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**UNIVERSITI SAINS MALAYSIA**

Peperiksaan Semester Pertama  
Sidang Akademik 2011/2012

Januari 2012

**EEE 445 – REKABENTUK LITAR ANALOG BERSEPADU**

Masa : 3 jam

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**ARAHAN KEPADA CALON:**

Sila pastikan bahawa kertas peperiksaan ini mengandungi **SEPULUH** muka surat bercetak dan **Lampiran SATU** muka surat sebelum anda memulakan peperiksaan ini.

Kertas soalan ini mengandungi **ENAM** soalan

Jawab **LIMA** soalan.

Mulakan jawapan anda untuk setiap soalan pada muka surat yang baru.

Agihan markah bagi soalan diberikan disudut sebelah kanan soalan berkenaan.

Jawab semua soalan di dalam Bahasa Malaysia atau Bahasa Inggeris atau kombinasi kedua-duanya.

**[Sekiranya terdapat sebarang percanggahan pada soalan peperiksaan, versi Bahasa Inggeris hendaklah diguna pakai].**

“In the event of any discrepancies, the English version shall be used”.

1. Rekabentuk penguat sumber-sepunya dengan beban resistif seperti yang ditunjukkan dalam litar skematik Rajah 1 mempunyai spesifikasi berikut:

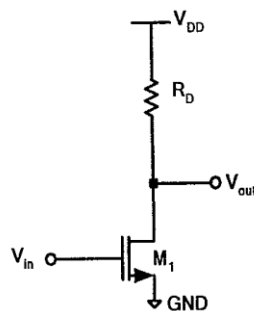
*The design of common-source amplifier with resistive load as shown in schematic circuit of Figure 1 below has the following specifications:*

- $V_{DD} = 1.8$  dan  $M_1$  dalam tepuan dengan voltan output minima bagi mengekalkan  $M_1$  dalam tepuan adalah 0.2V.

*$V_{DD} = 1.8V$  and  $M_1$  in saturation with minimum possible output voltage to keep  $M_1$  in saturation is 0.2V*

- Jumlah penggunaan kuasa penguat adalah 0.9mW.  
*Total power consumption of amplifier is 0.9mW.*

- Nilai gandaan mutlak adalah 10 untuk  $L=0.4 \mu\text{m}$   
*Absolute value of gain is 10 for  $L=0.4 \mu\text{m}$*



Rajah 1 : Penguat Sumber-Sepunya  
*Figure 1 : Common-Source amplifier*

Diberi parameter teknologi bagi transistor NMOS seperti berikut:

*Given the following technology parameter for the NMOS transistor:*

$$\lambda_{(\text{NMOS})} = 0, \gamma=0, V_{\text{TH}(\text{NMOS})} = 0.4\text{V}, \mu_n C_{\text{ox}} = 1 \text{ mA/V}^2.$$

Cari nilai-nilai berikut.

*Find the following values.*

- (i) Aras DC bagi input.  
*DC level of the input* (4 markah/marks)
- (ii) Lebar ( $W_1$ ) bagi transistor  $M_1$ .  
*Width ( $W_1$ ) of transistor  $M_1$*  (4 markah/marks)
- (iii)  $R_D$  (4 markah/marks)
- (iv) Aras nominal dc bias bagi nod output.  
*Nominal dc bias level of the output node.* (4 markah/marks)
- (v) Ayunan maksimum isyarat output bagi isyarat output simetri.  
*Maximum output signal swing for a symmetric output signal* (4 markah/marks)

2. (a) Terminal badan suatu transistor boleh digunakan sebagai input suatu penguat. Pertimbangkan litar bias PMOS seperti yang ditunjukkan dalam litar Rajah 2. Bagi  $V_{\text{bias}} = 1.4\text{V}$ , hitungkan untung isyarat-kecil bagi penguat PMOS, dengan mengambilkira  $g_{\text{mb}} = \eta g_{\text{m}}$ .

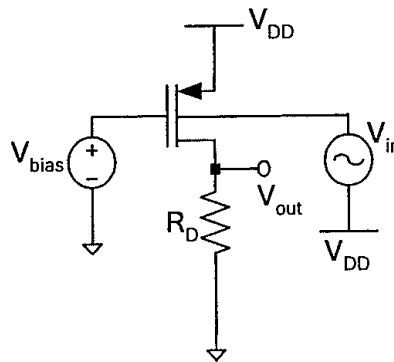
*It is possible to use the bulk terminal of a transistor as an input of an amplifier. Consider the PMOS bias circuit shown in Figure 2. For  $V_{\text{bias}} = 1.4\text{V}$ , calculate the small-signal gain of the PMOS amplifier, considering  $g_{\text{mb}} = \eta g_{\text{m}}$ .*

Andaikan parameter PMOS:

Assume PMOS parameters:

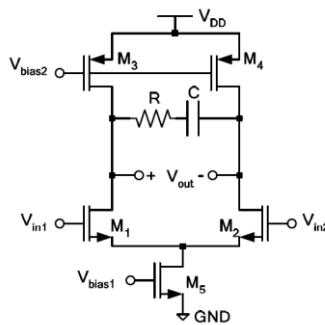
$\lambda=0$ ,  $\eta=0.2$ ,  $V_{TH(PMOS)} = -0.6V$ ,  $\mu_p C_{ox} = 100 \mu A/V^2$ ,  $R_D = 1k\Omega$ ,  $(W/L)_{PMOS}=20$ ,  
dan/and  $V_{DD} = 3V$ .

(8 markah/marks)



Rajah 2  
Figure 2

2. (b)



Rajah 3  
Figure 3

Bagi litar di atas, andai transistor  $M_1$  dan  $M_2$  serupa, dan  $M_3$  dan  $M_4$  serupa dan  $\gamma=0$ ,  
 $\lambda \neq 0$ :

In the above circuit, assume transistor  $M_1$  and  $M_2$ , and  $M_3$  and  $M_4$  are identical and  
 $\gamma=0$ ,  $\lambda \neq 0$ :

...5/-

- (i) Tentukan ungkapan bagi gandaan voltan pembeza isyarat-kecil  $\frac{V_{out}}{V_{in1} - V_{in2}}$  bagi litar tersebut.

*Find the expression for the small-signal differential voltage gain  $\frac{V_{out}}{V_{in1} - V_{in2}}$  of the circuit.*

- (ii) Apakah gandaan litar pada frekuensi rendah?  
*What is the gain of the circuit at very low frequencies?*
- (iii) Apakah gandaan litar pada frekuensi tinggi?  
*What is the gain of the circuit at very high frequencies?*

(12 markah/marks)

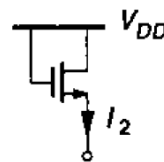
3. (a) Jelaskan mengapa struktur dalam litar-litar di bawah tidak dapat beroperasi sebagai sumber arus walaupun transistor-transistor adalah dalam tepuan.

*Explain why the structures in the Figure below cannot operate as current sources even though the transistors are in saturation.*

(4 markah/marks)



Rajah 4(a)  
Figure 4(a)

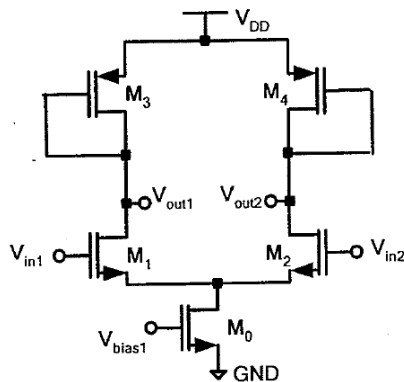


Rajah 4(b)  
Figure 4(b)

- (b) Rekabentuk penguat pembeza simetri berdasarkan litar dalam Rajah 5, dengan spesifikasi berikut:

*Design a symmetric differential amplifier based on the circuit in Figure 5 with the following design specifications:*

- $V_{DD} = 1.8V$
- Jumlah penggunaan kuasa 1.8mW  
*Total power consumption of 1.8 mW*
- Aras DC output 0.9V.  
*Output DC level of 0.9V*
- Jumlah gandaan 5.  
*Total gain of 5*
- $L = 0.4 \mu m$  untuk semua peranti.  
 *$L = 0.4 \mu m$  for all devices*



Rajah 5: Penguat pembeza simetri  
*Figure 5 : Symmetric Differential Amplifier*

Andaikan voltan minimum yang diperlukan pada salir  $M_0$  untuk mengekalkannya pada tepuan adalah 0.2V.

*Assume that the minimum required voltage at the drain of  $M_0$  to keep it in saturation is 0.2V.*

Parameter teknologi adalah:  
*The technology parameters are:*

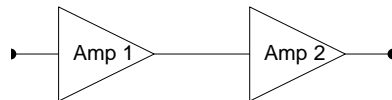
$$\lambda_{(NMOS, PMOS)} = 0, \gamma = 0, V_{TH(NMOS)} = |V_{TH(PMOS)}| = 0.4V, \mu_n C_{ox} = 1 \text{ mA/V}^2$$
$$\mu_p C_{ox} = 0.5 \text{ mA/V}^2, \text{ and } V_{DD} = 1.8V.$$

- (i) Tentukan  $V_{bias1}$ , dan kesemua lebar transistor ( $W_0, W_1, W_2, W_3$  dan  $W_4$ )  
*Find  $V_{bias1}$ , and all the transistor widths ( $W_0, W_1, W_2, W_3$  and  $W_4$ )*
- (ii) Tentukan minimum dan maksimum aras input DC.  
*Find the minimum and maximum allowable input DC levels.*

(16 markah/marks)

4. (a) Lukiskan penguat kendalian menyongsang dengan gandaan  $-\frac{R_f}{R_S}$  dan huraikan jumlah hingar keluaran.  
*Draw an inverting operational amplifier with gain of  $-\frac{R_f}{R_S}$  and derive the total output noise.*

(6 markah/marks)



Rajah 6: Dua lara penguat kendalian menyongsang  
*Figure 6: Two inverting operational amplifier in cascade*

- (b) Sekiranya  $R_S = 50 \Omega$  untuk penguat 1 dan 2 (Rajah 6), tentukan jumlah hingar keluaran untuk setiap penguat sekiranya  $R_f = 100 \Omega$  untuk penguat 1 dan  $200 \Omega$  untuk penguat 2.

*If source resistance,  $R_S = 50 \Omega$  for amplifier 1 and amplifier 2 (Figure 6), determine total output noise voltage for each amplifier if feedback resistance,  $R_f = 100 \Omega$  for amplifier 1 and  $200 \Omega$  for amplifier 2.*

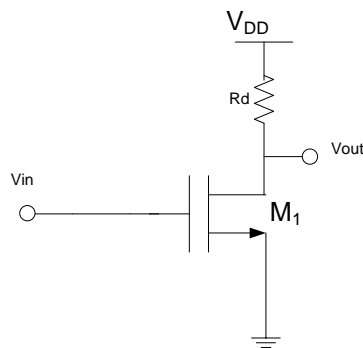
(8 markah/marks)

- (c) Kirakan faktor hingar bagi setiap penguat.  
*Calculate the noise factor for each amplifier.*

(6 markah/marks )

5. Fungsi pindah bagi litar dalam Rajah 7 adalah  
*The transfer function of circuit in Figure 7 is,*

$$\frac{V_{OUT}(s)}{V_{IN}} = \frac{-g_m R_D}{\left(1 + \frac{s}{\omega_{in}}\right)\left(1 + \frac{s}{\omega_{out}}\right)}$$



Rajah 7: Penguat Punca Sepunya  
*Figure 7: Common source amplifier*

- (a) Tentukan ungkapan untuk kutub masukan dan kirakan nilai ia sekiranya if  $R_s = 50 \Omega$ ,  $C_{gs} = 0.1 \text{ pF}$ ,  $g_m = 0.02 \text{ A/V}$ ,  $R_d = 500 \Omega$ ,  $C_{gd} = 0.01 \text{ pF}$  dan  $C_{db} = 0.001 \text{ pF}$ .

*Determine the expression for input pole and calculate the value if  $R_s = 50 \Omega$ ,  $C_{gs} = 0.1 \text{ pF}$ ,  $g_m = 0.02 \text{ A/V}$ ,  $R_d = 500 \Omega$ ,  $C_{gd} = 0.01 \text{ pF}$  and  $C_{db} = 0.001 \text{ pF}$ .*

(7 markah/marks)



- (b) Tentukan ungkapan untuk kutub keluaran dan kirakan nilai ia sekiranya if  $R_s = 50 \Omega$ ,  $C_{gs} = 0.1 \text{ pF}$ ,  $g_m = 0.02 \text{ A/V}$ ,  $R_d = 500 \Omega$ ,  $C_{gd} = 0.01 \text{ pF}$  dan  $C_{db} = 0.001 \text{ pF}$ .

*Determine the expression for output pole calculate the value if  $R_s = 50 \Omega$ ,  $C_{gs} = 0.1 \text{ pF}$ ,  $g_m = 0.02 \text{ A/V}$ ,  $R_d = 500 \Omega$ ,  $C_{gd} = 0.01 \text{ pF}$  and  $C_{db} = 0.001 \text{ pF}$ .*

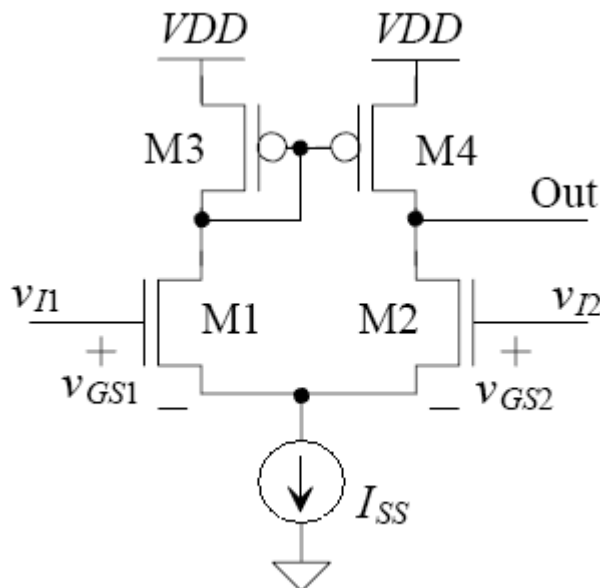
(7 markah/marks)

- (c) Apakah nilai gandaan yang diperlukan sekiranya jalur yang ditentukan ialah 15 MHz?. Beban ialah 50 pF. Dengan bebanan tersebut, apakah pandangan anda mengenai kestabilan litar itu

*What is the required gain if the wanted bandwidth is 15 MHz if external load is 50 pF? With the capacitive load, what is your prediction of the stability of the circuit*

(6 markah/marks)

6.



Rajah 8: Penguat Kebezaan

Figure 8: Differential Amplifier

- (a) Sekiranya W/L bagi M1 dan M2 ialah 10/2,  $\mu_n \cdot C_{ox} = 120 \mu A/V^2$  dan  $I_{SS} = 50 \mu A$ . Jika  $V_{I2} = 2.4 V$ , kirakan maksimum dan minimum voltan bagi get M1 supaya M1 dan M2 tidak tutup.

*Assume that W/L of M1 and M2 is 10/2,  $\mu_n \cdot C_{ox} = 120 \mu A/V^2$  and  $I_{SS} = 50 \mu A$ . If  $V_{I2} = 2.4 V$  (common mode voltage), calculate the maximum and minimum voltage on the gate of M1 that ensures neither M1 nor M2 shut off. Draw  $I_{D2}$  vs  $V_{I2}$ .*

(8 markah/marks)

- (b) (i) Lukiskan litar setara isyarat kecil untuk Rajah 8.  
*Draw small signal equivalent circuit for Figure 8.*

(6 markah/marks)

- (ii) Apakah tertib pertama gandaan mod kebezaan?  
*What is the first order differential mode gain?*

(3 markah/marks)

- (iii) Kira gandaan mod kebezaan apabila  $\lambda_n = 0.01 V^{-1}$  dan  $\lambda_p = 0.0125 V^{-1}$   
*Calculate the differential mode gain if  $\lambda_n = 0.01 V^{-1}$  and  $\lambda_p = 0.0125 V^{-1}$*

(3 markah/marks)

## Senarai Persamaan Umum/List of general equations

## 1. Current Equations for NMOS:

$$I_D = I_{DS} = \begin{cases} 0 & ; \text{if } V_{GS} < V_{TH} \text{ (Cut-off)} \\ \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot (V_{GS} - V_{TH}) \cdot V_{DS} & ; \text{if } V_{GS} > V_{TH}, V_{DS} \ll 2(V_{GS} - V_{TH}) \text{ (Deep Triode)} \\ \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot \left[ (V_{GS} - V_{TH}) \cdot V_{DS} - \frac{1}{2} \cdot V_{DS}^2 \right] & ; \text{if } V_{GS} > V_{TH}, V_{DS} < V_{GS} - V_{TH} \text{ (Triode)} \\ \frac{1}{2} \cdot \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot (V_{GS} - V_{TH})^2 & ; \text{if } V_{GS} > V_{TH}, V_{DS} > V_{GS} - V_{TH} \text{ (Saturation)} \end{cases}$$

## 2. Current Equations for PMOS:

$$I_D = I_{SD} = \begin{cases} 0 & ; \text{if } V_{SG} < |V_{TH}| \text{ (Cut-off)} \\ \mu_p \cdot C_{ox} \cdot \frac{W}{L} \cdot (V_{SG} - |V_{TH}|) \cdot V_{SD} & ; \text{if } V_{SG} > |V_{TH}|, V_{SD} \ll 2(V_{SG} - |V_{TH}|) \text{ (Deep Triode)} \\ \mu_p \cdot C_{ox} \cdot \frac{W}{L} \cdot \left[ (V_{SG} - |V_{TH}|) \cdot V_{SD} - \frac{1}{2} \cdot V_{SD}^2 \right] & ; \text{if } V_{SG} > |V_{TH}|, V_{SD} < V_{SG} - |V_{TH}| \text{ (Triode)} \\ \frac{1}{2} \cdot \mu_p \cdot C_{ox} \cdot \frac{W}{L} \cdot (V_{SG} - |V_{TH}|)^2 & ; \text{if } V_{SG} > |V_{TH}|, V_{SD} > V_{SG} - |V_{TH}| \text{ (Saturation)} \end{cases}$$

## 3. Transconductance in triode:

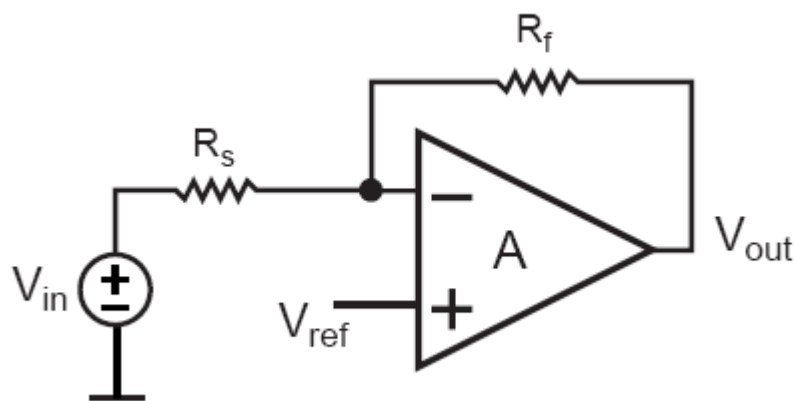
$$\begin{aligned} g_m &= \frac{\partial}{\partial V_{GS}} \left( \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot \left[ (V_{GS} - V_{TH}) \cdot V_{DS} - \frac{1}{2} \cdot V_{DS}^2 \right] \right) \Big|_{V_{DS} = \text{Const.}} \\ &= \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot V_{DS} \end{aligned}$$

## 4. Transconductance in saturation:

$$\begin{aligned} g_m &= \frac{\partial}{\partial V_{GS}} \left( \frac{1}{2} \cdot \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot (V_{GS} - V_{TH})^2 \right) \Big|_{V_{DS} = \text{Const.}} \\ &= \mu_n \cdot C_{ox} \cdot \frac{W}{L} \cdot (V_{GS} - V_{TH}) \end{aligned}$$

## Marking Scheme

4(a).



$$\overline{v_{nout(tot)}^2} \approx \left( \frac{-R_f}{R_s} \right)^2 \overline{e_{nR_s}^2} + \overline{e_{nR_f}^2}$$

( 6 pts )

(b)

Amplifier 1 : Output noise voltage =  $2^2 * 4KTR_S + 4KTR_F$   
 $= 4 * 8.28E-19 + 1.65E-18 = 4.968E-18 \text{ V}^2/\text{Hz}$  ( 4 pts )

Amplifier 2: Output noise voltage =  $4^2 * 4KTR_S + 4KTR_F$   
 $= 16 * 8.28E-19 + 3.312E-18 = 1.65E-17 \text{ V}^2/\text{Hz}$  ( 4 pts )

(c)

Amplifier =  $1 + R_s/R_f = 1 + 50/100 = 1.5$

Amplifier =  $1 + R_s/R_f = 1 + 50/200 = 1.25$  ( 6 pts )

5.

a). Determine the expression for input pole.

$$f_{p,in} = \frac{1}{2\pi R_S [C_{GS} + (1 + g_m R_D) C_{GD}]}$$

b). Determine the expression for output pole.

$$f_{p,out} = \frac{1}{2\pi [(C_{GD} + C_{DB}) R_D]}$$

c). Gain bandwidth product =  $g_m / C_{out}$ , = 0.02 / 50 pF

Gain = Gain bandwidth product / Bandwidth

Gain = 0.02 / 50 pF / 15e6 = 26.6

5. a).

$$V_{I1max} = \text{SQRT}(2 \cdot L \cdot I_{SS} / W \cdot \mu_n \cdot C_{ox}) + V_{I2}$$

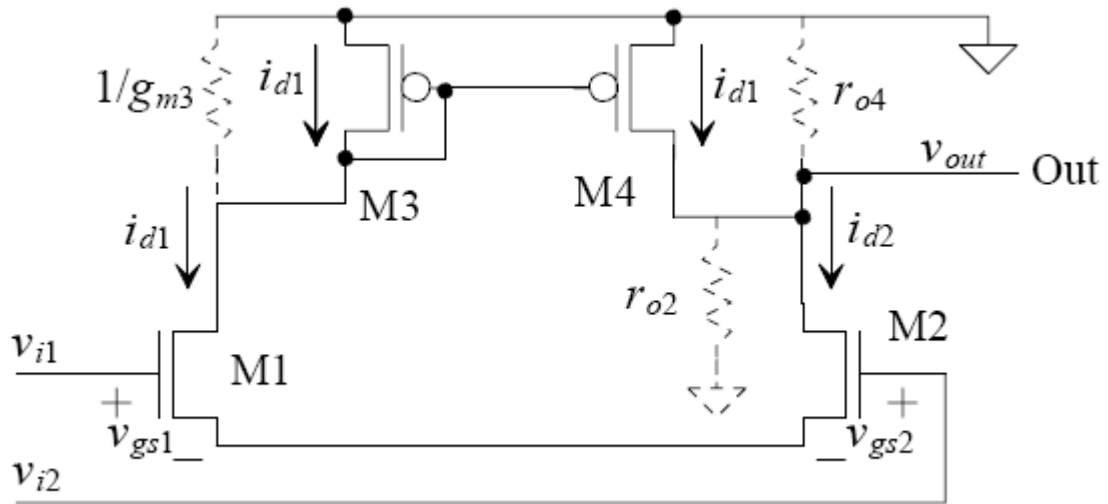
$$V_{I1max} = \text{SQRT}(2 \cdot L \cdot I_{SS} / W \cdot \mu_n \cdot C_{ox}) + 2.4 \text{ V}$$

Replace all given parameters.

$$V_{I1max} = 0.408 + 2.4 \text{ V} = 2.808 \text{ V}$$

$$V_{I1min} = 2.4 - 0.408 = 1.992 \text{ V}.$$

b).  
i.



Mark will be given based on.

1. Vdd is changed to ground
2. ISS replace with an open.
3.  $r_{o2}$  and  $r_{o4}$  are drawn.

ii. Based on the given Figure,  
 $A_d = g_m \cdot (r_{o2} // r_{o4})$ .

iii.  $g_m = 1.73 \text{ e-}4$ , based on given parameters.  
 $r_{o2} = 1 / \lambda_n I_d = 4 \text{ e}6 \text{ Ohm}$   $r_{o4} = 1 / \lambda_p I_d = 3.2 \text{ e}6$

so gain =  $1.73 \text{ e-}4 \times 1.77 \text{ e}6 = 307$