

---

UNIVERSITI SAINS MALAYSIA

Second Semester Examination  
Academic Session 2008/2009

April/May 2009

**EKC 462 – Advanced Control System for Industrial Processes**  
**[Sistem Kawalan Lanjutan untuk Proses Industri]**

Duration : 3 hours  
[Masa : 3 jam]

---

Please check that this examination paper consists of SEVEN pages of printed material and ONE page of Appendix before you begin the examination.

[*Sila pastikan bahawa kertas peperiksaan ini mengandungi TUJUH muka surat yang bercetak dan SATU muka surat Lampiran sebelum anda memulakan peperiksaan ini.*]

**Instructions:** Answer any FOUR (4) questions.

**Arahan:** Jawab mana-mana EMPAT (4) soalan.]

You may answer the question either in Bahasa Malaysia or in English.

[*Anda dibenarkan menjawab soalan sama ada dalam Bahasa Malaysia atau Bahasa Inggeris.*]

Answer any **FOUR** questions.

*Jawab mana-mana **EMPAT** soalan.*

1. Wardle and Wood (1969) gave the following transfer function matrix for the input-output behaviour of a distillation column
1. *Wardle dan Wood (1969) telah memberi matrik fungsi pemindahan bagi sifat masukan-keluaran bagi sebuah turus penyulingan*

$$\begin{bmatrix} CV_1(s) \\ CV_2(s) \end{bmatrix} = \begin{bmatrix} \frac{0.12e^{-6s}}{60s+1} & \frac{-0.101e^{12s}}{(48s+1)(45s+1)} \\ \frac{0.094e^{-8s}}{38s+1} & \frac{-0.12e^{-8s}}{35s+1} \end{bmatrix} \begin{bmatrix} MV_1(s) \\ MV_2(s) \end{bmatrix}$$

- [a] Calculate the relative gain of the loop and hence calculate the relative gain array.

[a] *Kirakan gandaan relatif bagi gelung dan kirakan juga tatasusunan gandaan relatif.*

[4 marks/markah]

- [b] Using the relative gain array, make comments on the selection of control loop pairing for two single loop controllers.

[b] *Dengan menggunakan tatasusunan gandaan relatif, berikan komen pada pemilihan pasangan gelung kawalan bagi dua pengawal gelung tunggal.*

[4 marks/markah]

- [c] To assess system sensitivity, the engineer considers:

- [i] a change in  $mv1(s)$  of magnitude 1 with  $mv2(s)$  held constant
- [ii] a change in  $mv2(s)$  of magnitude 1 with  $mv1(s)$  held constant

What are the effective gains that correspond to this input direction?

[c] *Untuk menilai kepekaan sistem, jurutera harus mempertimbangkan:*

- [i] *perubahan magnitud 1 pada  $mv1(s)$  dengan  $mv2(s)$  ditetapkan malar*
- [ii] *perubahan magnitud 1 pada  $mv2(s)$  dengan  $mv1(s)$  ditetapkan malar*

*Apakah gandaan berkesan yang sepadan bagi arah masukan tersebut?*

[8 marks/markah]

- [d] If the ratio of the two effective gains is the condition number of the plant, what is significance of the two effective gains? Please confirm your answer.

- [d] *Jika nisbah bagi dua gandaan berkesan adalah syarat bagi nombor keadaan sesebuah loji, apakah kepentingan dua gandaan berkesan tersebut? Sila sahkan jawapan anda.*

[5 marks/markah]

- [e] Using the value obtained for the condition number in [d] make comments about the sensitivity of the plant and the feasibility for applying a decoupling control law.

- [e] *Dengan menggunakan nilai yang diperolehi untuk nombor keadaan pada [d] berikan komen mengenai kepekaan loji dan kesesuaian penggunaan hukum kawalan tak berpasangan.*

[4 marks/markah]

2. [a] What is it meant by prediction horizon (M) and control horizon (P) in model based predictive control (MPC) schemes?

2. [a] *Apakah yang dimaksudkan dengan ramalan ufuk (M) dan kawalan ufuk (P) di dalam model berdasarkan skim kawalan ramalan (MPC)?*

[4 marks/markah]

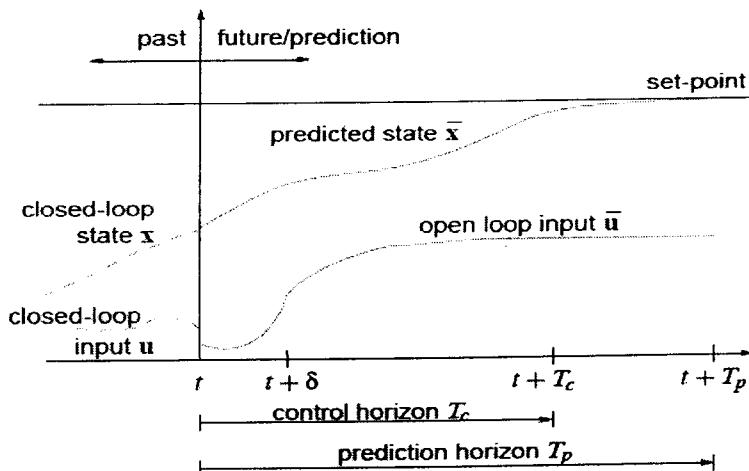


Figure Q.2. [b] : Principle of model predictive control.

*Rajah S.2. [b] : Prinsip model kawalan ramalan.*

- [b] Briefly explain about the principal of MPC control schemes based on the Figure Q.2. [b]?

- [b] *Terangkan secara ringkas prinsip bagi Skim Kawalan MPC berdasarkan Rajah S.2. [b].*

[4 marks/markah]

...4/-

- [c] Consider the following diagram representing conventional and nonlinear model predictive control strategy

[c] Pertimbangkan gambarajah berikut yang mewakili strategi lazim dan model kawalan ramalan yang tak linear

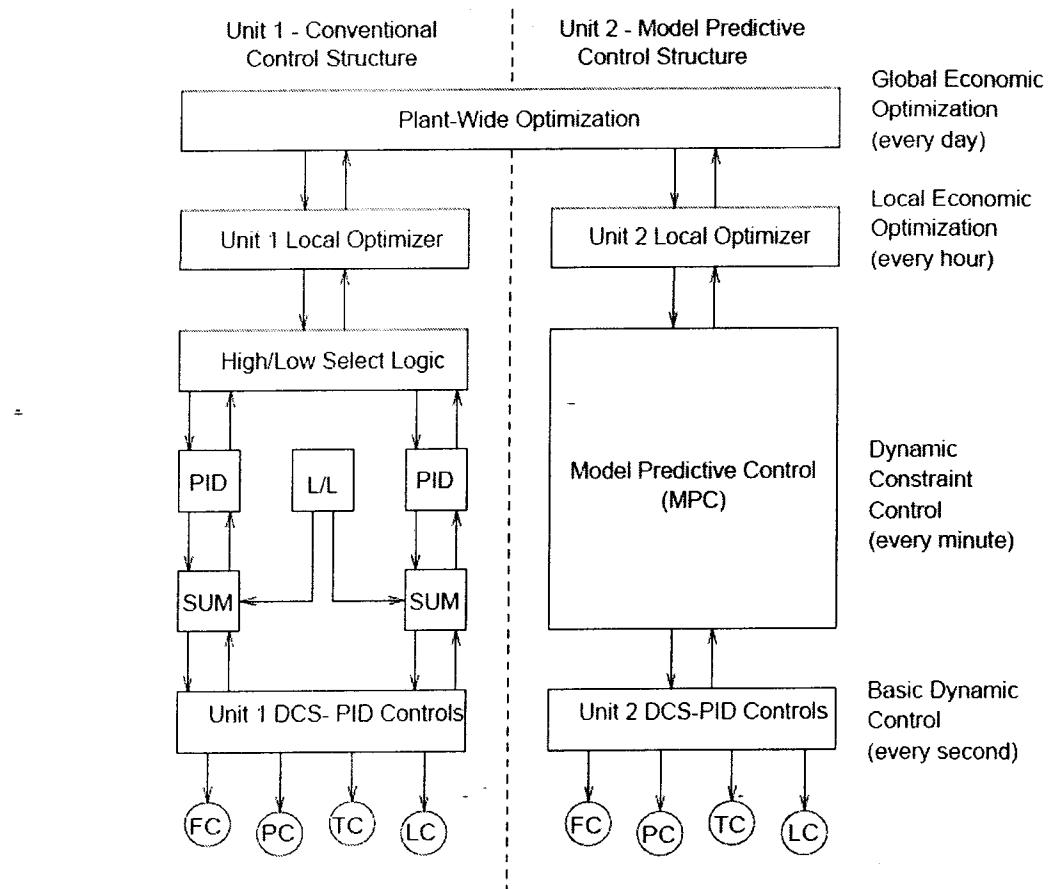


Figure Q.2. [c]. Hierarchy of control system functions in a typical processing plant. Conventional structure is shown at the left; MPC structure is shown at the right.

Rajah S.2. [c]. Hierarki bagi fungsi sistem kawalan dalam loji pemprosesan. Struktur lazim ditunjukkan pada sebelah kiri; struktur MPC ditunjukkan pada sebelah kanan.

- [i] Briefly discuss the key features of MPC as compared to conventional control strategy based on the Figure Q.2.[c].
- [i] Bincangkan secara ringkas sifat-sifat MPC berbanding dengan strategi kawalan lazim berdasarkan Rajah S.2.[c].

[4 marks/markah]

- [ii] Defining all terms and write down a typical controller cost function used in model predictive control laws.
- [ii] Takrifkan semua terma dan tuliskan ciri menyeluruh bagi fungsi pengawal kos yang digunakan dalam hukum kawalan ramalan.

[8 marks/markah]

...5/-

[iii] One of the general objectives of an MPC controller is to prevent violation of input and output constraints. Briefly explain how to support this statement.

[iii] Salah satu daripada objektif umum bagi sebuah pengawal MPC ialah untuk mencegah pelanggaran kekangan bagi masukan dan keluaran. Jelaskan bagaimana untuk menyokong kenyataan ini

[5 marks/markah]

3. [a] Design a model predictive control (MPC) strategy for the process

$$[G_p(s)] = \left[ \frac{e^{-6s}}{10s + 1} \right], \quad G_v = G_m = 1$$

Select a values of  $N$  based on 95% completion of the step response and  $\Delta t = 2$ . Obtain the controller gain  $K_c$  with the following design parameters.

Control Horizon  $M = 1$ , Prediction Horizon,  $P = 10$ , Output weight  $Q = I$ , and Input Weight  $R = 0$ .

3. [a] Rekabentukkan sebuah strategi model kawalan ramalan (MPC) bagi proses

$$[G_p(s)] = \left[ \frac{e^{-6s}}{10s + 1} \right], \quad G_v = G_m = 1$$

Pilih nilai  $N$  berdasarkan kepada 95% siap kepada langkah respon dan  $\Delta t = 2$ . Dapatkan gandaan pengawal  $K_c$  dengan parameter-parameter rekabentuk berikut.

Pengawal Ufuk  $M = 1$ , Ramalan Ufuk,  $P = 10$ , Berat Keluaran  $Q = I$ , dan Berat Masukan  $R = 0$ .

[12 marks/markah]

- [b] A process has the following input-output model:

$$\tilde{g}_p(s) = \frac{-2(3s+1)}{(-4s+1)(5s+1)}$$

Design the IMC-based PID controller (perhaps PI cascaded with a lead-lag filter) for this process.

- [b] Satu proses mempunyai model keluaran-masukan seperti berikut:

$$\tilde{g}_p(s) = \frac{-2(3s+1)}{(-4s+1)(5s+1)}$$

Rekabentukkan pengawal IMC-asas PID (mungkin PI dengan satu penapis mendulu-mengekor) bagi proses ini.

[13 marks/markah]

...6/-

4. [a] Explain the following:

- [i] Smith Predictor
- [ii] Inferential Control
- [iii] Adaptive Control

4. [a] Terangkan perkara-perkara yang berikut:

- [i] Pemampas Smith
- [ii] Pengawal Taabir
- [iii] Pengawal Suai

[12 marks/markah]

[b] Consider the following isothermal chemical reactor (Figure Q.4.[b]), where the dilution rate (feed flow rate per unit volume of reactor) is manipulated to achieve a desired concentration of product.

[b] Pertimbangkan reaktor kimia isoterma berikut (Rajah S.4[b]), di mana kadar pencairan (kadar aliran masuk per unit isipadu reaktor) diolah untuk mencapai kepekatan produk yang dikehendaki.

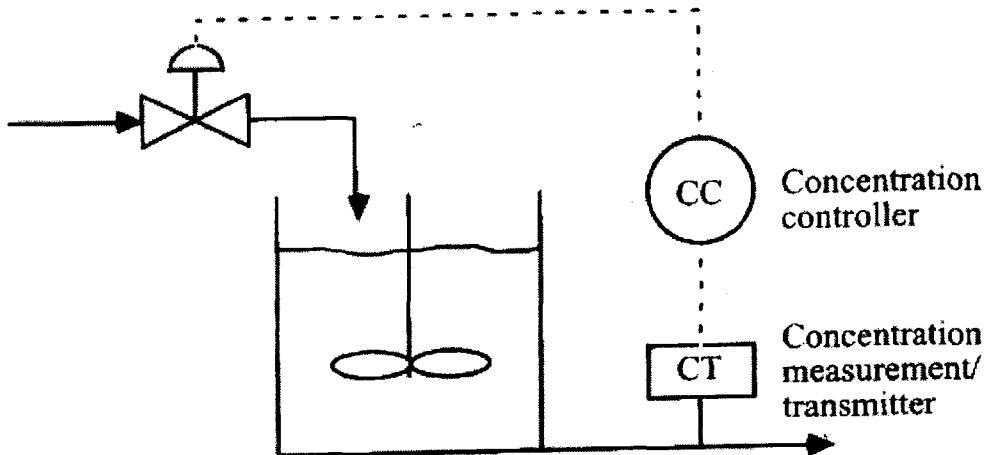


Figure Q.4. [b] : Chemical Reactor  
Rajah S.4[b]: Reaktor Kimia

The process model is:

$$\tilde{g}_p(s) = \frac{0.5848(-0.3549s + 1)e^{-0.5s}}{0.1858s^2 + 0.8627s + 1}$$

Design an IMC for this process using all-pass factorization technique.

*Model bagi proses tersebut ialah:*

$$\tilde{g}_p(s) = \frac{0.5848(-0.3549s + 1)e^{-0.5s}}{0.1858s^2 + 0.8627s + 1}$$

*Rekabentukkan pengawal IMC bagi proses ini dengan menggunakan teknik pemfaktoran semua lulus.*

[13 marks/markah]

...7/-

5. [a] Figure Q.5.[a] shows the proposed automatic control schemes for a reactor where an exothermic reaction  $A + B \rightarrow C$  takes place. Do the following:
- [i] Identify the control schemes proposed.
  - [ii] Justify the needs of such control schemes in the reactor.
5. [a] Rajah S.5.[a] menunjukkan cadangan skema-skema pengawal automatik bagi satu reaktor yang mana tindakbalas eksotermik  $A + B \rightarrow C$  berlaku. Laksanakan perkara-perkara berikut:
- [i] Kenalpasti skema-skema pengawal yang dicadangkan.
  - [ii] Jelaskan mengapa skema-skema pengawal itu diperlukan bagi reaktor tersebut.

[12 marks/markah]

- [b] A process including sensor and control valve can be modelled by a fourth-order transfer function:

$$g_0(s) = \frac{5}{(1.2s+1)(0.08s+1)(s+1)(0.008s+1)}$$

- [i] Derive an approximate FOPTD model using Skogestad's half rule
  - [ii] Design PID controller using IMC-Based PID procedure for the process.
- [b] Satu proses termasuk penderia dan injap kawalan boleh diungkapkan sebagai rangkap pindah tertib keempat seperti berikut:

$$g_0(s) = \frac{5}{(1.2s+1)(0.08s+1)(s+1)(0.008s+1)}$$

- [i] Terbitkan satu anggaran model FOPTD menggunakan peraturan separuh Skogestad
- [ii] Rekabentukkan pengawal PID menggunakan kaedah IMC-asas PID bagi proses tersebut.

[13 marks/markah]

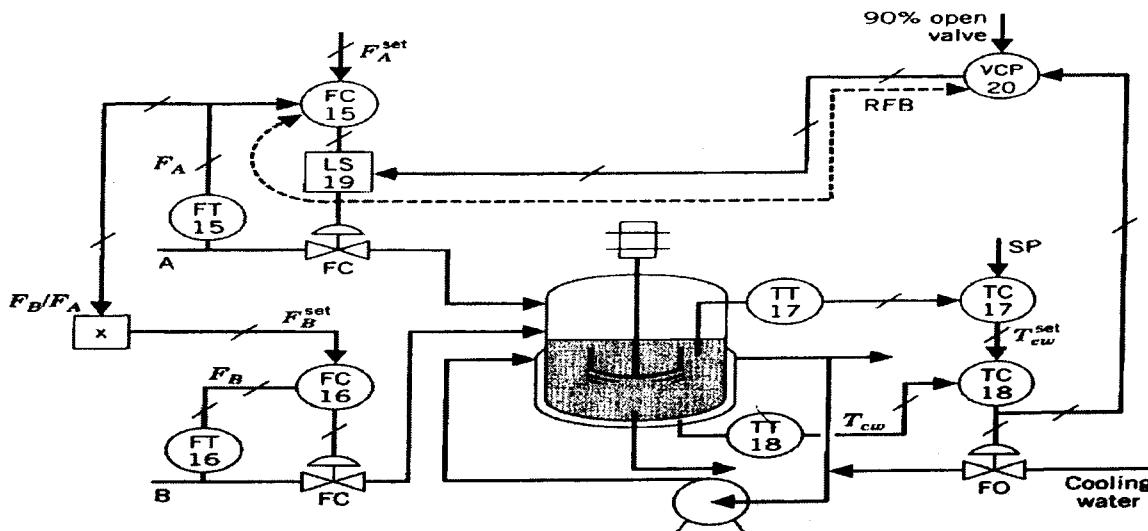


Figure Q.5.[a]: Proposed automatic control scheme for the reactor  
Rajah S.5.[a]: Cadangan skema pengawal automatik bagi satu reaktor

Appendix  
Lampiran

Table Laplace Transforms for Various Time-Domain Functions<sup>a</sup>

$f(t)$	$F(s)$
1. $\delta(t)$ (unit impulse)	$\frac{1}{s}$
2. $S(t)$ (unit step)	$\frac{1}{s}$
3. $t$ (ramp)	$\frac{1}{s^2}$
4. $t^{n-1}$	$\frac{(n-1)!}{s^n}$
5. $e^{-bt}$	$\frac{1}{s+b}$
6. $\frac{1}{\tau} e^{-t/\tau}$	$\frac{1}{\tau s + 1}$
7. $\frac{t^{n-1} e^{-bt}}{(n-1)!} \quad (n > 0)$	$\frac{1}{(s+b)^n}$
8. $\frac{1}{\tau^n(n-1)!} t^{n-1} e^{-t/\tau}$	$\frac{1}{(\tau s + 1)^n}$
9. $\frac{1}{b_1 - b_2} (e^{-b_2 t} - e^{-b_1 t})$	$\frac{1}{(s+b_1)(s+b_2)}$
10. $\frac{1}{\tau_1 - \tau_2} (e^{-t/\tau_1} - e^{-t/\tau_2})$	$\frac{1}{(\tau_1 s + 1)(\tau_2 s + 1)}$
11. $\frac{b_3 - b_1}{b_2 - b_1} e^{-b_1 t} + \frac{b_3 - b_2}{b_1 - b_2} e^{-b_2 t}$	$\frac{s+b_3}{(s+b_1)(s+b_2)}$
12. $\frac{1}{\tau_1} \frac{\tau_1 - \tau_3}{\tau_1 - \tau_2} e^{-t/\tau_1} + \frac{1}{\tau_2} \frac{\tau_2 - \tau_3}{\tau_2 - \tau_1} e^{-t/\tau_2}$	$\frac{\tau_3 s + 1}{(\tau_1 s + 1)(\tau_2 s + 1)}$
13. $1 - e^{-bt}$	$\frac{1}{s(\tau s + 1)}$
14. $\sin \omega t$	$\frac{\omega}{s^2 + \omega^2}$
15. $\cos \omega t$	$\frac{s}{s^2 + \omega^2}$
16. $\sin(\omega t + \phi)$	$\frac{\omega \cos \phi + s \sin \phi}{s^2 + \omega^2}$
17. $e^{-bt} \sin \omega t$	$\left\{ \begin{array}{l} \frac{\omega}{(s+b)^2 + \omega^2} \\ \frac{s+b}{(s+b)^2 + \omega^2} \end{array} \right.$
18. $e^{-bt} \cos \omega t$	$\left\{ \begin{array}{l} \frac{\omega}{(s+b)^2 + \omega^2} \\ \frac{s+b}{(s+b)^2 + \omega^2} \end{array} \right.$
19. $\frac{1}{\tau \sqrt{1 - \zeta^2}} e^{-\zeta t/\tau} \sin(\sqrt{1 - \zeta^2} t/\tau) \quad (0 \leq  \zeta  < 1)$	$\frac{1}{\tau^2 s^2 + 2\zeta \tau s + 1}$
20. $1 + \frac{1}{\tau_2 - \tau_1} (\tau_1 e^{-t/\tau_1} - \tau_2 e^{-t/\tau_2}) \quad (\tau_1 \neq \tau_2)$	$\frac{1}{s(\tau_1 s + 1)(\tau_2 s + 1)}$
21. $1 - \frac{1}{\sqrt{1 - \zeta^2}} e^{-\zeta t/\tau} \sin[\sqrt{1 - \zeta^2} t/\tau + \psi] \quad \psi = \tan^{-1} \frac{\sqrt{1 - \zeta^2}}{\zeta}, \quad (0 \leq  \zeta  < 1)$	$\frac{1}{s(\tau^2 s^2 + 2\zeta \tau s + 1)}$
22. $1 - e^{-\zeta t/\tau} [\cos(\sqrt{1 - \zeta^2} t/\tau) + \frac{\zeta}{\sqrt{1 - \zeta^2}} \sin(\sqrt{1 - \zeta^2} t/\tau)] \quad (0 \leq  \zeta  < 1)$	$\frac{1}{s(\tau^2 s^2 + 2\zeta \tau s + 1)}$
23. $1 + \frac{\tau_3 - \tau_1}{\tau_1 - \tau_2} e^{-t/\tau_1} + \frac{\tau_3 - \tau_2}{\tau_2 - \tau_1} e^{-t/\tau_2} \quad (\tau_1 \neq \tau_2)$	$\frac{\tau_3 s + 1}{s(\tau_1 s + 1)(\tau_2 s + 1)}$
24. $\frac{df}{dt}$	$sF(s) - f(0)$
25. $\frac{d^n f}{dt^n}$	$s^n F(s) - s^{n-1} f(0) - s^{n-2} f^{(1)}(0) - \dots - s f^{(n-2)}(0) - f^{(n-1)}(0)$
26. $f(t - t_0)S(t - t_0)$	$e^{-\omega t} F(s)$

<sup>a</sup>Note that  $f(t)$  and  $F(s)$  are defined for  $t \geq 0$  only.