**Figure 5**

$$G_{Throttle}(s) = \frac{10}{s+10}, G_{enginelag}(s) = \frac{1}{s+0.1},$$

$$G_c(s) = 1 + \frac{0.1}{s} = \frac{k_a(s+0.1)}{s}, H = 10s + 1$$

- [a] Find the loop transfer function  $G(s)H(s)$  **(10 marks)**
- [b] Using unit step response, determine the gains by sketch the graph time vs amplitude. **(10 marks)**
- [c] Discuss, how to improve the performance of this system. **(5 marks)**

Kaji ciri-ciri prestasi kelajuan kawalan autopilot yang sama seperti yang ditunjukkan dalam **Rajah 5** pengangkutan STOL yang disertakan dalam **Lampiran A**. Berikut adalah rangkap pindah bagi servo pendikit, lag enjin, kompensator laluan hadapan dan elemen suapbalik.



**Rajah 5**

$$G_{Throttle}(s) = \frac{10}{s+10}, G_{enginelag}(s) = \frac{1}{s+0.1},$$

$$G_c(s) = 1 + \frac{0.1}{s} = \frac{k_a(s+0.1)}{s}, H = 10s + 1$$

- [a] Tentukan gelung rangkap pindah  $G(s)H(s)$  (10 markah)
- [b] Tentukan gandar dengan memplot graf masa berlawanan dengan amplitud. (10 markah)
- [c] Bincangkan bagaimana untuk meningkatkan prestasi dalam sistem ini. (5 markah)

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## APPENDIX A/ LAMPIRAN A

## Geometric, Mass, and Aerodynamic Characteristic of Selected Airplanes

$b$ Wing span	$C_{L_\alpha} = \frac{\partial C_L}{\partial \alpha} \text{ (rad}^{-1}\text{)}$
$\bar{c}$ Mean chord	$C_{L_{\dot{\alpha}}} = \frac{\partial C_L}{\partial \left( \frac{\dot{\alpha} \bar{c}}{2u_0} \right)} \text{ (rad}^{-1}\text{)}$
$C_L = \frac{L}{QS}$	
$C_{L_M} = \frac{\partial C_L}{\partial M}$	$C_{l_{\delta_a}} = \frac{\partial C_l}{\partial \delta_r} \text{ (rad}^{-1}\text{)}$
$C_{L_{\delta_e}} = \frac{\partial C_L}{\partial \delta_e} \text{ (rad}^{-1}\text{)}$	$C_{l_{\delta_r}} = \frac{\partial C_l}{\partial \delta_r} \text{ (rad}^{-1}\text{)}$
$C_D = \frac{D}{QS}$	$C_n = \frac{N}{Q S b}$
$C_{D_\alpha} = \frac{\partial C_D}{\partial \alpha} \text{ (rad}^{-1}\text{)}$	$C_{n_\beta} = \frac{\partial C_n}{\partial \beta} \text{ (rad}^{-1}\text{)}$
$C_{D_M} = \frac{\partial C_D}{\partial M}$	$C_{n_r} = \frac{\partial C_n}{\partial (pb/2u_0)} \text{ (rad}^{-1}\text{)}$
$C_{D_{\delta_e}} = \frac{\partial C_D}{\partial \delta_e} \text{ (rad}^{-1}\text{)}$	$C_{n_r} = \frac{\partial C_n}{\partial (rb/2u_0)} \text{ (rad}^{-1}\text{)}$
$C_m = \frac{M}{QS\bar{c}}$	$C_{m_{\dot{\alpha}}} = \frac{\partial C_m}{\partial (\dot{\alpha} \bar{c} / 2u_0)} \text{ (rad}^{-1}\text{)}$
$C_{m_\alpha} = \frac{\partial C_m}{\partial \alpha} \text{ (rad}^{-1}\text{)}$	$C_{m_M} = \frac{\partial C_m}{\partial M}$
$C_y = \frac{Y}{QS}$	$C_{m_q} = \frac{\partial C_m}{\partial (q\bar{c}/2u_0)} \text{ (rad}^{-1}\text{)}$
$C_{y_\beta} = \frac{\partial C_y}{\partial \beta} \text{ (rad}^{-1}\text{)}$	$C_{n_{\delta_a}} = \frac{\partial C_n}{\partial \delta_a} \text{ (rad}^{-1}\text{)}$
$C_{y_{\delta_r}} = \frac{\partial C_y}{\partial \delta_r} \text{ (rad}^{-1}\text{)}$	$C_{n_{\delta_r}} = \frac{\partial C_n}{\partial \delta_r} \text{ (rad}^{-1}\text{)}$
$C_l = \frac{L}{Q S b}$	$I_x$ Rolling moment of inertia
$C_{l_\beta} = \frac{\partial C_l}{\partial \beta} \text{ (rad}^{-1}\text{)}$	$I_y$ Pitching moment of inertia
$C_{l_p} = \frac{\partial C_l}{\partial (pb/2u_0)} \text{ (rad}^{-1}\text{)}$	$I_z$ Yawing moment of inertia
$C_{l_r} = \frac{\partial C_l}{\partial (rb/2u_0)} \text{ (rad}^{-1}\text{)}$	$I_{xz}$ Product of inertia about $xz$ axis
	$M$ Mach number
	$Q$ Dynamic pressure
	$S$ Wing planform area
	$u_0$ Reference flight speed

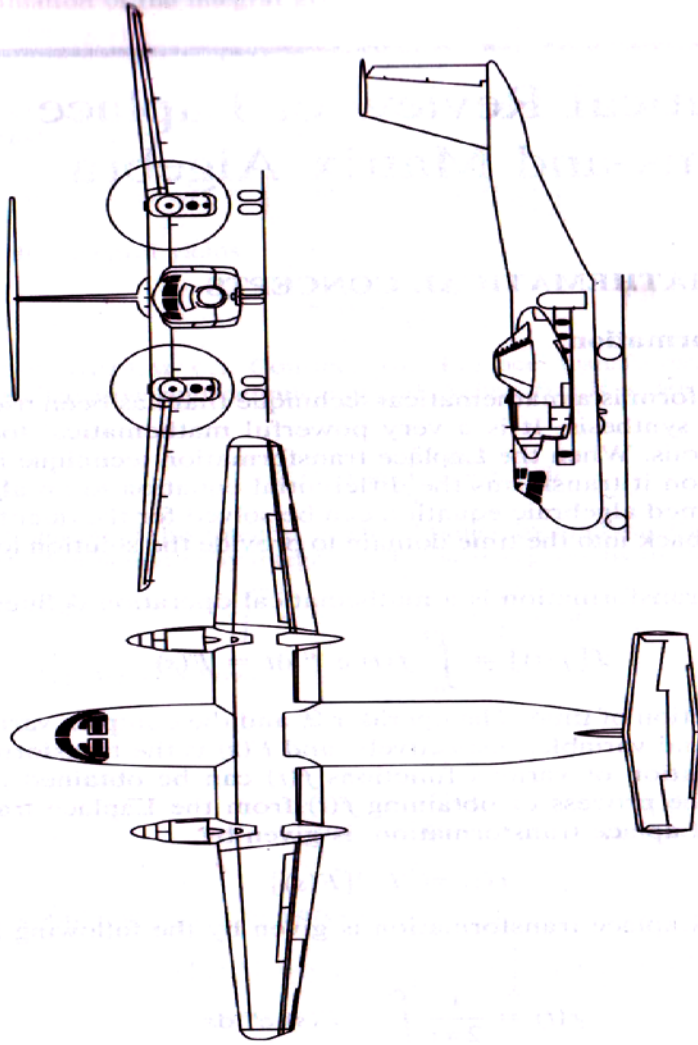
## APPENDIX B /LAMPIRANB

## STOL Transport Reference data

**TABLE B.28**  
**STOL Transport**

	$C_L$	$C_D$	$C_{L\alpha}$	$C_{D\alpha}$	$C_{m\alpha}$	$C_{L\dot{\alpha}}$	$C_{m\dot{\alpha}}$	$C_{Lq}$	$C_{mq}$	$C_{L\dot{q}}$	$C_{m\dot{q}}$	$C_{Lr}$	$C_{D_r}$	$C_{M_r}$	$C_{L\dot{r}}$	$C_{m\dot{r}}$
Longitudinal																
M = 0.14																
Sea level	1.5	0.127	5.24	0.67	-0.78	1.33	-6.05	7.83	-35.6	0	0	0	0	0	0.465	-2.12
M = 0.37																
10,000 ft	0.3	0.036	5.24	0.67	-0.78	1.33	-6.05	7.83	-35.6	0	0	0	0	0	0.465	-2.12
Lateral																
M = 0.14																
Sea level	$C_{y\beta}$	$C_{l\beta}$	$C_{r\beta}$	$C_{l\dot{\beta}}$	$C_{r\dot{\beta}}$	$C_{l\ddot{\beta}}$	$C_{r\ddot{\beta}}$	$C_{l\dot{r}}$	$C_{r\dot{r}}$	$C_{l\ddot{r}}$	$C_{r\ddot{r}}$	$C_{l\dot{q}}$	$C_{r\dot{q}}$	$C_{l\dot{r}}$	$C_{r\dot{r}}$	$C_{l\dot{q}}$
M = 0.37																
10,000 ft	-0.362	-0.125	0.101	-0.53	-0.283	0.410	-0.188	0.20	0	-0.233	-0.024	0.107				
M = 0.37																
10,000 ft	-0.362	-0.125	0.101	-0.53	-0.037	0.113	-0.171	0.20	0	-0.233	-0.024	0.107				

Note: All derivatives are per radian.



**Center of gravity and  
mass characteristics**

$W = 40,000$  lbs.  
 CG at 25% MAC  
 $I_x = 273,000$  Slug-ft<sup>2</sup>  
 $I_y = 215,000$  Slug-ft<sup>2</sup>  
 $I_z = 447,000$  Slug-ft<sup>2</sup>  
 $I_{xz} = 0$

**Reference geometry**

$S = 945$  ft<sup>2</sup>  
 $b = 96$  ft  
 $\bar{c} = 10.1$  ft