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UNIVERSITI SAINS MALAYSIA

Peperiksaan Semester Kedua  
Sidang Akademik 2003/2004

Februari/Mac 2004

**JIK 317 – Kimia Kuantum & Teori Kumpulan**

Masa : 3 jam

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Sila pastikan bahawa kertas peperiksaan ini mengandungi ENAM BELAS muka surat yang bercetak sebelum anda memulakan peperiksaan ini.

Jawab LIMA soalan sahaja.

Setiap jawapan mesti dijawab di dalam buku jawapan yang disediakan.

Setiap soalan bernilai 20 markah dan markah subsoalan diperlihatkan di penghujung subsoalan itu.

...2/-

1. (a) Dengan berpandukan contoh molekul yang sesuai, jelaskan istilah-istilah berikut:

- (i) Pusat penyongsangan,  $i$
- (ii) Paksi putaran tak wajar,  $S_n$
- (iii) Karakter,  $\chi$

(6 markah)

(b) Bagi molekul *cis*-PtBr<sub>2</sub>Cl<sub>2</sub>

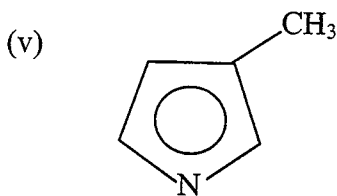
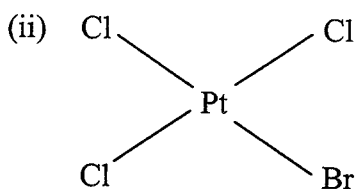
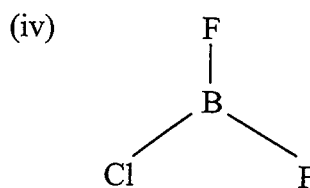
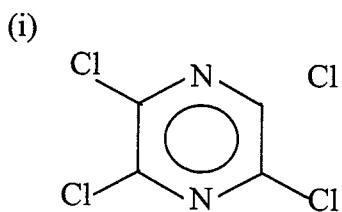
- (i) Tentukan kumpulan titiknya.
- (ii) Terbitkan matrik  $3 \times 3$  bagi setiap operasi simetri yang tergolong dalam kumpulan titik tersebut.
- (iii) Daripada matrik dalam (ii), tentukan nilai karakter bagi setiap operasi tersebut.

(14 markah)

2. Bagi setiap molekul berikut:

(a) Senaraikan unsur-unsur simetri.

(b) Tentukan kumpulan titik



(iii)  $H - C \equiv N$

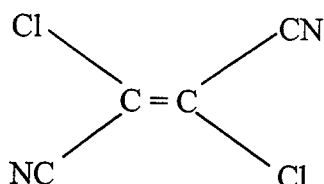
(15 markah)

...3/-

- (c) Dengan contoh molekul yang sesuai, bezakan antara namatanda  $C_{2h}$  dan  $D_{2h}$ .

(5 markah)

3. Bagi molekul yang mempunyai struktur berikut:



- (a) Jelaskan cara bagaimana menentukan kumpulan titiknya.

(5 markah)

- (b) Dapatkan perwakilan terturunkan bagi

(i)  $\Gamma_{C-Cl}$  (ikatan C – Cl sebagai fungsi dasar)

(ii)  $\Gamma_{C-CN}$  (ikatan C – CN sebagai fungsi dasar)

(4 markah)

- (c) Seterusnya, dengan proses penurunan, dapatkan perwakilan tak terturunkan bagi

(i)  $\Gamma_{C-Cl}$

(ii)  $\Gamma_{C-CN}$

(6 markah)

- (d) Tentukan getaran yang aktif dalam Raman dan inframerah untuk molekul tersebut.

(5 markah)

...4/-

4. Fungsi gelombang pada masa  $t = 0$  untuk satu zarah bebas diberikan oleh persamaan

$$\Psi(x, 0) = A e^{\frac{-x^2}{a^2} + ik_0 x}$$

- (a) Hitung faktor A. (5 markah)
- (b) Hitung ketumpatan kebarangkalian  $\rho$ . (5 markah)
- (c) Tentukan kedudukan di mana fungsi ini memuncak. (5 markah)
- (d) Hitung kebarangkalian ketumpatan arus

$$j_x = \frac{i\hbar}{2m} \left( \Psi \frac{\partial \Psi^*}{\partial x} - \Psi^* \frac{\partial \Psi}{\partial x} \right)$$

(5 markah)

5. (a) Terangkan tiga keputusan eksperimen Kesan Fotoelektrik yang tidak dapat diterangkan oleh mekanik klasik. (10 markah)
- (b) Fungsi gelombang untuk satu zarah diberikan oleh persamaan

$$\Psi(x) = A e^{\frac{-x^2}{a^2} + ik_0 x}$$

- (i) Hitung nilai jangkaan untuk kedudukan zarah. (5 markah)
- (ii) Hitung nilai jangkaan untuk momentum zarah. (5 markah)

...5/-

6. (a) Hitung ungkapan nyata untuk operator berikut:

(i)  $\left(\frac{d}{dx} x\right)^2$  (4 markah)

(ii)  $\left(\frac{d}{dx} + \frac{1}{x}\right)^3$  (4 markah)

(iii)  $\left(x \frac{d}{dx}\right)^2$  (4 markah)

(b) Hitung hubungan komutasi untuk operator berikut:

(i)  $x$  dan  $\frac{d}{dx}$  (4 markah)

(ii)  $\frac{\partial}{\partial \varphi}$  dan  $f(r, \theta, \varphi)$  (4 markah)



# Character Tables

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## THE NONAXIAL GROUPS

$C_1$	$E$		
$A$	1		
$C_2$	$E \sigma_h$		
$A'$	1 1	$x, y, R_z$	$x^2, y^2, z^2, xy$
$A''$	1 -1	$z, R_x, R_y$	$yz, xz$
$C_3$	$E i$		
$A_1$	1 1	$R_x, R_y, R_z$	$x^2, y^2, z^2, xy, xz, yz$
$A_2$	1 -1	$x, y, z$	

## THE AXIAL GROUPS

### ► The $C_n$ Groups

$C_2$	$E C_2$		
$A$	1 1	$z, R_z$	$x^2, y^2, z^2, xy$
$B$	1 -1	$x, y, R_x, R_y$	$yz, xz$
$C_3$	$E C_3 C_3^2$	$\varepsilon = \exp(2\pi i/3)$	
$A$	1 1 1	$z, R_z$	$x^2 + y^2, z^2$
$E$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^2 \\ 1 & \varepsilon^2 & \varepsilon \end{Bmatrix}$	$(x, y), (R_x, R_y)$	$(x^2 - y^2, xy), (yz, xz)$

$C_4$	$E$	$C_4$	$C_2$	$C_4^3$		
$A$	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$B$	1	-1	1	-1		$x^2 - y^2, xy$
$E$	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$				$(x, y), (R_x, R_y)$	$(xz, yz)$

$C_5$	$E$	$C_5$	$C_5^2$	$C_5^3$	$C_5^4$	$\varepsilon = \exp(2\pi i/5)$	
$A$	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$E_1$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^2 & \varepsilon^{2*} & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon^{2*} & \varepsilon^2 & \varepsilon \end{Bmatrix}$					$(x, y), (R_x, R_y)$	$(yz, xz)$
$E_2$	$\begin{Bmatrix} 1 & \varepsilon^2 & \varepsilon^* & \varepsilon & \varepsilon^{2*} \\ 1 & \varepsilon^{2*} & \varepsilon & \varepsilon^* & \varepsilon^2 \end{Bmatrix}$						$(x^2 - y^2, xy)$

$C_6$	$E$	$C_6$	$C_3$	$C_2$	$C_3^2$	$C_6^5$	$\varepsilon = \exp(2\pi i/6)$	
$A$	1	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$B$	1	-1	1	-1	1	-1		
$E_1$	$\begin{Bmatrix} 1 & \varepsilon & -\varepsilon^* & -1 & -\varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & -\varepsilon & -1 & -\varepsilon^* & \varepsilon \end{Bmatrix}$						$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	$\begin{Bmatrix} 1 & -\varepsilon^* & -\varepsilon & 1 & -\varepsilon^* & -\varepsilon \\ 1 & -\varepsilon & -\varepsilon^* & 1 & -\varepsilon & -\varepsilon^* \end{Bmatrix}$							$(x^2 - y^2, xy)$

$C_7$	$E$	$C_7$	$C_7^2$	$C_7^3$	$C_7^4$	$C_7^5$	$C_7^6$	$\varepsilon = \exp(2\pi i/7)$	
$A$	1	1	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$E_1$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^2 & \varepsilon^3 & \varepsilon^{3*} & \varepsilon^{2*} & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon^{2*} & \varepsilon^{3*} & \varepsilon^3 & \varepsilon^2 & \varepsilon \end{Bmatrix}$							$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	$\begin{Bmatrix} 1 & \varepsilon^2 & \varepsilon^{3*} & \varepsilon^* & \varepsilon & \varepsilon^3 & \varepsilon^{2*} \\ 1 & \varepsilon^{2*} & \varepsilon^3 & \varepsilon & \varepsilon^* & \varepsilon^{3*} & \varepsilon^2 \end{Bmatrix}$								$(x^2 - y^2, xy)$
$E_3$	$\begin{Bmatrix} 1 & \varepsilon^3 & \varepsilon^* & \varepsilon^2 & \varepsilon^{2*} & \varepsilon & \varepsilon^{3*} \\ 1 & \varepsilon^{3*} & \varepsilon & \varepsilon^{2*} & \varepsilon^2 & \varepsilon^* & \varepsilon^3 \end{Bmatrix}$								

$C_8$	$E$	$C_8$	$C_4$	$C_2$	$C_3^2$	$C_8^3$	$C_8^5$	$C_8^7$	$\varepsilon = \exp(2\pi i/8)$	
$A$	1	1	1	1	1	1	1	1	$z, R_z$	$x^2 + y^2, z^2$
$B$	1	-1	1	1	1	-1	-1	-1		
$E_1$	$\begin{Bmatrix} 1 & \varepsilon & i & -1 & -i & -\varepsilon^* & -\varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & -i & -1 & i & -\varepsilon & -\varepsilon^* & \varepsilon \end{Bmatrix}$								$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	$\begin{Bmatrix} 1 & i & -1 & 1 & -1 & -i & i & -i \\ 1 & -i & -1 & 1 & -1 & i & -i & i \end{Bmatrix}$									$(x^2 - y^2, xy)$
$E_3$	$\begin{Bmatrix} 1 & -\varepsilon & i & -1 & -i & \varepsilon^* & \varepsilon & -\varepsilon^* \\ 1 & -\varepsilon^* & -i & -1 & i & \varepsilon & \varepsilon^* & -\varepsilon \end{Bmatrix}$									



► The  $S_n$  Groups

$S_4$	$E$	$S_4$	$C_2$	$S_4^2$		
$A_1$	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$B_1$	1	-1	1	-1	$z$	$x^2 - y^2, xy$
$E$	$\begin{Bmatrix} 1 & i & -1 & -i \\ 1 & -i & -1 & i \end{Bmatrix}$				$(x, y), (R_x, R_y)$	$(xz, yz)$

$S_6$	$E$	$C_3$	$C_3^2$	$i$	$S_6^2$	$S_6$	$\varepsilon = \exp(2\pi i/3)$
$A_1$	1	1	1	1	1	1	$R_z$
$E_1$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* & 1 & \varepsilon & \varepsilon^* \\ 1 & \varepsilon^* & \varepsilon & 1 & \varepsilon^* & \varepsilon \end{Bmatrix}$						$(R_x, R_y)$
$A_2$	1	1	1	-1	-1	-1	$z$
$E_2$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* & -1 & -\varepsilon & -\varepsilon^* \\ 1 & \varepsilon^* & \varepsilon & -1 & -\varepsilon^* & -\varepsilon \end{Bmatrix}$						$(x, y)$

$S_8$	$E$	$S_8$	$C_4$	$S_8^2$	$C_2$	$S_8^3$	$C_2^2$	$S_8^4$	$\varepsilon = \exp(2\pi i/8)$
$A_1$	1	1	1	1	1	1	1	1	$R_z$
$B_1$	1	-1	1	-1	1	-1	1	-1	$z$
$E_1$	$\begin{Bmatrix} 1 & \varepsilon & i & -\varepsilon^* & -1 & -\varepsilon & -i & \varepsilon^* \\ 1 & \varepsilon^* & -i & -\varepsilon & -1 & -\varepsilon^* & i & \varepsilon \end{Bmatrix}$								$(x, y), (R_x, R_y)$
$E_2$	$\begin{Bmatrix} 1 & i & -1 & -i & 1 & i & -1 & -i \\ 1 & -i & -1 & i & 1 & -i & -1 & i \end{Bmatrix}$								$(x^2 - y^2, xy)$
$E_3$	$\begin{Bmatrix} 1 & -\varepsilon^* & -i & \varepsilon & -1 & \varepsilon^* & i & -\varepsilon \\ 1 & -\varepsilon & i & \varepsilon^* & -1 & \varepsilon & -i & -\varepsilon^* \end{Bmatrix}$								$(xz, yz)$

► The  $C_{nv}$  Groups

$C_{2v}$	$E$	$C_2$	$\sigma_v(xz)$	$\sigma'_v(yz)$		
$A_1$	1	1	1	1	$z$	$x^2, y^2, z^2$
$A_2$	1	1	-1	-1	$R_z$	$xy$
$B_1$	1	-1	1	-1	$x, R_y$	$xz$
$B_2$	1	-1	-1	1	$y, R_x$	$yz$

$C_{3v}$	$E$	$2C_3$	$3\sigma_v$		
$A_1$	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	-1	$R_z$	
$E$	2	-1	0	$(x, y), (R_x, R_y)$	$(x^2 - y^2, xy), (xz, yz)$

C-4

APPENDIX C

$C_{4v}$	$E$	$2C_4$	$C_2$	$2\sigma_v$	$2\sigma_d$		
$A_1$	1	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	-1	$R_z$	
$B_1$	1	-1	1	1	-1		$x^2 - y^2$
$B_2$	1	-1	1	-1	1		$xy$
$E$	2	0	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$

$C_{3v}$	$E$	$2C_3$	$2C_2$	$3\sigma_v$		
$A_1$	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	$R_z$	
$E_1$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		$(x^2 - y^2, xy)$

$C_{6v}$	$E$	$2C_6$	$2C_3$	$C_2$	$3\sigma_v$	$3\sigma_d$		
$A_1$	1	1	1	1	1	1	$z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	1	-1	-1	$R_z$	
$B_1$	1	-1	1	-1	1	-1		
$B_2$	1	-1	1	-1	-1	1		
$E_1$	2	1	-1	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

► The  $C_{nh}$  Groups

$C_{2h}$	$E$	$C_2$	$i$	$\sigma_h$		
$A_g$	1	1	1	1	$R_z$	$x^2, y^2, z^2, xy$
$B_g$	1	-1	1	-1	$R_x, R_y$	$xz, yz$
$A_u$	1	1	-1	-1	$z$	
$B_u$	1	-1	-1	1	$x, y$	

$C_{3h}$	$E$	$C_3$	$C_3^2$	$\sigma_h$	$S_3$	$S_3^2$	$\varepsilon = \exp(2\pi i/3)$	
$A'$	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$E'$	2	$\begin{Bmatrix} \varepsilon & \varepsilon^* \\ \varepsilon^* & \varepsilon \end{Bmatrix}$	$\begin{Bmatrix} \varepsilon^2 & \varepsilon \\ \varepsilon & \varepsilon^2 \end{Bmatrix}$	1	$\begin{Bmatrix} \varepsilon & \varepsilon^* \\ \varepsilon^* & \varepsilon \end{Bmatrix}$	$\begin{Bmatrix} \varepsilon^2 & \varepsilon \\ \varepsilon & \varepsilon^2 \end{Bmatrix}$	$(x, y)$	$(x^2 - y^2, xy)$
$A''$	1	1	1	-1	-1	-1	$z$	
$E''$	2	$\begin{Bmatrix} \varepsilon & \varepsilon^* \\ \varepsilon^* & \varepsilon \end{Bmatrix}$	$\begin{Bmatrix} \varepsilon^2 & \varepsilon \\ \varepsilon & \varepsilon^2 \end{Bmatrix}$	-1	$\begin{Bmatrix} -\varepsilon & -\varepsilon^* \\ -\varepsilon^* & -\varepsilon \end{Bmatrix}$	$\begin{Bmatrix} -\varepsilon^2 & -\varepsilon \\ -\varepsilon & -\varepsilon^2 \end{Bmatrix}$	$(R_x, R_y)$	$(xz, yz)$



## THE DIHEDRAL GROUPS

### ► The $D_n$ Groups

$D_2$	$E$	$C_2(z)$	$C_2(y)$	$C_2(x)$		
$A$	1	1	1	1		$x^2, y^2, z^2$
$B_1$	1	1	-1	-1	$z, R_z$	$xy$
$B_2$	1	-1	1	-1	$y, R_y$	$xz$
$B_3$	1	-1	-1	1	$x, R_x$	$yz$

$D_3$	$E$	$2C_3$	$3C_2$	$(x \text{ axis is coincident with } C_2)$		
$A_1$	1	1	1			$x^2 + y^2, z^2$
$A_2$	1	1	-1	$z, R_z$		
$E$	2	-1	0	$(x, y), (R_x, R_y)$		$(x^2 - y^2, xy), (xz, yz)$

$D_4$	$E$	$2C_4$	$C_2(=C_4^2)$	$2C_2'$	$2C_2''$	$(x \text{ axis coincident with } C_2')$	
$A_1$	1	1	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	-1	$z, R_z$	
$B_1$	1	-1	1	1	-1		$x^2 - y^2$
$B_2$	1	-1	1	-1	1		$xy$
$E$	2	0	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$

$D_5$	$E$	$2C_5$	$2C_5'$	$5C_2$	$(x \text{ axis coincident with } C_2)$	
$A_1$	1	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	$z, R_z$	
$E_1$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0		$(x^2 - y^2, xy)$

$D_6$	$E$	$2C_6$	$2C_3$	$C_2$	$3C_2'$	$3C_2''$	$(x \text{ axis coincident with } C_2')$	
$A_1$	1	1	1	1	1	1		$x^2 + y^2, z^2$
$A_2$	1	1	1	1	-1	-1	$z, R_z$	
$B_1$	1	-1	1	-1	1	-1		
$E_2$	1	-1	1	-1	-1	1		
$E_1$	2	1	-1	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$
$E_2$	2	-1	-1	2	0	0		$(x^2 - y^2, xy)$

► The  $D_{nh}$  Groups

$D_{2h}$	E	$C_2(z)$	$C_2(y)$	$C_2(x)$	i	$\sigma(xy)$	$\sigma(xz)$	$\sigma(yz)$		
$A_g$	1	1	1	1	1	1	1	1		$x^2, y^2, z^2$
$B_{1g}$	1	1	-1	-1	1	1	-1	-1	$R_z$	xy
$B_{2g}$	1	-1	1	-1	1	-1	1	-1	$R_y$	xz
$B_{3g}$	1	-1	-1	1	1	-1	-1	1	$R_x$	yz
$A_u$	1	1	1	1	-1	-1	-1	-1		
$B_{1u}$	1	1	-1	-1	-1	-1	1	1	z	
$B_{2u}$	1	-1	1	-1	-1	1	-1	1	y	
$B_{3u}$	1	-1	-1	1	-1	1	1	-1	x	

$D_{2h}$	E	$2C_2$	$3C_2$	$\sigma_h$	$2S_6$	$3\sigma_v$	(x axis coincident with $C_2$ )				
$A'_1$	1	1	1	1	1	1					$x^2 + y^2, z^2$
$A'_2$	1	1	-1	1	1	-1	$R_z$				
$E'$	2	-1	0	2	-1	0	(x, y)				$(x^2 - y^2, xy)$
$A''_1$	1	1	1	-1	-1	-1					
$A''_2$	1	1	-1	-1	-1	1	z				
$E''$	2	-1	0	-2	1	0	( $R_x, R_y$ )				$(xz, yz)$

$D_{6h}$	E	$2C_6$	$C_2$	$2C_3$	$2C_2'$	i	$2S_6$	$\sigma_h$	$2\sigma_v$	$2\sigma_d$	(x axis coincident with $C_2'$ )	
$A_{1g}$	1	1	1	1	1	1	1	1	1	1		$x^2 + y^2, z^2$
$A_{2g}$	1	1	1	-1	-1	1	1	1	-1	-1	$R_z$	
$B_{1g}$	1	-1	1	1	-1	1	-1	1	1	-1		$x^2 - y^2$
$B_{2g}$	1	-1	1	-1	1	1	-1	1	-1	1		xy
$E_g$	2	0	-2	0	0	2	0	-2	0	0	( $R_x, R_y$ )	$(xz, yz)$
$A_{1u}$	1	1	1	1	1	-1	-1	-1	-1	-1		
$A_{2u}$	1	1	1	-1	-1	-1	-1	-1	1	1	z	
$B_{1u}$	1	-1	1	1	-1	-1	1	-1	-1	1		
$B_{2u}$	1	-1	1	-1	1	-1	1	-1	1	-1		
$E_u$	2	0	-2	0	0	-2	0	2	0	0	(x, y)	

$D_{5h}$	E	$2C_5$	$2C_5^2$	$5C_2$	$\sigma_h$	$2S_{10}$	$2S_5^2$	$5\sigma_v$	(x axis coincident with $C_2$ )	
$A'_1$	1	1	1	1	1	1	1	1		$x^2 + y^2, z^2$
$A'_2$	1	1	1	-1	1	1	1	-1	$R_z$	
$E'_1$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	(x, y)	
$E'_2$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	2	$-2 \cos 144^\circ$	$2 \cos 72^\circ$	0		$(x^2 - y^2, xy)$
$A''_1$	1	1	1	1	-1	-1	-1	-1		
$A''_2$	1	1	1	-1	-1	-1	-1	1	z	
$E''_1$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	-2	$-2 \cos 72^\circ$	$-2 \cos 144^\circ$	0	( $R_x, R_y$ )	$(xz, yz)$
$E''_2$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	-2	$-2 \cos 144^\circ$	$-2 \cos 72^\circ$	0		

$D_{6h}$	$E$	$2C_6$	$2C_3$	$C_2$	$3C_2'$	$3C_2''$	$i$	$2S_6$	$2S_6$	$\sigma_h$	$3\sigma_d$	$3\sigma_v$	(x axis coincident with $C_2'$ )			
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2+y^2, z^2$		
$A_{2g}$	1	1	1	1	-1	-1	1	1	1	1	-1	-1				
$B_{1g}$	1	-1	1	-1	1	-1	1	-1	1	-1	1	-1				
$B_{2g}$	1	-1	1	-1	-1	1	1	-1	1	-1	-1	1				
$E_{1g}$	2	1	-1	-2	0	0	2	1	-1	-2	0	0			$(R_x, R_y)$	$(xz, yz)$ $(x^2 - y^2, xy)$
$E_{2g}$	2	-1	-1	2	0	0	2	-1	-1	2	0	0				
$A_{1u}$	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	$z$			
$A_{2u}$	1	1	1	1	-1	-1	-1	-1	-1	-1	1	1				
$B_{1u}$	1	-1	1	-1	1	-1	-1	1	-1	1	-1	1				
$B_{2u}$	1	-1	1	-1	-1	1	-1	1	-1	1	1	-1				
$E_{1u}$	2	1	-1	-2	0	0	-2	-1	1	2	0	0			$(x, y)$	
$E_{2u}$	2	-1	-1	2	0	0	-2	1	1	-2	0	0				

$D_{6h}$	$E$	$2C_6$	$2C_3$	$2C_2$	$C_2$	$4C_2'$	$4C_2''$	$i$	$2S_6$	$2S_6$	$2S_6$	$\sigma_h$	$4\sigma_d$	$4\sigma_v$	(x axis coincident with $C_2'$ )			
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$		
$A_{2g}$	1	1	1	1	1	-1	-1	1	1	1	1	1	-1	-1				
$B_{1g}$	1	-1	-1	1	1	1	-1	1	-1	-1	1	1	1	-1				
$B_{2g}$	1	-1	-1	1	1	-1	1	1	-1	-1	1	1	-1	1				
$E_{1g}$	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0			$(R_x, R_y)$	$(xz, yz)$ $(x^2 - y^2, xy)$
$E_{2g}$	2	0	0	-2	2	0	0	2	0	0	-2	2	0	0				
$E_{1u}$	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	$z$			
$A_{1u}$	1	1	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1				
$A_{2u}$	1	1	1	1	1	-1	-1	-1	-1	-1	-1	-1	1	1				
$B_{1u}$	1	-1	-1	1	1	1	-1	-1	1	1	-1	-1	-1	1				
$B_{2u}$	1	-1	-1	1	1	-1	1	-1	1	1	-1	-1	1	-1				
$E_{1u}$	2	$\sqrt{2}$	$-\sqrt{2}$	0	-2	0	0	-2	$-\sqrt{2}$	$\sqrt{2}$	0	2	0	0			$(x, y)$	
$E_{2u}$	2	0	0	-2	2	0	0	-2	0	0	2	-2	0	0				
$E_{2u}$	2	$-\sqrt{2}$	$\sqrt{2}$	0	-2	0	0	-2	$\sqrt{2}$	$-\sqrt{2}$	0	2	0	0				

► The  $D_{nd}$  Groups

$D_{2d}$	$E$	$2S_4$	$C_2$	$2C_2'$	$2\sigma_d$	(x axis coincident with $C_2'$ )	
$A_1$	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	-1	-1		
$B_1$	1	-1	1	1	-1	$z$	$x^2 - y^2$ $xy$
$B_2$	1	-1	1	-1	1		
$E$	2	0	-2	0	0	$(x, y), (R_x, R_y)$	$(xz, yz)$

$D_{2d}$	$E$	$2C_3$	$3C_2$	$i$	$2S_6$	$3\sigma_d$	(x axis coincident with $C_2$ )	
$A_{1g}$	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_{2g}$	1	1	-1	1	1	-1		
$E_g$	2	-1	0	2	-1	0	$(R_x, R_y)$	$(x^2 - y^2, xy); (xz, yz)$
$A_{1u}$	1	1	1	-1	-1	-1	$z$	
$A_{2u}$	1	1	-1	-1	-1	1		
$E_u$	2	-1	0	-2	1	0		

$D_{2d}$	$E$	$2S_4$	$2C_2$	$2S_4^3$	$C_2$	$4C_2'$	$4\sigma_d$	(x axis coincident with $C_2'$ )	
$A_1$	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$
$A_2$	1	1	1	1	1	-1	-1		
$B_1$	1	-1	1	-1	1	1	-1		
$B_2$	1	-1	1	-1	1	-1	1		
$E_1$	2	$\sqrt{2}$	0	$-\sqrt{2}$	-2	0	0	$(x, y)$	$(x^2 - y^2, xy)$
$E_2$	2	0	-2	0	2	0	0		
$E_3$	2	$-\sqrt{2}$	0	$\sqrt{2}$	-2	0	0		

$D_{2d}$	1	$2C_2$	$2C_2'$	$5C_2$	$i$	$2S_{10}^3$	$2S_{10}$	$5\sigma_d$	(x axis coincident with $C_2$ )			
$A_{1g}$	1	1	1	1	1	1	1	1	$R_z$	$x^2 + y^2, z^2$		
$A_{2g}$	1	1	1	-1	1	1	1	-1				
$E_{1g}$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0			$(R_x, R_y)$	$(xz, yz)$
$E_{2g}$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0				
$A_{1u}$	1	1	1	1	-1	-1	-1	-1	$z$	$(x^2 - y^2, xy)$		
$A_{2u}$	1	1	1	-1	-1	-1	-1	1				
$E_{1u}$	2	$2 \cos 72^\circ$	$2 \cos 144^\circ$	0	-2	$-2 \cos 72^\circ$	$-2 \cos 144^\circ$	0			$(x, y)$	
$E_{2u}$	2	$2 \cos 144^\circ$	$2 \cos 72^\circ$	0	-2	$-2 \cos 144^\circ$	$-2 \cos 72^\circ$	0				

$D_{3d}$	$E$	$2S_6$	$2C_6$	$2S_6^5$	$2C_3$	$2S_6^3$	$C_2$	$6C_2'$	$6\sigma_d$	(x axis coincident with $C_2$ )	
$A_1$	1	1	1	1	1	1	1	1	1	$R_z$	$x^2 + z^2, z^2$
$A_2$	1	1	1	1	1	1	1	-1	-1		
$B_1$	1	-1	1	-1	1	-1	1	1	-1		
$B_2$	1	-1	1	-1	1	-1	1	-1	1		
$E_1$	2	$\sqrt{3}$	1	0	-1	$-\sqrt{3}$	-2	0	0	$(x, y)$	$(x^2 - y^2, xy)$
$E_2$	2	1	-1	-2	-1	1	2	0	0		
$E_3$	2	0	-2	0	2	0	-2	0	0		
$E_4$	2	-1	-1	2	-1	-1	2	0	0	$(R_x, R_y)$	$(xz, yz)$
$E_5$	2	$-\sqrt{3}$	1	0	-1	$\sqrt{3}$	-2	0	0		

## THE CUBIC GROUPS

### ► Tetrahedral Groups

T	$E$	$4C_3$	$4C_3^2$	$3C_2$	$\epsilon = \exp(2\pi i/3)$	
A	1	1	1	1	$\left\{ \begin{matrix} 1 & \epsilon & \epsilon^* & 1 \\ 1 & \epsilon^* & \epsilon & 1 \end{matrix} \right\}$	$x^2 + y^2 + z^2$
E						$(2z^2 - x^2 - y^2)$
T	3	0	0	-1		$(xy, xz, yz)$

$T_d$	$E$	$4C_3$	$4C_2$	$3C_2$	$i$	$4S_6$	$4S_6^5$	$3\sigma_d$	$(\varepsilon = \exp(2\pi i/3))$	
$A_1$	1	1	1	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_2$	1	1	1	1	-1	-1	-1	-1		
$E$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* & 1 & 1 & \varepsilon & \varepsilon^* & 1 \\ 1 & \varepsilon^* & \varepsilon & 1 & 1 & \varepsilon^* & \varepsilon & 1 \end{Bmatrix}$									$(2z^2 - x^2 - y^2, x^2 - y^2)$
$E'$	$\begin{Bmatrix} 1 & \varepsilon & \varepsilon^* & 1 & -1 & -\varepsilon & -\varepsilon^* & -1 \\ 1 & \varepsilon^* & \varepsilon & 1 & -1 & -\varepsilon^* & -\varepsilon & -1 \end{Bmatrix}$									
$T_2$	3	0	0	-1	3	0	0	-1	$(R_x, R_y, R_z)$	$(xz, yz, xy)$
$T_1$	3	0	0	-1	-3	0	0	1	$(x, y, z)$	

$T_d$	$E$	$8C_3$	$3C_2$	$6S_4$	$6\sigma_d$		
$A_1$	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_2$	1	1	1	-1	-1		
$E$	2	-1	2	0	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T_1$	3	0	-1	1	-1	$(R_x, R_y, R_z)$	
$T_2$	3	0	-1	-1	1	$(x, y, z)$	$(xy, xz, yz)$

► Octahedral Groups

$O$	$E$	$6C_4$	$3C_2(=C_2')$	$8C_3$	$6C_2$		
$A_1$	1	1	1	1	1		$x^2 + y^2 + z^2$
$A_2$	1	-1	1	1	-1		
$E$	2	0	2	-1	0		$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T_1$	3	1	-1	0	-1	$(R_x, R_y, R_z)$	$(x, y, z)$
$T_2$	3	-1	-1	0	1		$(xy, xz, yz)$

$O_h$	$E$	$8C_3$	$6C_2$	$6C_4$	$3C_2(=C_2')$	$i$	$6S_4$	$8S_6$	$3\sigma_h$	$6\sigma_d$	
$A_{1g}$	1	1	1	1	1	1	1	1	1	1	$x^2 + y^2 + z^2$
$A_{2g}$	1	1	-1	-1	1	1	-1	1	1	-1	
$E_g$	2	-1	0	0	2	2	0	-1	2	0	$(2z^2 - x^2 - y^2, x^2 - y^2)$
$T_{1g}$	3	0	-1	1	-1	3	1	0	-1	-1	$(R_x, R_y, R_z)$
$T_{2g}$	3	0	1	-1	-1	3	-1	0	-1	1	$(xz, yz, xy)$
$A_{1u}$	1	1	1	1	1	-1	-1	-1	-1	-1	
$A_{2u}$	1	1	-1	-1	1	-1	1	-1	-1	1	
$E_u$	2	-1	0	0	2	-2	0	1	-2	0	
$T_{1u}$	3	0	-1	1	-1	-3	-1	0	1	1	$(x, y, z)$
$T_{2u}$	3	0	1	-1	-1	-3	1	0	1	-1	



$$\int u dv = uv - \int v du$$

$$\int \sin^n x dx = \frac{-\sin^{n-1} x \cos x}{n} + \frac{n-1}{n} \int \sin^{n-2} x dx$$

$$\int \cos^n x dx = \frac{\cos^{n-1} x \sin x}{n} + \frac{n-1}{n} \int \cos^{n-2} x dx$$

$$\int_{-1}^1 f(x) dx = \begin{cases} 0 & f(x) \text{ ganjil} \\ 2 \int_0^1 f(x) dx & f(x) \text{ genap} \end{cases}$$

Fungsi ganjil  $f(-x) = -f(x)$

Fungsi genap  $f(-x) = f(x)$

$$e^{i\theta} = \cos\theta + i \sin\theta$$

$$\int_{-\infty}^{\infty} x e^{-\frac{x^2}{a^2}} dx = 0$$

$$\int_0^{\infty} x^n e^{-\alpha x} dx = \frac{n!}{\alpha^{n+1}}$$

$$\int_{-\infty}^{\infty} e^{-\frac{x^2}{a^2}} dx = a\sqrt{\pi}$$

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