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UNIVERSITI SAINS MALAYSIA

First Semester Examination  
2013/2014 Academic Session

December 2013/January 2014

**ESA 321/3 – Aerospace Structure**  
*[Struktur Aeroangkasa]*

Duration : 3 hours  
*Masa : 3 jam*

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Please ensure that this paper contains **EIGHT (8)** printed pages, **TWO (2)** pages appendix and **FIVE (5)** questions before you begin examination.

*Sila pastikan bahawa kertas soalan ini mengandungi **LAPAN (8)** mukasurat bercetak, **DUA (2)** mukasurat lampiran dan **LIMA (5)** soalan sebelum anda memulakan peperiksaan.*

**Instructions** : Answer **ALL** questions.

**Arahan** : Jawab **SEMUA** soalan.

1. **Appendix/Lampiran** **[2 pages/mukasurat]**

Student may answer the questions either in **English or Bahasa Malaysia**.

*Pelajar boleh menjawab soalan dalam **Bahasa Inggeris atau Bahasa Malaysia**.*

Each questions must begin from a new page.

*Setiap soalan mestilah dimulakan pada mukasurat yang baru.*

In the event of any discrepancies, the English version shall be used.

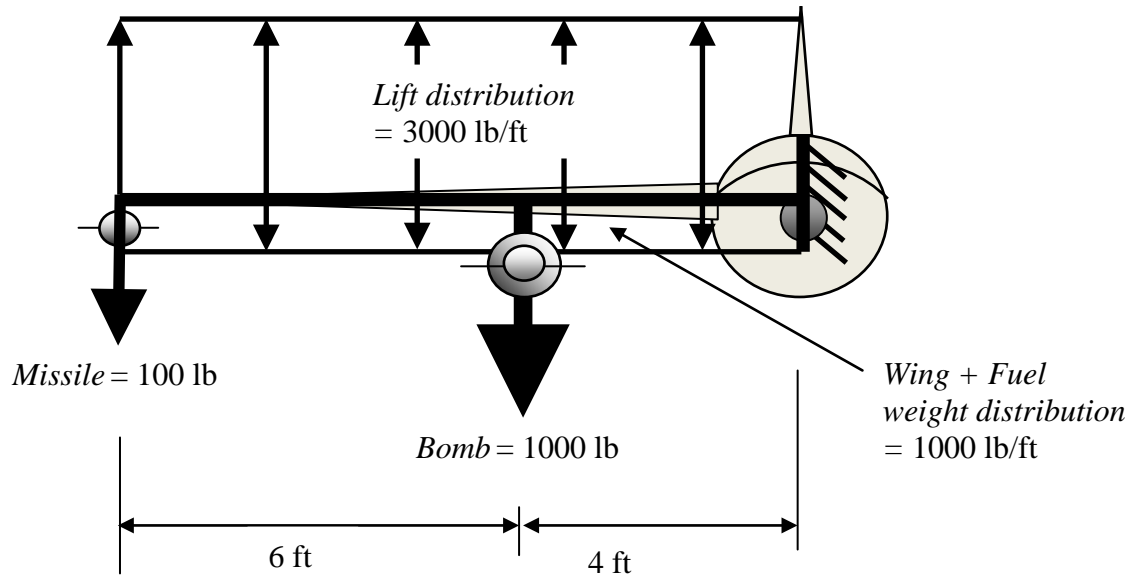
*Sekiranya terdapat sebarang percanggahan pada soalan peperiksaan, versi Bahasa Inggeris hendaklah diguna pakai.*

Answer **ALL** questions.

Jawab **SEMUA** soalan.

1. Using **Figure 1** shown below, draw the load, shear and bending moment diagram.

Dengan menggunakan **Rajah 1** di bawah, lukiskan rajah beban, ricih dan momen lentur.



**Figure 1**

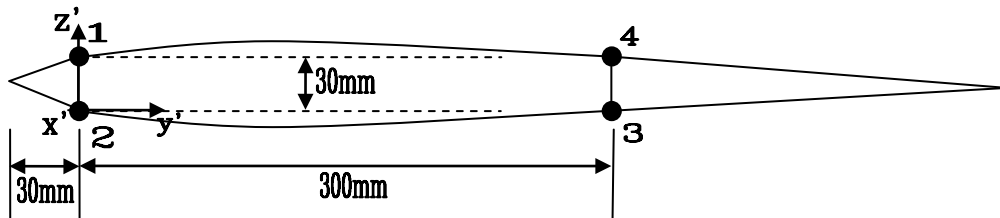
(20 marks/markah)

2. Bending moments of  $M_y = -50 \text{ kNm}$  and  $M_z = 10 \text{ kNm}$  are applied on the idealized thin-walled 4 booms wing beam section shown in **Figure 2**.

Determine the axial stresses in all booms.

*Momen lentur  $M_y = -50 \text{ kNm}$  dan  $M_z = 10 \text{ kNm}$  dikenakan ke atas keratan–rentas rasuk dinding-nipis 4 gelegar yang ditunjukkan di **Rajah 2**.*

*Tentukan tegasan paksi pada setiap gelegar.*



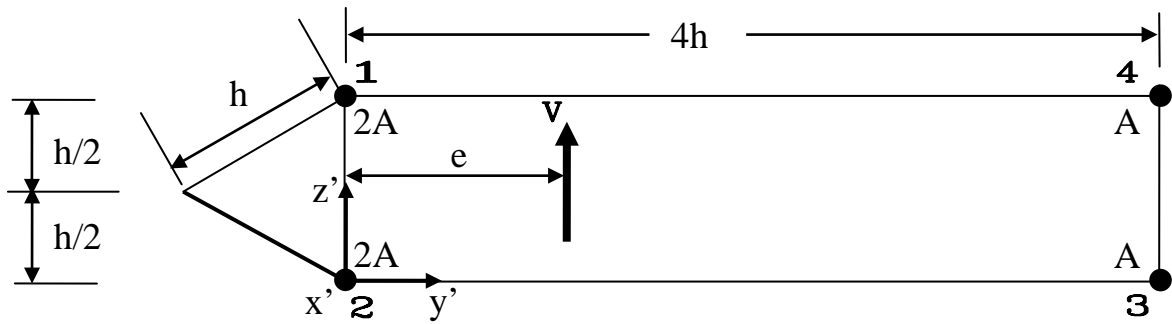
Area of booms /Luas gelegar,  
 $A_1 = A_2 = A_4 = 3000 \text{ mm}^2$   
 $A_3 = 2000 \text{ mm}^2$

**Figure 2**  
**Rajah 2**

(20 marks/markah)

3. Determine  $e$ , the shear center of the idealized thin-walled 4-boom wing beam section shown in **Figure 3**.

Tentukan  $e$ , pusat ricih rasuk kotak 4-gelegar ideal yang ditunjukkan di **Rajah 3**.



Thickness of all walls/ *Tebal semua dinding* =  $t$

Area of booms/ *Luas gelegar*

$$A_1 = A_2 = 2A$$

$$A_3 = A_4 = A$$

**Figure 3**

**Rajah 3**

(20 marks/markah)

4. **Figure 4** shows 2-spar wing structure.

*Rajah 4* menunjukkan struktur sayap 2-spar.

- Wing box skins are considered flat/ *Kulit kotak sayap dianggap rata*
- Structure made of aluminum/*Struktur dibuat dari aluminum:*  
 $E = 10 \times 10^6$  psi;  $\nu = 0.32$ ;  $\sigma_{\text{yield}} = 37$  ksi;  $\sigma_{\text{ult}} = 42$  ksi
- Max compressive load/*Beban mampat maks,  $N_x$*  1200 lb/in
- Skin thickness/ *Tebal kulit,  $t_{sk}$*  0.05 in
- Stringer thickness /*Tebal gelegar,  $t_{st}$*  0.04 in
- Rib spacing/ *jarak rusuk,  $a$*  24 in
- Stringer spacing/ *Jarak gelegar,  $b$*  3 in

[a] Determine if the skin and stringer can fail in buckling.

*Tentukan jika kulit dan gelegar boleh gagal secara lengkakan*

**(5 marks/markah)**

[b] Optimize the skin-stringer structure design by finding appropriate rib and stringer spacing's, ***a*** & ***b*** so that the structure fail simultaneously in buckling.

*Optimumkan rekabentuk struktur kulit-stringer dengan mencari jarak sesuai, ***a*** & ***b*** rusuk dan gelegar, supaya struktur gagal serentak secara lengkakan.*

- Ratio ***a/b*** > 3  
*Nisbah ***a/b*** > 3*

**(15 markah/markah)**

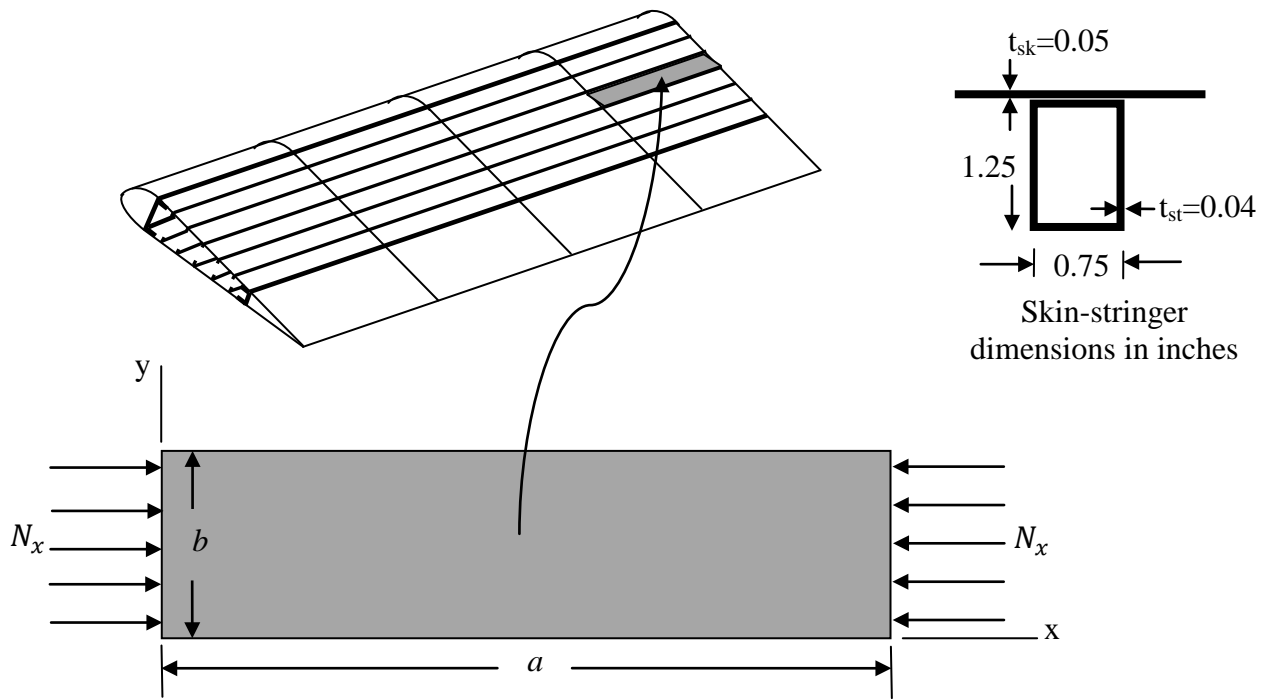
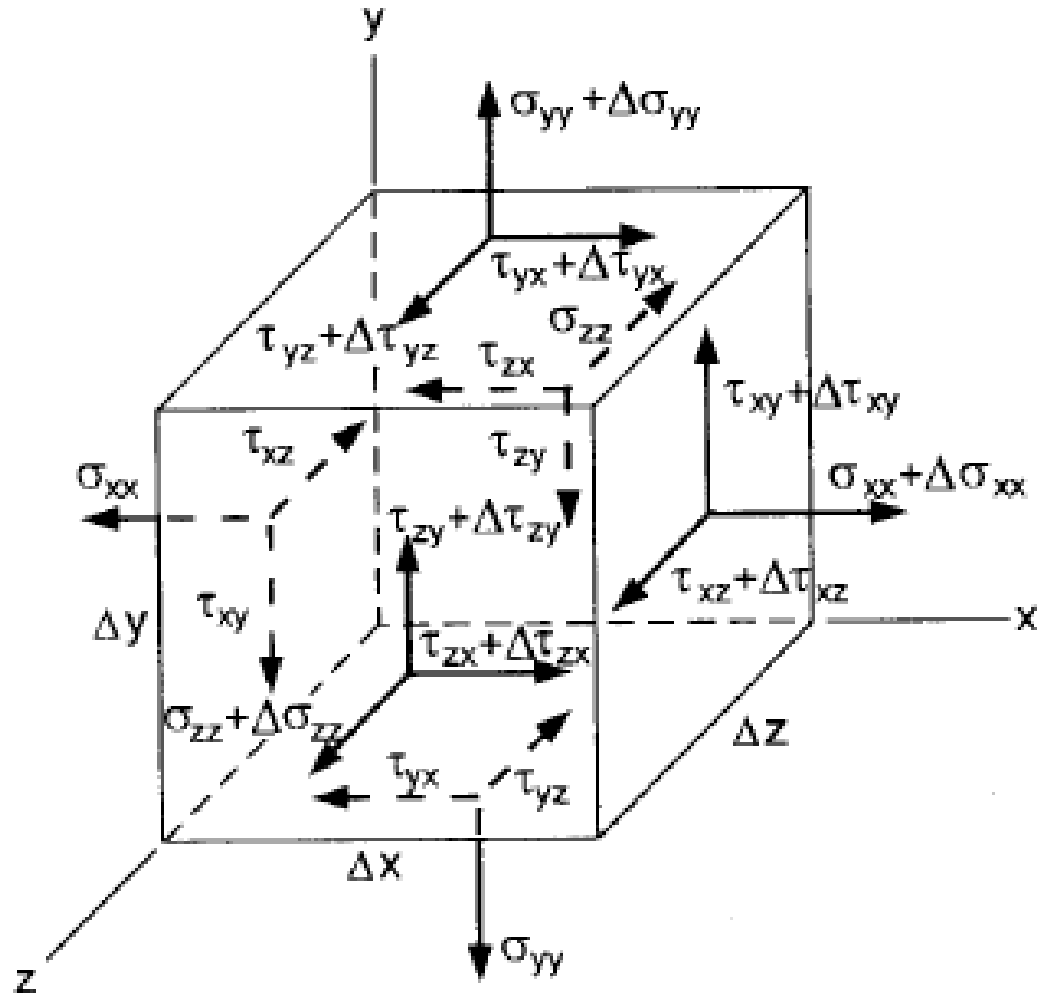


Figure 4  
Rajah 4

(15 marks/markah)

5. [a] Using **Figure 5[a]**, derive the equilibrium equation in the y-direction.

*Menggunakan Rajah 5[a], terbitkan persamaan keseimbangan pada arah-y.*

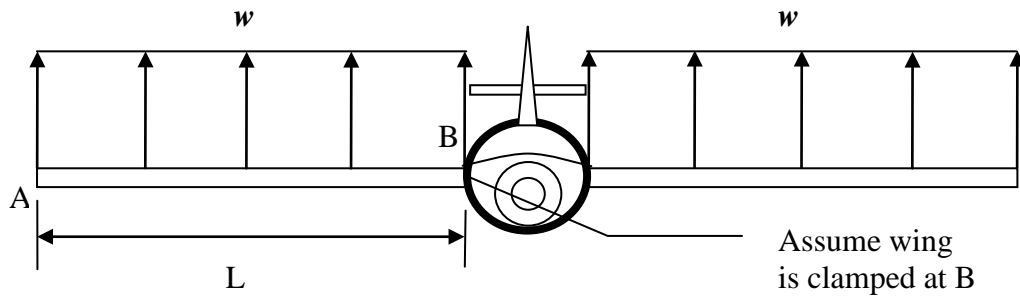


**Figure 5[a]**  
**Rajah 5[a]**

(5 marks/markah)

- [b] In **Figure 5[b]**, determine using energy method vertical displacement,  $e_v$  and rotation  $\theta$  at the wing tip at A subjected to wing load  $w$ . Wing shape is rectangle and straight with constant thickness.

*Di Rajah 5[b], dengan menggunakan cara tenaga tentukan anjakan menegak  $e_v$  dan putaran  $\theta$  pada hujung sayap di A akibat beban sayap  $w$ . Bentuk sayap adalah segiempat tepat dan tegak dengan ketebalan yang seragam.*



**Figure 5[b]**  
**Rajah 5[b]**

**(15 marks/markah)**

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## APPENDIX/LAMPIRAN

$$\sigma_x = \frac{P}{A} + \frac{-(M_z I_y + M_y I_{yz})y + (M_y I_z + M_z I_{yz})z}{I_y I_z - I_{yz}^2}$$

$$\Delta q = - \left[ \frac{(V_y I_y - V_z I_{yz})Q_z + (V_z I_z - V_y I_{yz})Q_y}{I_y I_z - I_{yz}^2} \right]$$

$$\theta = \frac{q}{2AG} \oint \frac{ds}{t}$$

$$q_i = \frac{\partial U}{\partial F_i}$$

$$= \sum_{j=1}^m \left( \int \frac{N_j}{E_j A_j} \frac{\partial N_j}{\partial F_i} dz + \int \frac{k_j V_j}{G_j A_j} \frac{\partial V_j}{\partial F_i} dz \right. \\ \left. + \int \frac{M_j}{E_j I_j} \frac{\partial M_j}{\partial F_i} dz + \int \frac{T_j}{G_j J_j} \frac{\partial T_j}{\partial F_i} dz \right)$$

$$\theta_i = \frac{\partial U}{\partial M_i}$$

$$= \sum_{j=1}^m \left( \int \frac{N_j}{E_j A_j} \frac{\partial N_j}{\partial M_i} dz + \int \frac{k_j V_j}{G_j A_j} \frac{\partial V_j}{\partial M_i} dz \right. \\ \left. + \int \frac{M_j}{E_j I_j} \frac{\partial M_j}{\partial M_i} dz + \int \frac{T_j}{G_j J_j} \frac{\partial T_j}{\partial M_i} dz \right)$$

$$P_{cr} = \frac{\pi^2 EI}{L_e^2}$$

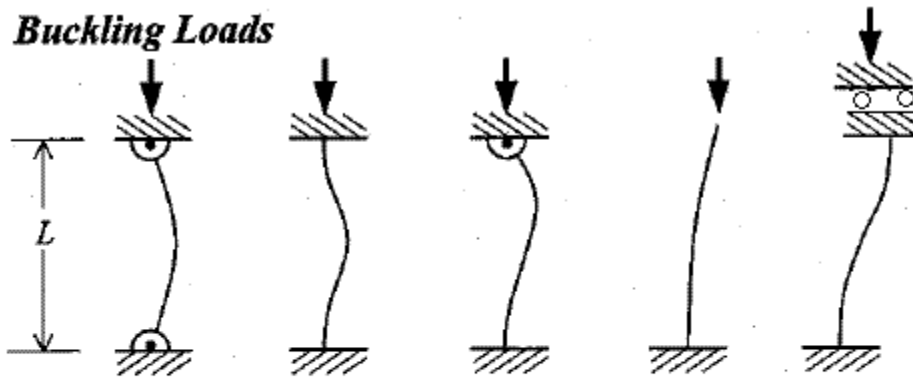
$$\sigma_{cr} = \frac{\pi^2 EI}{AL_e^2}$$

$$\sigma_{cr} = \frac{\pi^2 E}{(L_e / r)^2}$$

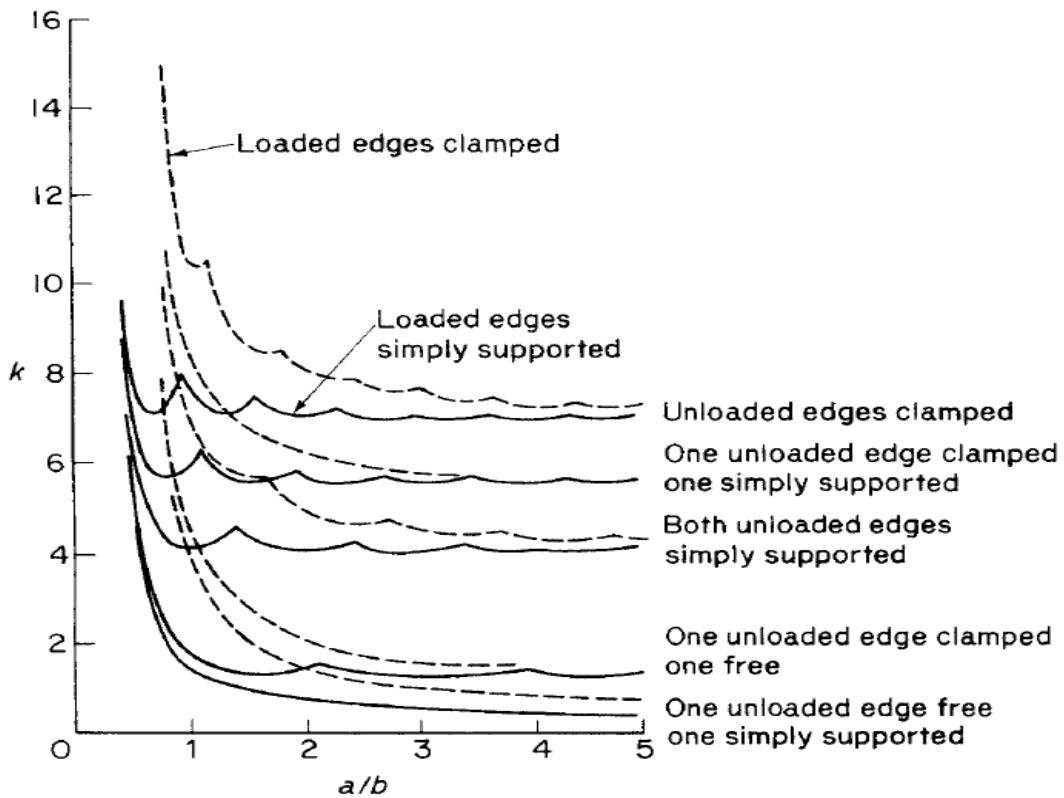
$$\sigma_{cr} = k \frac{\pi^2 E}{12(1-\nu^2)} \left(\frac{t}{b}\right)^2$$

$$\frac{b_{eff}}{2t} = 0.85 \sqrt{\frac{E_s}{\sigma_{stiffener}}} \text{ (simply-supported)}$$

**Buckling Loads**



Buckling Load	$\frac{\pi^2 EI}{L^2}$	$\frac{4\pi^2 EI}{L^2}$	$\frac{2.045\pi^2 EI}{L^2}$	$\frac{\pi^2 EI}{4L^2}$	$\frac{\pi^2 EI}{L^2}$
Effective Length $L_e$	$L$	$0.5L$	$0.699L$	$2L$	$L$



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