
UNIVERSITI SAINS MALAYSIA

First Semester Examination
Academic Session 2009/2010

November 2009

EEE 510 – ADVANCED ANALOGUE CIRCUIT DESIGN

Duration: 3 hours

INSTRUCTION TO CANDIDATE:

Please check that this examination paper contains **SIX (6)** pages of printed material before you begin the examination.

This paper contains **SIX (6)** questions.

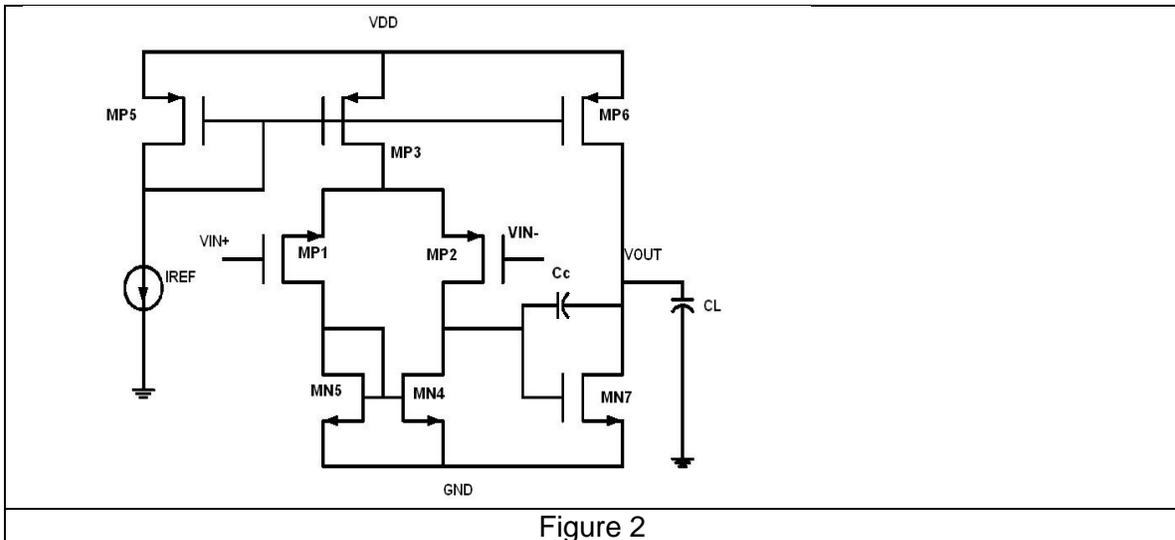
Instructions: Answer **FIVE (5)** questions.

Answer to any question must start on a new page.

Distribution of marks for each question is given accordingly.

All questions must be answered in English.

2. Refer to Figure 2



(a) Find expression of first dominant pole. (10%)

(b) Find the ratio of input gm first stage and second ratio if you were to place the second dominant pole 1.5 times unity frequency. Assume that C_c is equivalent to $0.5 C_L$.

(10%)

3. State the region of operating for nmos and conditions

(a) Saturation (5%)

(b) Triode (5%)

(c) Cutoff (5%)

(d) What is the effect of threshold voltage if there exists substrate voltage. (5%)

4. (a) Proof that small-signal transfer function of small-signal differential mode half-circuit (see Figure 3) is obtained as follows.

$$A_v(s) = \frac{g_{mi}g_{mL}R_{oB}R_L(1-s^2/(g_{mB}g_{mL}/C_B C_C))}{(1+g_{mL}R_L R_{oB} C_C s)(1+(C_B(C_L+C_C)/g_{mL} C_C)s+(C_L C_B/g_{mB}g_{mL})s^2)} \quad (1)$$

(16%)

- (b) From equation [1], how many dominant pole, non-dominant pole and zeros are there?

(4%)

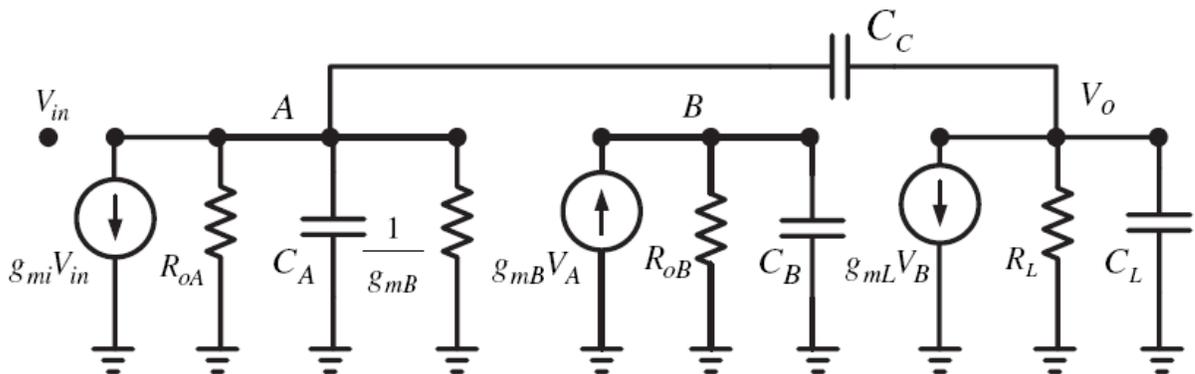


Figure 3 : Small-signal model of the differential mode half-circuit of two stage fully differential

- 5. (a) Draw the large signal equivalent circuit of the circuit in Figure 4. (8%)
- (b) Draw the small signal equivalent circuit of the circuit in Figure 4. (8%)
- (c) If $R_C = 5\text{ k}\Omega$, $I_C = 100\text{ }\mu\text{A}$ and current gain, $\beta = 100$, determine the gain, A_V of the circuit in Figure 4.

(4%)

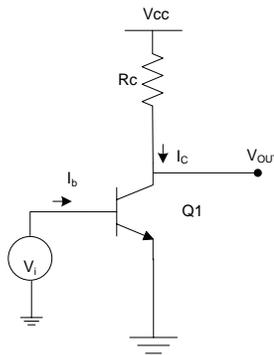


Figure 4 : Common Emitter Amplifier

- 6. (a) Figure 5 shows a typical Class A Bipolar amplifier. Based on the circuit, proof that the ideal efficiency of the amplifier is 25 %.

(10%).

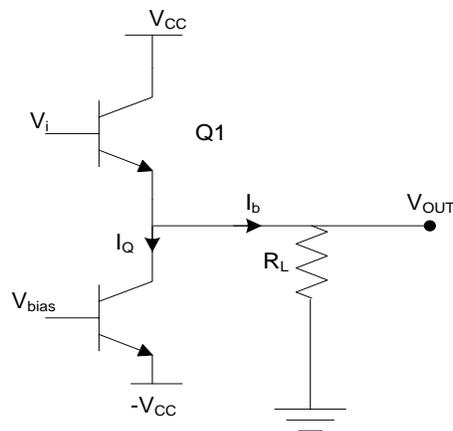


Figure 5. Class A Amplifier

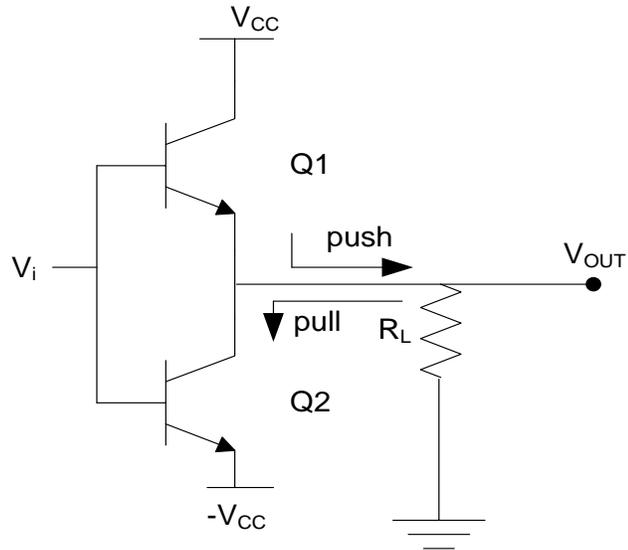


Figure 6. Class B Amplifier

- (b) Figure 6 shows a typical Class B Bipolar amplifier. Based on the circuit, proof that the ideal efficiency of the amplifier is 78.6 %.

(10%)

SOLUTIONS

Marking Scheme

1. a. Applying KCL at the two internal nodes and at output node gives three equations

$$v_o/Z_L + g_{m5}v_a = sC_c(v_b - v_o)$$

$$g_{m7}v_b = v_a/Z_A - (v_b - v_a)/r_{o7}$$

$$-g_{m1}v_i = v_b/Z_B + sC_c(v_b - v_o) + (v_b - v_a)/r_{o7} + g_{m7}v_b$$

where

$$Z_A = R_{oA}/(1 + sR_{oA}C_A)$$

$$Z_B = R_{oB}/(1 + sR_{oB}C_B)$$

$$Z_L = R_L/(1 + sR_LC_L)$$

These equations can be used to find the transfer function:

$$\frac{v_o}{v_i}(s) = G \frac{n_0 + n_1s + n_2s^2}{a_0 + a_1s + a_2s^2 + a_3s^3}$$

$$\begin{aligned} a_0 &= 1 + \frac{R_{oA}}{g_{m7}R_{oB}r_{o7}} + \frac{1}{g_{m7}R_{oB}} + \frac{1}{g_{m7}r_{o7}} \\ a_1 &= \tau_A \left(1 + \frac{1}{g_{m7}R_{oB}} + \frac{1}{g_{m7}r_{o7}} \right) + \frac{\tau_B}{g_{m7}R_{oB}} \left(1 + \frac{R_{oA}}{r_{o7}} \right) \\ &+ \tau_L \left(1 + \frac{1}{g_{m7}R_{oB}} + \frac{1}{g_{m7}r_{o7}} + \frac{R_{oA}}{g_{m7}R_{oB}r_{o7}} \right) \\ &+ R_L C_c \left(1 + \frac{1}{g_{m7}R_{oB}} + \frac{1}{g_{m7}r_{o7}} + \frac{R_{oA}}{g_{m7}R_{oB}r_{o7}} \right) \\ &+ g_{m5}R_L R_{oA} C_c \left(1 + \frac{1}{g_{m7}r_{o7}} + \frac{1}{g_{m5}g_{m7}R_L R_{oA}} + \frac{1}{g_{m5}g_{m7}r_{o7}R_L} \right) \end{aligned}$$

$$\begin{aligned}
a_2 &= \tau_B \tau_L \left(\frac{R_{oA}}{g_{m7} R_{oB} r_{o7}} + \frac{1}{g_{m7} R_{oB}} \right) + \tau_B R_L C_c \left(\frac{R_{oA}}{g_{m7} R_{oB} r_{o7}} + \frac{1}{g_{m7} R_{oB}} \right) \\
&+ \tau_A \tau_L \left(1 + \frac{1}{g_{m7} R_{oB}} + \frac{1}{g_{m7} r_{o7}} \right) + \tau_A R_L C_c \left(1 + \frac{1}{g_{m7} R_{oB}} + \frac{1}{g_{m7} r_{o7}} + \frac{1}{g_{m7} R_L} \right) \\
&+ \tau_L R_{oA} C_c \left(\frac{1}{g_{m7} r_{o7}} + \frac{1}{g_{m7} R_{oA}} \right) + \tau_B \tau_A \left(\frac{1}{g_{m7} R_{oB}} \right) \\
a_3 &= \frac{\tau_A (C_B \tau_L + C_B R_L C_c + \tau_L C_c)}{g_{m7}} \\
G &= g_{m1} g_{m5} R_{oA} R_L \\
n_0 &= 1 + \frac{1}{g_{m7} r_{o7}} \\
n_1 &= - \frac{(R_{oA} + r_{o7}) C_c}{g_{m5} R_{oA} g_{m7} r_{o7}} \\
n_2 &= - \frac{C_A C_c}{g_{m5} g_{m7}}
\end{aligned}$$

where

$$\tau_A = R_{oA} C_A$$

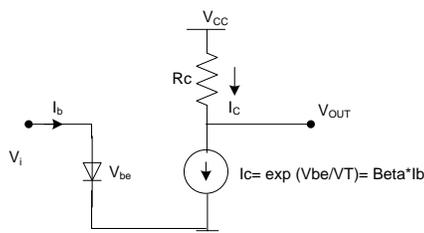
$$\tau_B = R_{oB} C_B$$

$$\tau_L = R_L C_L$$

b. one real dominant pole, two non-dominant pole and two zeros.

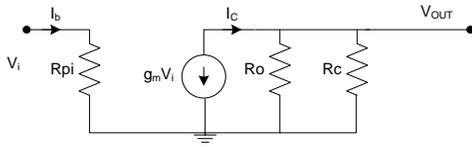
2.

a.



Students are required to explain briefly each parameters/components.

b.



Students are required to explain briefly each parameters/components.

c. $A_v = -g_m R_c$,
 $g_m = I_c / V_T = 100 \mu\text{A} / 25 \text{ mV} = 4 \text{ mS}$
 so, $A_v = -4 \text{ mS} * 5 \text{ k}\Omega = 20$

3.

a.

Consider the output signal power that can be delivered to load R_L when sinusoidal input is applied at V_i . Assuming that V_o is approximately sinusoidal, the average power delivered to R_L is

$$P_L = (1/2) * V_{op} * I_{opeak}$$

If the P_{Lmax} is maximum value of P_L

$$P_{Lmax} = (1/2) * V_{ompeak} * I_{ompeak}$$

Where $V_{ompeak} = V_{CC} - V_{CE(sat)}$ and $I_{ompeak} = I_Q$

Efficiency = P_L / P_{supply} ,

$$P_{supply} = 2V_{CC} * I_Q$$

$$\text{Finally, Efficiency} = (1/2) * (V_{CC} - V_{CE(sat)}) * I_Q / 2V_{CC} * I_Q$$

We have, , Efficiency = $(1/4) * (1 - V_{CE(sat)} / V_{CC})$, because $V_{CE(sat)} \ll V_{CC}$,

Therefore Efficiency = $1/4$ or 25 %.

b.

Due to nature of the current waveform, integration of collector current is required to (students need to show this) establish, $I_{supply} = (1/\pi) (I_{opeak})$

Thus

$$P_{\text{supply}} = (2/\pi)V_{\text{CC}} * V_{\text{op}} / R_{\text{L}}$$

While, the average power delivered to load R_{L}

$$P_{\text{L}} = (1/2) * V_{\text{op}}^2 / R_{\text{L}}$$

Therefore, Efficiency = $(\pi / 4) * (V_{\text{op}}/V_{\text{CC}})$. Student still continue further, but this expression is enough to show the efficiency is 78.6 % with some assumption.