

UNIVERSITI SAINS MALAYSIA

Peperiksaan Kursus Semasa Cuti Panjang
Sidang Akademik 2002/2003

April 2003

KTE 211 – Teori Kumpulan dan Spektroskopi

Masa : 2 jam

Sila pastikan bahawa kertas peperiksaan ini mengandungi ENAM BELAS muka surat yang bercetak sebelum anda memulakan peperiksaan ini.

Kertas peperiksaan ini mengandungi dua bahagian iaitu, Bahagian A dan Bahagian B. **Jawab kedua-dua soalan di Bahagian A dan pilih dua lagi soalan daripada Bahagian B.** Jumlah soalan yang perlu dijawab ialah **EMPAT**.

Jika calon menjawab lebih daripada empat soalan hanya empat soalan pertama mengikut susunan dalam skrip jawapan akan diberi markah.

Jadual Karakter dilampirkan.

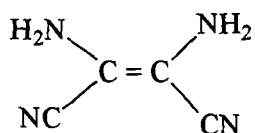
BAHAGIAN A

1. (a) Takrifkan setiap istilah berikut dengan berdasarkan teori kumpulan:

- (i) Kumpulan titik
- (ii) Paksi putaran tak wajar
- (iii) Jadual karakter
- (iv) Satah simetri
- (v) Perwakilan tak terturunkan

(15 markah)

(b) Dengan menggunakan kaedah matriks 3×3 (x, y, z) terbitkan set nilai karakter bagi setiap operasi simetri molekul berikut:



(10 markah)

2. (a) Nyatakan asas teori yang dapat menjelaskan pembentukan jalur dalam spektrum inframerah (IR). (6 markah)

(b) Nyatakan peranan molekul yang bersifat "kromofor" dalam pembentukan jalur spektrum ultralembayung (UV) sesuatu sebatian tersebut. (6 markah)

(c) Berikan penjelasan bagi turutan nilai nombor gelombang (cm^{-1}) untuk pengikatan antara C dan atom berikut:

$$\nu(\text{C-H}) > \nu(\text{C-C}) > \nu(\text{C-Cl}) > \nu(\text{C-Br}) > \nu(\text{C-I})$$

(6 markah)

- (d) Apakah yang dimaksudkan dengan istilah *satu sel unit*? Berikan nama bagi semua (tujuh) kekisi asas sel unit. (7 markah)

BAHAGIAN B

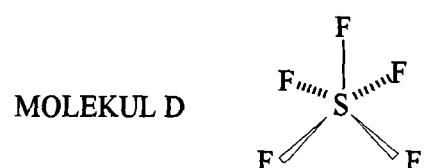
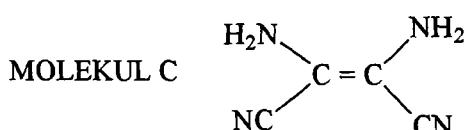
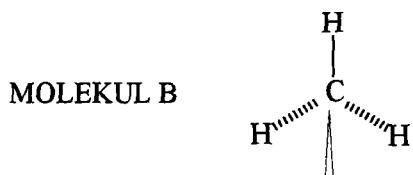
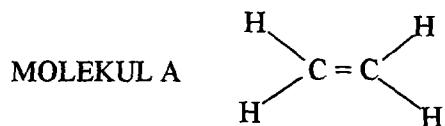
Pilih mana-mana DUA soalan

3. Gambarajah berikut menunjukkan empat molekul A, B, C dan D.

(i) Tunjukkan kesemua operasi simetri yang terdapat pada setiap molekul tersebut dengan lakaran yang sesuai. (9 markah)

(ii) Berikan lakaran stereografik kumpulan titik bagi setiap molekul tersebut. (8 markah)

(iii) Berikan kumpulan titik bagi setiap molekul tersebut dan terangkan jawapan anda. (8 markah)



4. (a) Gambarajah berikut menunjukkan molekul NH_3 yang dilakarkan berdasarkan paksi-paksi koordinat Cartes x, y dan z..

(i) Berikan kesemua unsur simetri yang wujud pada molekul tersebut.

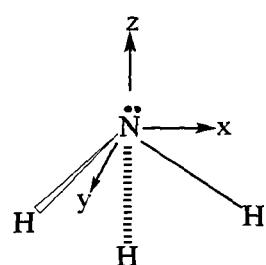
(6 markah)

(ii) Tentukan kumpulan titik bagi molekul tersebut.

(2 markah)

(iii) Tentukan nilai karakter bagi setiap operasi dengan berdasarkan paksi koordinat Cartes yang diberikan bagi atom nitrogen.

(9 markah)

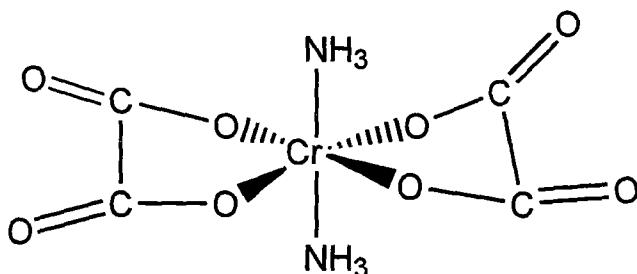


- (b) (i) Lakarkan molekul $\text{Co}(\text{NH}_3)_3\text{Cl}_3$ yang tergolong dalam kumpulan titik C_{3v} dan terangkan jawapan anda.
- (ii) Berikan dan lakarkan SATU contoh molekul yang mempunyai isomer *cis* dan *trans*. Dengan berpandukan teori kumpulan, bezakan antara isomer *cis* dan *trans* bagi molekul tersebut.

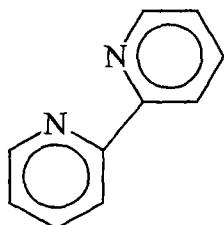
(8 markah)

5. (a) Nyatakan kaedah spektroskopi yang paling sesuai untuk pencirian sebatian berikut. Berikan dua alasan terhadap pemilihan yang telah dilakukan dan perihalkan kumpulan berfungsi yang dapat menyumbang kepada spektrum yang dijangkakan.

i.



ii.



iii. $\text{cis-Pt}(\text{CN})_2\text{Cl}_2$

(15 markah)

- (b) Tuliskan esei ringkas yang memperihalkan perbezaan teori asas bagi kaedah spektroskopi resonans magnetik nukleus (NMR) dan spektroskopi Raman.

(10 markah)

6. Berikan penjelasan terhadap kenyataan berikut:

- (a) Spektrum inframerah untuk sebatian $\text{Cr}(\text{CO})_6$ akan mempamirkan hanya satu jalur tajam bagi regangan pengikatan CO.
(8 markah)
- (b) Spektrum inframerah untuk ion sulfat, $[\text{SO}_4]^{2-}$ akan mempamirkan penambahan bilangan jalur apabila kumpulan titik ion sulfat berubah melalui pengikatannya daripada t_d kepada C_{3v} .
(8 markah)

- (c) Kaedah kristalografi sinaran-X akan dapat memberikan penyelesaian terhadap penentuan struktur molekul. Nyatakan pertimbangan yang perlu diambil kira dalam mendapatkan penyelesaian struktur molekul yang sebenar.

(9 markah)

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LAMPIRAN*Character Tables*

THE NONAXIAL GROUPS

| C_1 | E | | |
|-------|-----|------------|-----------------------------|
| A | 1 | | |
| C_s | E | σ_h | |
| A' | 1 | 1 | x, y, R_z |
| A'' | 1 | -1 | z, R_x, R_y |
| C_i | E | i | |
| A_g | 1 | 1 | R_x, R_y, R_z |
| A_u | 1 | -1 | x, y, z |
| | | | x^2, y^2, z^2, xy |
| | | | yz, xz |
| | | | $x^2, y^2, z^2, xy, xz, yz$ |

THE AXIAL GROUPS

► The C_n Groups

| C_2 | E | C_2 | | |
|-------|--|-------|------------------|--------------------------------|
| A | 1 | 1 | z, R_z | x^2, y^2, z^2, xy |
| B | 1 | -1 | x, y, R_x, R_y | yz, xz |
| C_3 | E | C_3 | C_3^2 | $\varepsilon = \exp(2\pi i/3)$ |
| A | 1 | 1 | 1 | z, R_z |
| E | $\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{Bmatrix}$ | | | $(x, y), (R_x, R_y)$ |
| | | | | $(x^2 + y^2, z^2)$ |
| | | | | $(x^2 - y^2, xy), (yz, xz)$ |

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| C_4 | E | C_4 | C_2 | C_4^3 | | |
|-------|--|-------|-------|---------|----------------------|------------------|
| A | 1 | 1 | 1 | 1 | z, R_z | $x^2 + y^2, z^2$ |
| B | 1 | -1 | 1 | -1 | | $x^2 - y^2, xy$ |
| E | $\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$ | | | | $(x, y), (R_x, R_y)$ | (xz, yz) |

| C_5 | E | C_5 | C_5^2 | C_5^3 | C_5^4 | $\varepsilon = \exp(2\pi i/5)$ |
|-------|--|-------|---------|---------|---------|--------------------------------|
| A | 1 | 1 | 1 | 1 | 1 | z, R_z |
| E_1 | $\begin{Bmatrix} 1 & \varepsilon & \varepsilon^2 & \varepsilon^{2*} & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon^{2*} & \varepsilon^2 & \varepsilon \end{Bmatrix}$ | | | | | $x^2 + y^2, z^2$ |
| E_2 | $\begin{Bmatrix} 1 & \varepsilon^2 & \varepsilon^* & \varepsilon & \varepsilon^{2*} \\ 1 & \varepsilon^{2*} & \varepsilon & \varepsilon^* & \varepsilon^2 \end{Bmatrix}$ | | | | | (yz, xz) |
| | | | | | | $(x^2 - y^2, xy)$ |

| C_6 | E | C_6 | C_3 | C_2 | C_3^2 | C_6^2 | $\varepsilon = \exp(2\pi i/6)$ |
|-------|--|-------|-------|-------|---------|---------|--------------------------------|
| A | 1 | 1 | 1 | 1 | 1 | 1 | |
| B | 1 | -1 | 1 | -1 | 1 | -1 | z, R_z |
| E_1 | $\begin{Bmatrix} 1 & \varepsilon & -\varepsilon^* & -1 & -\varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & -\varepsilon & -1 & -\varepsilon^* & \varepsilon \end{Bmatrix}$ | | | | | | $(x, y), (R_x, R_y)$ |
| E_2 | $\begin{Bmatrix} 1 & -\varepsilon^* & -\varepsilon & 1 & -\varepsilon^* & -\varepsilon \\ 1 & -\varepsilon & -\varepsilon^* & 1 & -\varepsilon & -\varepsilon^* \end{Bmatrix}$ | | | | | | (xz, yz) |
| | | | | | | | $(x^2 - y^2, xy)$ |

| C_7 | E | C_7 | C_7^2 | C_7^3 | C_7^4 | C_7^5 | C_7^6 | $\varepsilon = \exp(2\pi i/7)$ |
|-------|--|-------|---------|---------|---------|---------|---------|--------------------------------|
| A | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| E_1 | $\begin{Bmatrix} 1 & \varepsilon & \varepsilon^2 & \varepsilon^3 & \varepsilon^{3*} & \varepsilon^{2*} & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon^{2*} & \varepsilon^{3*} & \varepsilon^3 & \varepsilon^2 & \varepsilon \end{Bmatrix}$ | | | | | | | $(x, y), (R_x, R_y)$ |
| E_2 | $\begin{Bmatrix} 1 & \varepsilon^2 & \varepsilon^{3*} & \varepsilon^* & \varepsilon & \varepsilon^3 & \varepsilon^{2*} \\ 1 & \varepsilon^{2*} & \varepsilon^3 & \varepsilon & \varepsilon^* & \varepsilon^{3*} & \varepsilon^2 \end{Bmatrix}$ | | | | | | | (xz, yz) |
| E_3 | $\begin{Bmatrix} 1 & \varepsilon^3 & \varepsilon^* & \varepsilon^2 & \varepsilon^{2*} & \varepsilon & \varepsilon^{3*} \\ 1 & \varepsilon^{3*} & \varepsilon & \varepsilon^{2*} & \varepsilon^2 & \varepsilon^* & \varepsilon^3 \end{Bmatrix}$ | | | | | | | $(x^2 - y^2, xy)$ |

| C_8 | E | C_8 | C_4 | C_2 | C_4^3 | C_8^3 | C_8^4 | C_8^7 | $\varepsilon = \exp(2\pi i/8)$ |
|-------|--|-------|-------|-------|---------|---------|---------|---------|--------------------------------|
| A | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| B | 1 | -1 | 1 | 1 | 1 | -1 | -1 | -1 | z, R_z |
| E_1 | $\begin{Bmatrix} 1 & \varepsilon & i & -1 & -i & -\varepsilon^* & -\varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & -i & -1 & i & -\varepsilon & -\varepsilon^* & \varepsilon \end{Bmatrix}$ | | | | | | | | $(x, y), (R_x, R_y)$ |
| E_2 | $\begin{Bmatrix} 1 & i & -1 & 1 & -1 & -i & i & -i \\ 1 & -i & -1 & 1 & -1 & i & -i & i \end{Bmatrix}$ | | | | | | | | (xz, yz) |
| E_3 | $\begin{Bmatrix} 1 & -\varepsilon & i & -1 & -i & \varepsilon^* & \varepsilon & -\varepsilon^* \\ 1 & -\varepsilon^* & -i & -1 & i & \varepsilon & \varepsilon^* & -\varepsilon \end{Bmatrix}$ | | | | | | | | $(x^2 - y^2, xy)$ |

► The S_n Groups

| S_4 | E | S_4 | C_2 | S_4^3 | | |
|-------|--|-------|-------|---------|----------------------|------------------|
| A | 1 | 1 | 1 | 1 | R_z | $x^2 + y^2, z^2$ |
| B | 1 | -1 | 1 | -1 | z | $x^2 - y^2, xy$ |
| E | $\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$ | | | | $(x, y), (R_x, R_y)$ | (xz, yz) |

| S_6 | E | C_3 | C_3^2 | i | S_6^3 | S_6 | $\varepsilon = \exp(2\pi i/3)$ |
|-------|--|-------|---------|-----|---------|--------------|--------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | 1 | R_z $x^2 + y^2, z^2$ |
| E_1 | $\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* & 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon & 1 & \varepsilon^* & \varepsilon \end{Bmatrix}$ | | | | | (R_x, R_y) | $(x^2 - y^2, xy), (xy, yz)$ |
| A_2 | 1 | 1 | 1 | -1 | -1 | -1 | z |
| E_2 | $\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* & -1 & -\varepsilon & -\varepsilon^* \\ 1 & \varepsilon^* & \varepsilon & -1 & -\varepsilon^* & -\varepsilon \end{Bmatrix}$ | | | | | | (x, y) |

| S_8 | E | S_8 | C_4 | S_8^3 | C_2 | S_8^5 | C_4^3 | S_8^7 | $\varepsilon = \exp(2\pi i/8)$ |
|-------|--|-------|-------|---------|-------|---------|----------------------|---------|--------------------------------|
| A | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | R_z $x^2 + y^2, z^2$ |
| B | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | z |
| E_1 | $\begin{Bmatrix} 1 & \varepsilon & i & -\varepsilon^* & -1 & -\varepsilon & -i & \varepsilon^* \\ 1 & \varepsilon^* & -i & -\varepsilon & -1 & -\varepsilon^* & i & \varepsilon \end{Bmatrix}$ | | | | | | $(x, y), (R_x, R_y)$ | | |
| E_2 | $\begin{Bmatrix} 1 & i & -1 & -i & 1 & i & -1 & -i \\ 1 & -i & -1 & i & 1 & -i & -1 & i \end{Bmatrix}$ | | | | | | | | $(x^2 - y^2, xy)$ |
| E_3 | $\begin{Bmatrix} 1 & -\varepsilon^* & -i & \varepsilon & -1 & \varepsilon^* & i & -\varepsilon \\ 1 & -\varepsilon & i & \varepsilon^* & -1 & \varepsilon & -i & -\varepsilon^* \end{Bmatrix}$ | | | | | | | | (xz, yz) |

► The C_{nv} Groups

| C_{2v} | E | C_2 | $\sigma_v(xz)$ | $\sigma'_v(yz)$ | | |
|----------|-----|-------|----------------|-----------------|----------|-----------------|
| A_1 | 1 | 1 | 1 | 1 | z | x^2, y^2, z^2 |
| A_2 | 1 | 1 | -1 | -1 | R_z | xy |
| B_1 | 1 | -1 | 1 | -1 | x, R_y | xz |
| B_2 | 1 | -1 | -1 | 1 | y, R_x | yz |

| C_{3v} | E | $2C_3$ | $3\sigma_v$ | | |
|----------|-----|--------|-------------|----------------------|-----------------------------|
| A_1 | 1 | 1 | 1 | z | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | -1 | R_z | |
| E | 2 | -1 | 0 | $(x, y), (R_x, R_y)$ | $(x^2 - y^2, xy), (xz, yz)$ |

C-4

APPENDIX C

| C_{4v} | E | $2C_4$ | C_2 | $2\sigma_c$ | $2\sigma_d$ | | |
|----------|-----|--------|-------|-------------|-------------|----------------------|------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | z | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | 1 | -1 | -1 | R_z | |
| B_1 | 1 | -1 | 1 | 1 | -1 | | $x^2 - y^2$ |
| B_2 | 1 | -1 | 1 | -1 | 1 | | xy |
| E | 2 | 0 | -2 | 0 | 0 | $(x, y), (R_x, R_y)$ | (xz, yz) |

| C_{5v} | E | $2C_5$ | $2C_5^2$ | $5\sigma_c$ | | | |
|----------|-----|--------------------|--------------------|-------------|----|----------------------|-------------------|
| A_1 | 1 | 1 | | 1 | 1 | z | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | | 1 | -1 | R_z | |
| E_1 | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | | $(x, y), (R_x, R_y)$ | (xz, yz) |
| E_2 | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | | | $(x^2 - y^2, xy)$ |

| C_{6v} | E | $2C_6$ | $2C_3$ | C_2 | $3\sigma_c$ | $3\sigma_d$ | |
|----------|-----|--------|--------|-------|-------------|-------------|---------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | z | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | 1 | 1 | -1 | R_z | |
| B_1 | 1 | -1 | 1 | -1 | 1 | -1 | |
| B_2 | 1 | -1 | 1 | -1 | -1 | 1 | |
| E_1 | 2 | 1 | -1 | -2 | 0 | 0 | $(x, y), (R_x, R_y)$ |
| E_2 | 2 | -1 | -1 | 2 | 0 | 0 | (xz, yz) $(x^2 - y^2, xy)$ |

► The C_{nh} Groups

| C_{2h} | E | C_2 | i | σ_h | | |
|----------|-----|-------|-----|------------|------------|---------------------|
| A_g | 1 | 1 | 1 | 1 | R_z | x^2, y^2, z^2, xy |
| B_g | 1 | -1 | 1 | -1 | R_x, R_y | xz, yz |
| A_u | 1 | 1 | -1 | -1 | z | |
| B_u | 1 | -1 | -1 | 1 | x, y | |

| C_{3h} | E | C_3 | C_3^2 | σ_h | S_3 | S_3^2 | $\varepsilon = \exp(2\pi i/3)$ |
|----------|--|--|--|------------|--------------|---------|--------------------------------|
| A' | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| E' | $\begin{pmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{pmatrix}$ | $\begin{pmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{pmatrix}$ | $\begin{pmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{pmatrix}$ | | (x, y) | | $(x^2 - y^2, xy)$ |
| A'' | 1 | 1 | 1 | -1 | -1 | -1 | z |
| E'' | $\begin{pmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{pmatrix}$ | $\begin{pmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{pmatrix}$ | $\begin{pmatrix} 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon \end{pmatrix}$ | | (R_x, R_y) | | (xz, yz) |

| C_{4h} | E | C_4 | C_2 | C_4^3 | i | S_4^3 | σ_h | S_4 | |
|----------|---|---|---|--|---|---|--|-------|------------------|
| A_g | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | R_z |
| B_g | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | $x^2 + y^2, z^2$ |
| E_g | $\begin{cases} 1 & i \\ 1 & -i \end{cases}$ | $\begin{cases} -1 & -i \\ -1 & i \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & -1 \end{cases}$ | $\begin{cases} -i & i \\ i & -i \end{cases}$ | $\begin{cases} 1 & i \\ 1 & -i \end{cases}$ | $\begin{cases} -1 & -1 \\ -1 & 1 \end{cases}$ | $\begin{cases} -i & i \\ i & -i \end{cases}$ | | $x^2 - y^2, xy$ |
| A_u | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | (R_x, R_y) |
| B_u | 1 | -1 | 1 | -1 | -1 | 1 | -1 | 1 | z |
| E_u | $\begin{cases} 1 & i \\ 1 & -i \end{cases}$ | $\begin{cases} -1 & -i \\ -1 & i \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & -1 \end{cases}$ | $\begin{cases} -i & i \\ -i & i \end{cases}$ | $\begin{cases} -1 & -i \\ -1 & i \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & -i \end{cases}$ | $\begin{cases} 1 & i \\ 1 & -i \end{cases}$ | | (x, y) |

| C_{5h} | E | C_5 | C_5^2 | C_5^3 | C_5^4 | σ_h | S_5 | S_5^2 | S_5^3 | S_5^4 | $\varepsilon = \exp(2\pi i/5)$ |
|----------|---|---|--|--|--|---|--|---|--|--|--------------------------------|
| A' | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | R_z |
| E'_1 | $\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^*$ | $\begin{cases} \varepsilon & \varepsilon^2 \\ \varepsilon^* & \varepsilon^{2*} \end{cases}$ | $\begin{cases} \varepsilon^2 & \varepsilon^{2*} \\ \varepsilon^{2*} & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon^* & \varepsilon \\ \varepsilon & \varepsilon \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & 1 \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^2 \\ \varepsilon^* & \varepsilon^{2*} \end{cases}$ | $\begin{cases} \varepsilon^2 & \varepsilon^{2*} \\ \varepsilon^{2*} & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon^{2*} & \varepsilon \\ \varepsilon & \varepsilon \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^2 \\ \varepsilon^* & \varepsilon \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & 1 \end{cases}$ | (x, y) |
| E'_2 | $\begin{cases} 1 & \varepsilon^2 \\ 1 & \varepsilon^{2*} \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^* \\ \varepsilon^* & \varepsilon \end{cases}$ | $\begin{cases} \varepsilon^* & \varepsilon \\ \varepsilon & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^{2*} \\ \varepsilon^{2*} & \varepsilon^2 \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & 1 \end{cases}$ | $\begin{cases} \varepsilon^2 & \varepsilon^* \\ \varepsilon^{2*} & \varepsilon \end{cases}$ | $\begin{cases} \varepsilon^* & \varepsilon \\ \varepsilon & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^* \\ \varepsilon^* & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^2 \\ \varepsilon^2 & \varepsilon \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & 1 \end{cases}$ | $(x^2 - y^2, xy)$ |
| A'' | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | z |
| E''_1 | $\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^2 \\ \varepsilon^* & \varepsilon^{2*} \end{cases}$ | $\begin{cases} \varepsilon^2 & \varepsilon^{2*} \\ \varepsilon^{2*} & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon^* & \varepsilon \\ \varepsilon & \varepsilon \end{cases}$ | $\begin{cases} -1 & -1 \\ -1 & -1 \end{cases}$ | $\begin{cases} -\varepsilon & -\varepsilon^2 \\ -\varepsilon^* & -\varepsilon^{2*} \end{cases}$ | $\begin{cases} -\varepsilon^2 & -\varepsilon^{2*} \\ -\varepsilon^{2*} & -\varepsilon^2 \end{cases}$ | $\begin{cases} -\varepsilon^{2*} & -\varepsilon \\ -\varepsilon & -\varepsilon \end{cases}$ | $\begin{cases} -\varepsilon & -\varepsilon^2 \\ -\varepsilon^* & -\varepsilon \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & 1 \end{cases}$ | (R_x, R_y) |
| E''_2 | $\begin{cases} 1 & \varepsilon^2 \\ 1 & \varepsilon^{2*} \end{cases}$ | $\begin{cases} \varepsilon & \varepsilon^* \\ \varepsilon^* & \varepsilon \end{cases}$ | $\begin{cases} \varepsilon^* & \varepsilon \\ \varepsilon & \varepsilon^2 \end{cases}$ | $\begin{cases} \varepsilon^2 & \varepsilon^{2*} \\ \varepsilon^{2*} & \varepsilon^2 \end{cases}$ | $\begin{cases} -1 & -1 \\ -1 & -1 \end{cases}$ | $\begin{cases} -\varepsilon^2 & -\varepsilon^* \\ -\varepsilon^{2*} & -\varepsilon \end{cases}$ | $\begin{cases} -\varepsilon^* & -\varepsilon \\ -\varepsilon & -\varepsilon^2 \end{cases}$ | $\begin{cases} -\varepsilon & -\varepsilon^2 \\ -\varepsilon^* & -\varepsilon \end{cases}$ | $\begin{cases} -\varepsilon^2 & -\varepsilon \\ -\varepsilon & -\varepsilon^2 \end{cases}$ | $\begin{cases} 1 & 1 \\ 1 & 1 \end{cases}$ | (xz, yz) |

| C_{4h} | E | C_3 | C_2 | C_3^2 | C_6^2 | i | S_3^2 | S_6^2 | σ_h | S_6 | S_3 | | $\epsilon = \exp(2\pi i/6)$ |
|----------|----------|------------------------------|------------------------------|----------|------------------------------|------------------------------|----------|------------------------------|------------------------------|----------|------------------------------|--------------|-----------------------------|
| A_g | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | | |
| B_g | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | R_z | $x^2 + y^2, z^2$ |
| E_{1g} | {1 1} | ϵ ϵ^* | $-\epsilon^*$ $-\epsilon$ | -1 -1 | $-\epsilon$ ϵ | ϵ^* ϵ | 1 1 | ϵ ϵ^* | $-\epsilon^*$ $-\epsilon$ | -1 -1 | $-\epsilon$ ϵ | (R_x, R_y) | (xz, yz) |
| E_{2g} | {1 1} | $-\epsilon^*$ $-\epsilon$ | $-\epsilon$ $-\epsilon^*$ | 1 1 | $-\epsilon^*$ $-\epsilon$ | $-\epsilon$ $-\epsilon^*$ | 1 1 | $-\epsilon^*$ $-\epsilon$ | $-\epsilon$ $-\epsilon^*$ | 1 1 | $-\epsilon^*$ $-\epsilon$ | | $(x^2 - y^2, xy)$ |
| A_u | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | | |
| B_u | 1 | -1 | 1 | -1 | 1 | -1 | -1 | 1 | -1 | 1 | -1 | z | |
| E_{1u} | {1 1} | ϵ ϵ^* | $-\epsilon^*$ $-\epsilon$ | -1 -1 | $-\epsilon$ ϵ | ϵ^* ϵ | -1 -1 | $-\epsilon$ ϵ | ϵ^* ϵ | 1 1 | $-\epsilon^*$ $-\epsilon$ | (x, y) | |
| E_{2u} | {1 1} | $-\epsilon^*$ $-\epsilon$ | $-\epsilon$ $-\epsilon^*$ | 1 1 | $-\epsilon^*$ $-\epsilon$ | $-\epsilon$ $-\epsilon^*$ | -1 -1 | ϵ^* ϵ | ϵ ϵ^* | -1 -1 | ϵ^* ϵ | | |

THE DIHEDRAL GROUPS

► *The D_n Groups*

| D_2 | E | $C_2(z)$ | $C_2(y)$ | $C_2(x)$ | |
|-------|-----|----------|----------|----------|-----------------|
| A | 1 | 1 | 1 | 1 | x^2, y^2, z^2 |
| B_1 | 1 | 1 | -1 | -1 | z, R_z |
| B_2 | 1 | -1 | 1 | -1 | y, R_y |
| B_3 | 1 | -1 | -1 | 1 | x, R_x |

| D_3 | E | $2C_3$ | $3C_2$ | (x axis is coincident with C_2) | |
|-------|-----|--------|--------|---------------------------------------|-----------------------------|
| A_1 | 1 | 1 | 1 | | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | -1 | z, R_z | |
| E | 2 | -1 | 0 | $(x, y), (R_x, R_y)$ | $(x^2 - y^2, xy), (xz, yz)$ |

| D_4 | E | $2C_4$ | $C_2 (= C_2')$ | $2C_2'$ | $2C_2''$ | (x axis coincident with C_2') |
|-------|-----|--------|----------------|---------|----------|-------------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | |
| A_2 | 1 | 1 | 1 | -1 | -1 | z, R_z |
| B_1 | 1 | -1 | 1 | 1 | -1 | |
| B_2 | 1 | -1 | 1 | -1 | 1 | $x^2 - y^2$ |
| E | 2 | 0 | -2 | 0 | 0 | $(x, y), (R_x, R_y)$ |

| D_5 | E | $2C_5$ | $2C_5'$ | $5C_2$ | (x axis coincident with C_2) |
|-------|-----|--------------------|--------------------|--------|------------------------------------|
| A_1 | 1 | 1 | 1 | 1 | |
| A_2 | 1 | 1 | 1 | -1 | z, R_z |
| E_1 | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | $(x, y), (R_x, R_y)$ |
| E_2 | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | (xz, yz) $(x^2 - y^2, xy)$ |

| D_6 | E | $2C_6$ | $2C_3$ | C_2 | $3C_2'$ | $3C_2''$ | (x axis coincident with C_2') |
|-------|-----|--------|--------|-------|---------|----------|-------------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| A_2 | 1 | 1 | 1 | 1 | -1 | -1 | z, R_z |
| B_1 | 1 | -1 | 1 | -1 | 1 | -1 | |
| B_2 | 1 | -1 | 1 | -1 | -1 | 1 | |
| E_1 | 2 | 1 | -1 | -2 | 0 | 0 | $(x, y), (R_x, R_y)$ |
| E_2 | 2 | -1 | -1 | 2 | 0 | 0 | (xz, yz) $(x^2 - y^2, xy)$ |

► The D_{nh} Groups

| D_{2h} | E | $C_2(z)$ | $C_2(y)$ | $C_2(x)$ | i | $\sigma(xy)$ | $\sigma(xz)$ | $\sigma(yz)$ | |
|----------|-----|----------|----------|----------|-----|--------------|--------------|--------------|-----------------|
| A_g | 1 | 1 | 1 | 1 | 1 | 1 | -1 | 1 | x^2, y^2, z^2 |
| B_{1g} | 1 | 1 | -1 | -1 | 1 | 1 | -1 | -1 | R_z |
| B_{2g} | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | xy |
| B_{3g} | 1 | -1 | -1 | 1 | 1 | -1 | -1 | 1 | xz |
| A_u | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | yz |
| B_{1u} | 1 | 1 | -1 | -1 | -1 | -1 | 1 | 1 | z |
| B_{2u} | 1 | -1 | 1 | -1 | -1 | 1 | -1 | 1 | y |
| B_{3u} | 1 | -1 | -1 | 1 | -1 | 1 | 1 | -1 | x |

| D_{3h} | E | $2C_3$ | $3C_2$ | σ_h | $2S_3$ | $3\sigma_c$ | (x axis coincident with C_3) |
|----------|-----|--------|--------|------------|--------|-------------|---------------------------------|
| A'_1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A'_2 | 1 | 1 | -1 | 1 | 1 | -1 | R_z |
| E' | 2 | -1 | 0 | 2 | -1 | 0 | (x, y) |
| A''_1 | 1 | 1 | 1 | -1 | -1 | -1 | $(x^2 - y^2, xy)$ |
| A''_2 | 1 | 1 | -1 | -1 | -1 | 1 | z |
| E'' | 2 | -1 | 0 | -2 | 1 | 0 | (R_x, R_y) |
| | | | | | | | (xz, yz) |

| D_{4h} | E | $2C_4$ | C_2 | $2C'_2$ | $2C''_2$ | i | $2S_4$ | σ_h | $2\sigma_c$ | $2\sigma_d$ | (x axis coincident with C_2) |
|----------|-----|--------|-------|---------|----------|-----|--------|------------|-------------|-------------|---------------------------------|
| A_{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_{2g} | 1 | 1 | 1 | -1 | -1 | 1 | 1 | 1 | -1 | -1 | R_z |
| B_{1g} | 1 | -1 | 1 | 1 | -1 | 1 | -1 | 1 | 1 | -1 | $x^2 - y^2$ |
| B_{2g} | 1 | -1 | 1 | -1 | 1 | 1 | -1 | 1 | -1 | 1 | xy |
| E_g | 2 | 0 | -2 | 0 | 0 | 2 | 0 | -2 | 0 | 0 | (R_x, R_y) |
| A_{1u} | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | (xz, yz) |
| A_{2u} | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | 1 | 1 | z |
| B_{1u} | 1 | -1 | 1 | 1 | -1 | -1 | 1 | -1 | -1 | 1 | |
| B_{2u} | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | |
| E_u | 2 | 0 | -2 | 0 | 0 | -2 | 0 | 2 | 0 | 0 | (x, y) |

| D_{5h} | E | $2C_5$ | $2C'_5$ | $5C_2$ | σ_h | $2S_5$ | $2S'_5$ | $5\sigma_c$ | (x axis coincident with C_2) |
|----------|-----|--------------------|--------------------|--------|------------|---------------------|---------------------|-------------|---------------------------------|
| A'_1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A'_2 | 1 | 1 | 1 | -1 | 1 | 1 | 1 | -1 | R_z |
| E'_1 | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | (x, y) |
| E'_2 | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | -2 | $-2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | $(x^2 - y^2, xy)$ |
| A''_1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | |
| A''_2 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | 1 | z |
| E''_1 | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | -2 | $-2 \cos 72^\circ$ | $-2 \cos 144^\circ$ | 0 | (R_x, R_y) |
| E''_2 | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | -2 | $-2 \cos 144^\circ$ | $-2 \cos 72^\circ$ | 0 | (xz, yz) |

| D_{6u} | E | $2C_6$ | $2C_3$ | C_2 | $3C'_2$ | $3C''_2$ | i | $2S_3$ | $2S_6$ | σ_h | $3\sigma_d$ | $3\sigma_e$ | (x axis coincident with C'_2) |
|----------|-----|--------|--------|-------|---------|----------|-----|--------|--------|------------|-------------|-------------|----------------------------------|
| A_{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_{2g} | 1 | 1 | 1 | 1 | -1 | -1 | 1 | 1 | 1 | 1 | -1 | -1 | R_z |
| B_{1g} | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | |
| B_{2g} | 1 | -1 | 1 | -1 | -1 | 1 | 1 | -1 | 1 | -1 | -1 | 1 | |
| E_{1g} | 2 | 1 | -1 | -2 | 0 | 0 | 2 | 1 | -1 | -2 | 0 | 0 | (R_x, R_y) |
| E_{2g} | 2 | -1 | -1 | 2 | 0 | 0 | 2 | -1 | -1 | 2 | 0 | 0 | (xz, yz) $(x^2 - y^2, xy)$ |
| A_{1u} | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | |
| A_{2u} | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | 1 | z |
| B_{1u} | 1 | -1 | 1 | -1 | 1 | -1 | -1 | 1 | -1 | 1 | -1 | 1 | |
| B_{2u} | 1 | -1 | 1 | -1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | |
| E_{1u} | 2 | 1 | -1 | -2 | 0 | 0 | -2 | -1 | 1 | 2 | 0 | 0 | (x, y) |
| E_{2u} | 2 | -1 | -1 | 2 | 0 | 0 | -2 | 1 | 1 | -2 | 0 | 0 | |

| D_{4u} | E | $2C_4$ | $2C'_4$ | $2C_4$ | C_2 | $4C'_2$ | $4C''_2$ | i | $2S_4$ | $2S_8$ | $2S_4$ | σ_h | $4\sigma_e$ | $4\sigma_d$ | (x axis coincident with C'_2) |
|----------|-----|-------------|-------------|--------|-------|---------|----------|-----|-------------|-------------|--------|------------|-------------|-------------|----------------------------------|
| A_{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_{2g} | 1 | 1 | 1 | 1 | 1 | -1 | -1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | R_z |
| B_{1g} | 1 | -1 | -1 | 1 | 1 | 1 | -1 | 1 | -1 | -1 | 1 | 1 | 1 | -1 | |
| B_{2g} | 1 | -1 | -1 | 1 | 1 | -1 | 1 | 1 | -1 | -1 | 1 | 1 | -1 | 1 | |
| E_{1g} | 2 | $\sqrt{2}$ | $-\sqrt{2}$ | 0 | -2 | 0 | 0 | 2 | $\sqrt{2}$ | $-\sqrt{2}$ | 0 | -2 | 0 | 0 | (R_x, R_y) |
| E_{2g} | 2 | 0 | 0 | -2 | 2 | 0 | 0 | 2 | 0 | 0 | -2 | 2 | 0 | 0 | (xz, yz) $(x^2 - y^2, xy)$ |
| E_{1e} | 2 | $-\sqrt{2}$ | $\sqrt{2}$ | 0 | -2 | 0 | 0 | 2 | $-\sqrt{2}$ | $\sqrt{2}$ | 0 | -2 | 0 | 0 | |
| A_{1u} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | |
| A_{2u} | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | -1 | -1 | 1 | 1 | z |
| B_{1u} | 1 | -1 | -1 | 1 | 1 | 1 | -1 | -1 | 1 | 1 | -1 | -1 | -1 | 1 | |
| B_{2u} | 1 | -1 | -1 | 1 | 1 | -1 | 1 | -1 | 1 | 1 | -1 | -1 | 1 | -1 | |
| E_{1u} | 2 | $\sqrt{2}$ | $-\sqrt{2}$ | 0 | -2 | 0 | 0 | -2 | $-\sqrt{2}$ | $\sqrt{2}$ | 0 | 2 | 0 | 0 | (x, y) |
| E_{2u} | 2 | 0 | 0 | -2 | 2 | 0 | 0 | -2 | 0 | 0 | 2 | -2 | 0 | 0 | |
| E_u | 2 | $-\sqrt{2}$ | $\sqrt{2}$ | 0 | -2 | 0 | 0 | -2 | $\sqrt{2}$ | $-\sqrt{2}$ | 0 | 2 | 0 | 0 | |

► The D_{nd} Groups

| D_{2d} | E | $2S_4$ | C_2 | $2C'_2$ | $2\sigma_d$ | (x axis coincident with C'_2) |
|----------|-----|--------|-------|---------|-------------|----------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | 1 | -1 | -1 | R_z |
| B_1 | 1 | -1 | 1 | 1 | -1 | $x^2 - y^2$ |
| B_2 | 1 | -1 | 1 | -1 | 1 | xy |
| E | 2 | 0 | -2 | 0 | 0 | $(x, y), (R_x, R_y)$ |

| D_{3d} | E | $2C_3$ | $3C_2$ | i | $2S_6$ | $3\sigma_d$ | (x axis coincident with C_2) |
|----------|-----|--------|--------|-----|--------|-------------|---------------------------------|
| A_{1g} | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_{2g} | 1 | 1 | -1 | 1 | 1 | -1 | R_z |
| E_g | 2 | -1 | 0 | 2 | -1 | 0 | (R_x, R_y) |
| A_{1u} | 1 | 1 | 1 | -1 | -1 | -1 | $(x^2 - y^2, xy); (xz, yz)$ |
| A_{2u} | 1 | 1 | -1 | -1 | -1 | 1 | z |
| E_u | 2 | -1 | 0 | -2 | 1 | 0 | (x, y) |

| D_{4d} | E | $2S_3$ | $2C_4$ | $2S_3^2$ | C_2 | $4C'_2$ | $4\sigma_d$ | (x axis coincident with C'_2) |
|----------|-----|-------------|--------|-------------|-------|---------|-------------|----------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_2 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | R_z |
| B_1 | 1 | -1 | 1 | -1 | 1 | 1 | -1 | z |
| B_2 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | (x, y) |
| E_1 | 2 | $\sqrt{2}$ | 0 | $-\sqrt{2}$ | -2 | 0 | 0 | $(x^2 - y^2, xy)$ |
| E_2 | 2 | 0 | -2 | 0 | 2 | 0 | 0 | (xz, yz) |
| E_3 | 2 | $-\sqrt{2}$ | 0 | $\sqrt{2}$ | -2 | 0 | 0 | (R_x, R_y) |

| D_{4d} | 1 | $2C_5$ | $2C_5^2$ | $5C_2$ | i | $2S_{10}^3$ | $2S_{10}$ | $5\sigma_d$ | (x axis coincident with C_2) |
|----------|---|--------------------|--------------------|--------|-----|---------------------|---------------------|-------------|---------------------------------|
| A_{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2, z^2$ |
| A_{2g} | 1 | 1 | 1 | -1 | 1 | 1 | 1 | -1 | R_z |
| E_{1g} | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | (R_x, R_y) |
| E_{2g} | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | (xz, yz) |
| A_{1u} | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | $(x^2 - y^2, xy)$ |
| A_{2u} | 1 | 1 | 1 | -1 | -1 | -1 | -1 | 1 | z |
| E_{1u} | 2 | $2 \cos 72^\circ$ | $2 \cos 144^\circ$ | 0 | -2 | $-2 \cos 72^\circ$ | $-2 \cos 144^\circ$ | 0 | (x, y) |
| E_{2u} | 2 | $2 \cos 144^\circ$ | $2 \cos 72^\circ$ | 0 | -2 | $-2 \cos 144^\circ$ | $-2 \cos 72^\circ$ | 0 | |

| D_{4d} | E | $2S_{12}$ | $2C_6$ | $2S_4$ | $2C_3$ | $2S_{12}^3$ | C_2 | $6C'_2$ | $6\sigma_d$ | (x axis coincident with C_2) |
|----------|-----|-------------|--------|--------|--------|-------------|-------|---------|-------------|---------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + z^2, z^2$ |
| A_2 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | -1 | -1 | R_z |
| B_1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | 1 | -1 | |
| B_2 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | -1 | 1 | z |
| E_1 | 2 | $\sqrt{3}$ | 1 | 0 | -1 | $-\sqrt{3}$ | -2 | 0 | 0 | (x, y) |
| E_2 | 2 | 1 | -1 | -2 | -1 | 1 | 2 | 0 | 0 | $(x^2 - y^2, xy)$ |
| E_3 | 2 | 0 | -2 | 0 | 2 | 0 | -2 | 0 | 0 | |
| E_4 | 2 | -1 | -1 | 2 | -1 | -1 | 2 | 0 | 0 | |
| E_5 | 2 | $-\sqrt{3}$ | 1 | 0 | -1 | $\sqrt{3}$ | -2 | 0 | 0 | (R_x, R_y) |
| | | | | | | | | | | (xz, yz) |

THE CUBIC GROUPS

► Tetrahedral Groups

| T | E | $4C_3$ | $4C_3^2$ | $3C_2$ | $\epsilon = \exp(2\pi i/3)$ |
|-----|-----|---|----------|--------|---------------------------------|
| A | | 1 | 1 | 1 | $x^2 + y^2 + z^2$ |
| E | | $\begin{cases} 1 & \epsilon \\ 1 & \epsilon^* \\ 1 & \epsilon^* \\ 1 & 1 \end{cases}$ | | | $(2z^2 - x^2 - y^2, x^2 - y^2)$ |
| T | | 3 | 0 | 0 | $(R, R_y, R_z), (x, y, z)$ |
| | | | | | (xy, xz, yz) |

| T_h | E | $4C_3$ | $4C_3^2$ | $3C_2$ | i | $4S_6$ | $4S_6^2$ | $3\sigma_h$ | $(\varepsilon = \exp(2\pi i/3))$ |
|-------|--|--|----------|--------|-----|--|--|-------------|----------------------------------|
| A_g | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2 + z^2$ |
| A_u | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | |
| E_g | $\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$ | $\begin{cases} \varepsilon^* \\ \varepsilon \end{cases}$ | 1 | 1 | 1 | $\begin{cases} \varepsilon \\ \varepsilon^* \end{cases}$ | $\begin{cases} \varepsilon^* \\ \varepsilon \end{cases}$ | 1 | $(2z^2 - x^2 - y^2, x^2 - y^2)$ |
| E_u | $\begin{cases} 1 & \varepsilon \\ 1 & \varepsilon^* \end{cases}$ | $\begin{cases} \varepsilon^* \\ \varepsilon \end{cases}$ | 1 | -1 | -1 | $\begin{cases} -\varepsilon \\ -\varepsilon^* \end{cases}$ | $\begin{cases} -\varepsilon^* \\ -\varepsilon \end{cases}$ | -1 | |
| T_g | 3 | 0 | 0 | -1 | 3 | 0 | 0 | -1 | (R_x, R_y, R_z) |
| T_u | 3 | 0 | 0 | -1 | -3 | 0 | 0 | 1 | (xz, yz, xy) |
| | | | | | | | | | (x, y, z) |

| T_d | E | $8C_3$ | $3C_2$ | $6S_4$ | $6\sigma_d$ | |
|-------|-----|--------|--------|--------|-------------|---------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2 + z^2$ |
| A_2 | 1 | 1 | 1 | -1 | -1 | |
| E | 2 | -1 | 2 | 0 | 0 | $(2z^2 - x^2 - y^2, x^2 - y^2)$ |
| T_1 | 3 | 0 | -1 | 1 | -1 | (R_x, R_y, R_z) |
| T_2 | 3 | 0 | -1 | -1 | 1 | (x, y, z) |
| | | | | | | (xy, xz, yz) |

► Octahedral Groups

| O | E | $6C_4$ | $3C_2 (= C_4^2)$ | $8C_3$ | $6C_2$ | |
|-------|-----|--------|------------------|--------|--------|---------------------------------|
| A_1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2 + z^2$ |
| A_2 | 1 | -1 | 1 | 1 | -1 | |
| E | 2 | 0 | 2 | -1 | 0 | $(2z^2 - x^2 - y^2, x^2 - y^2)$ |
| T_1 | 3 | 1 | -1 | 0 | -1 | $(R_x, R_y, R_z), (x, y, z)$ |
| T_2 | 3 | -1 | -1 | 0 | 1 | (xy, xz, yz) |

| O_h | E | $8C_3$ | $6C_2$ | $6C_4$ | $3C_2 (= C_4^2)$ | i | $6S_4$ | $8S_6$ | $3\sigma_h$ | $6\sigma_d$ | |
|----------|-----|--------|--------|--------|------------------|-----|--------|--------|-------------|-------------|---------------------------------|
| A_{1g} | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | $x^2 + y^2 + z^2$ |
| A_{2g} | 1 | 1 | -1 | -1 | 1 | 1 | -1 | 1 | 1 | -1 | |
| E_g | 2 | -1 | 0 | 0 | 2 | 2 | 0 | -1 | 2 | 0 | $(2z^2 - x^2 - y^2, x^2 - y^2)$ |
| T_{1g} | 3 | 0 | -1 | 1 | -1 | 3 | 1 | 0 | -1 | -1 | (R_x, R_y, R_z) |
| T_{2g} | 3 | 0 | 1 | -1 | -1 | 3 | -1 | 0 | -1 | 1 | (xz, yz, xy) |
| A_{1u} | 1 | 1 | 1 | 1 | 1 | -1 | -1 | -1 | -1 | -1 | |
| A_{2u} | 1 | 1 | -1 | -1 | 1 | -1 | 1 | -1 | -1 | 1 | |
| E_u | 2 | -1 | 0 | 0 | 2 | -2 | 0 | 1 | -2 | 0 | |
| T_{1u} | 3 | 0 | -1 | 1 | -1 | -3 | -1 | 0 | 1 | 1 | (x, y, z) |
| T_{2u} | 3 | 0 | 1 | -1 | -1 | -3 | 1 | 0 | 1 | -1 | |

Pemalar Asas dalam Kimia Fizik

| <u>Simbol</u> | <u>Keterangan</u> | <u>Nilai</u> |
|----------------------|-------------------|--|
| N_A | Nombor Avogadro | $6.022 \times 10^{23} \text{ mol}^{-1}$ |
| F | Pemalar Faraday | $96,500 \text{ C mol}^{-1}$, atau coulomb per mol, elektron |
| e | Cas elektron | $4.80 \times 10^{-10} \text{ esu}$ $1.60 \times 10^{-19} \text{ C atau coulomb}$ |
| m_e | Jisim elektron | $9.11 \times 10^{-28} \text{ g}$ $9.11 \times 10^{-31} \text{ kg}$ |
| m_p | Jisim proton | $1.67 \times 10^{-24} \text{ g}$ $1.67 \times 10^{-27} \text{ kg}$ |
| h | Pemalar Planck | $6.626 \times 10^{-27} \text{ erg s}$ $6.626 \times 10^{-34} \text{ J s}$ |
| c | Halaju cahaya | $3.0 \times 10^{10} \text{ cm s}^{-1}$ $3.0 \times 10^8 \text{ m s}^{-1}$ |
| R | Pemalar gas | $8.314 \times 10^7 \text{ erg K}^{-1} \text{ mol}^{-1}$ $8.314 \text{ J K}^{-1} \text{ mol}^{-1}$ $0.082 \text{ l atm K}^{-1} \text{ mol}^{-1}$ $1.987 \text{ cal K}^{-1} \text{ mol}^{-1}$ |
| k | Pemalar Boltzmann | $1.380 \times 10^{-16} \text{ erg K}^{-1} \text{ molekul}^{-1}$ $1.380 \times 10^{-23} \text{ J K}^{-1} \text{ molekul}^{-1}$ |
| g | | 981 cm s^{-2} 9.81 m s^{-2} |
| 1 atm | | 76 cmHg $1.013 \times 10^6 \text{ dyne cm}^{-2}$ $101,325 \text{ N m}^{-2}$ |
| $2.303 \frac{RT}{F}$ | | 0.0591 V, atau volt, pada 25°C |

Berat Atom yang Berguna

| | | | | |
|------------|------------|------------|------------|------------|
| H = 1.0 | C = 12.0 | I = 126.9 | Fe = 55.8 | As = 74.9 |
| Br = 79.9 | Cl = 35.5 | Ag = 107.9 | Pb = 207.0 | Xe = 131.1 |
| Na = 23.0 | K = 39.1 | N = 14.0 | Cu = 63.5 | F = 19.0 |
| O = 16.0 | S = 32.0 | P = 31.0 | Ca = 40.1 | Mg = 24.0 |
| Sn = 118.7 | Cs = 132.9 | Te = 128.0 | | |