
UNIVERSITI SAINS MALAYSIA

Final Examination
Academic Session 2008/2009

April 2009

JIM 104 – Introduction To Statistics
[Pengantar Statistik]

Duration : 3 hours
[Masa: 3 jam]

Please ensure that this examination paper contains THIRTY TWO printed pages before you begin the examination.

Answer FOUR questions only. You may answer either in Bahasa Malaysia or in English.

Read the instructions carefully before answering.

Each question is worth 100 marks.

[Sila pastikan bahawa kertas peperiksaan ini mengandungi TIGA PULUH DUA muka surat yang bercetak sebelum anda memulakan peperiksaan ini.]

Jawab EMPAT soalan sahaja. Anda dibenarkan menjawab sama ada dalam Bahasa Malaysia atau Bahasa Inggeris.

Baca arahan dengan teliti sebelum anda menjawab soalan.

Setiap soalan diperuntukkan 100 markah.]

...2/-

1. Given the following data:

25	24	25	24	25
23	25	19	32	23
22	24	26	25	23
28	25	25	26	27
22	28	24	23	24
21	25	22	29	23

- (a) Find

- (i) median,
(ii) mode.

(40 marks)

- (b) Construct a frequency distribution. Use 5 classes.

(30 marks)

- (c) From the distribution, find

- (i) its mean,
(ii) its standard deviation.

(30 marks)

2. (a) The average age of accountants at *Three Rivers Corp* is 26 years, with a standard deviation of 6 years. The average salary of the accountants is RM31,000, with a standard deviation of RM4,000. Compare the variations of age and income.

(20 marks)

- (b) Which of the following exam scores has a better relative position?

X , a score of 42 on exam with mean = 39 and standard deviation = 4.

Y , a score of 76 on an exam with mean = 71 and standard deviation = 3.

(20 marks)

- (c) 51% of families had no children, 20% had one child, 19% had two children, 7% had three children and 3% had four or more children. If a family is selected at random, find the probability that the family has:
- (i) two or three children,
 - (ii) more than one child,
 - (iii) less than three children.

Based on the answer in parts (i), (ii) and (iii), which is most likely to occur? Explain why?

(20 marks)

- (d) In statistics class there are 18 juniors and 10 seniors. Six of the seniors are females, and 12 of the juniors are males. If a student is selected at random, find the probability of selecting the following:
- (i) a junior or a female,
 - (ii) a senior or a female,
 - (iii) a junior or a senior.

(20 marks)

- (e) 70.3% of females ages 20 to 24 have never been married. Choose 5 females in this age category at random. Find the probability that
- (i) none has never been married,
 - (ii) at least one has been married.

(20 marks)

3. (a) A student takes a 20 question, multiple choice exam with five choices for each question and guesses on each question. Find the probability of guessing at least 15 out of 20 correctly.
- (25 marks)
- (b) If 2% of the batteries manufactured by a company are defective, find the probability that in a sample of 144 batteries, 3 are defective ones.
- (25 marks)
- (c) The average salary for first year teachers is RM27,989. If the distribution is approximately normal with $\sigma = \text{RM}3,250$, find the probability that a randomly selected first year teacher earns,
- (i) between RM20,000 and RM30,000 a year,
 - (ii) less than RM20,000 a year.

(25 marks)

...4/-

- (d) A researcher is interested in estimating the average monthly salary of sports reporters in a large city. He wants to be 90% confident that his estimate is correct. If the standard deviation is RM1,100, find the sample size needed to get the desired information and to be accurate to within RM150. (25 marks)
4. (a) The heights of 28 police officers were measured. The standard deviation of the sample was 1.83 inches. Find the 95% confidence interval of the standard deviation of heights of the officers. (25 marks)
- (b) The average salary for public school teachers for a specific year was reported to be RM39,385. A random sample of 50 public school teachers in a particular state had a mean of RM41,680 and a standard deviation of RM5,975. Is there sufficient evidence with $\alpha = 0.05$ to conclude that the mean salary differs from RM39,385? (25 marks)
- (c) In what ways is the t -distribution similar to the standard normal distribution? In what ways is the t -distribution different from the standard normal distribution? (25 marks)
- (d) A researcher claims that the standard deviation of the ages of cats is smaller than the standard deviation of the ages of dogs owned by families in a large city. A randomly selected sample of 29 cats has a standard deviation of 2.7 years, and a random sample of 16 dogs has a standard deviation of 3.5 years. Is the researcher correct? Use $\alpha = 0.05$. If there is a difference, suggest a reason for the difference. (25 marks)
5. (a) The proportion of students in private schools is around 11%. A random sample of 450 students from a wide geographic area indicated that 55 attended private schools. Estimate the true proportion of students attending private schools with 95% confidence. How does your estimate compare to 11%? (30 marks)
- (b) Find the 95% confidence interval for the variance and standard deviation for the time it takes a customer to place a telephone order with a large catalogue company if a sample of 23 telephone orders has a standard deviation of 3.8 minutes. Assume the variable is normally distributed. (20 marks)

- (c) A manager states that in his factory, the average number of days per year missed by the employees due to illness is less than the national average of 10. The following data show the number of days missed by 40 employees last year. Is there sufficient evidence to believe the manager's statement at $\alpha = 0.05$? (use s to estimate σ). Use the P -value method.

0	6	12	3	3	5	4	1
3	9	6	0	7	6	3	4
7	4	7	1	0	8	12	3
2	5	10	5	15	3	2	5
3	11	8	2	2	4	1	9

(30 marks)

- (d) Two groups of students are given a problem-solving test and the results are compared. Find the 90% confidence interval of the true difference in means.

Mathematics majors	Computer Science majors
$\bar{x}_1 = 83.6$	$\bar{x}_2 = 79.2$
$s_1 = 4.3$	$s_2 = 3.8$
$n_1 = 36$	$n_2 = 36$

(20 marks)

1. Diberi data berikut:

25	24	25	24	25
23	25	19	32	23
22	24	26	25	23
28	25	25	26	27
22	28	24	23	24
21	25	22	29	23

- (a) Cari

- (i) median,
(ii) mod.

(40 markah)

- (b) Bina taburan kekerapan bagi data di atas. Gunakan 5 kelas.

(30 markah)

- (c) Daripada taburan, cari

- (i) min,
(ii) sisihan piawai.

(30 markah)

2. (a) Purata umur akauntan di syarikat *Three Rivers* adalah 26 tahun dengan sisihan piawai 6 tahun. Purata gaji akauntan adalah RM31,000, dengan sisihan piawai RM4,000. Bandingkan variasi bagi umur dan pendapatan.

(20 markah)

- (b) Markah peperiksaan yang mana mempunyai kedudukan relatif yang lebih baik?

X , markah peperiksaan 42 dengan $\text{min} = 39$ dan sisihan piawai = 4
 Y , markah peperiksaan 76 dengan $\text{min} = 71$ dan sisihan piawai = 3.

(20 markah)

- (c) 51% keluarga tidak mempunyai anak, 20% mempunyai seorang anak, 19% mempunyai 2 orang anak, 7% mempunyai 3 orang anak dan 3% mempunyai 4 orang anak atau lebih. Jika satu keluarga dipilih secara rawak, cari kebarangkalian bahawa keluarga itu mempunyai:
- (i) dua atau tiga orang anak,
 - (ii) lebih dari seorang anak,
 - (iii) kurang dari tiga orang anak.

Berasaskan jawapan dalam bahagian (i), (ii) dan (iii), yang mana paling kerap berlaku? Jelaskan mengapa?

(20 markah)

- (d) Dalam kelas statistik terdapat 18 orang junior dan 10 orang senior. Enam orang dari senior adalah perempuan dan 12 orang dari junior adalah lelaki. Jika seorang pelajar dipilih secara rawak, cari kebarangkalian bahawa:
- (i) seorang junior atau seorang perempuan yang terpilih,
 - (ii) seorang senior atau seorang perempuan yang terpilih,
 - (iii) seorang junior atau seorang senior yang terpilih.
- (20 markah)
- (e) 70.3% daripada wanita yang berumur di antara 20 tahun dan 24 tahun tidak pernah berkahwin. 5 orang wanita pada kategori umur tersebut dipilih secara rawak. Cari kebarangkalian bahawa:
- (i) tiada seorang pun yang pernah berkahwin,
 - (ii) paling kurang seorang pernah berkahwin.

(20 markah)

3. (a) Seorang pelajar mengambil peperiksaan yang mengandungi 20 soalan objektif, yang mempunyai 5 pilihan jawapan untuk setiap soalan dan meneka jawapan setiap soalan. Dapatkan kebarangkalian ia memperolehi 15 jawapan yang betul.
- (25 markah)
- (b) Jika 2% daripada bateri yang dibuat oleh sebuah syarikat adalah rosak, dapatkan kebarangkalian bahawa dalam satu sampel 144 bateri, terdapat 3 bateri yang rosak.
- (25 markah)

- (c) Gaji purata guru tahun pertama adalah RM27,989. Jika taburan adalah hampir normal dengan $\sigma = \text{RM}3,250$, hitung kebarangkalian bahawa guru tahun pertama yang terpilih secara rawak mendapat gaji
- (i) antara RM20,000 dan RM30,000 setahun,
(ii) kurang daripada RM20,000 setahun.
- (25 markah)
- (d) Seorang penyelidik ingin mengetahui purata gaji bulanan pemberita sukan di sebuah bandar besar. Dia menginginkan keyakinan 90% bahawa anggarannya adalah betul. Jika sisihan piawai adalah RM1,100, dapatkan saiz sampel yang diperlukan untuk mendapatkan maklumat yang diinginkan dan ketepatan dalam lingkungan RM150.
- (25 markah)
4. (a) Ketinggian 28 pegawai polis diukur, sisihan piawai dari sampel adalah 1.83 inci. Dapatkan selang keyakinan 95% daripada sisihan piawai ketinggian pegawai polis.
- (25 markah)
- (b) Purata gaji untuk guru sekolah untuk tahun tertentu adalah dilaporkan sebanyak RM39,385. Sampel rawak 50 guru sekolah di negeri tertentu mempunyai purata RM41,680 dan sisihan piawai RM5,975. Adakah bukti yang cukup pada aras $\alpha = 0.05$ untuk menyimpulkan bahawa purata gaji berbeza daripada RM39,385?
- (25 markah)
- (c) Apakah kesamaan antara taburan t dengan taburan normal piawai? Apakah perbezaan antara taburan t dengan taburan normal piawai?
- (25 markah)
- (d) Seorang penyelidik mendakwa bahawa sisihan piawai umur kucing adalah lebih kecil daripada sisihan piawai umur anjing yang dimiliki oleh keluarga di bandar besar. Satu sampel rawak 29 ekor kucing mempunyai sisihan piawai 2.7 tahun dan satu sampel rawak 16 ekor anjing mempunyai sisihan piawai 3.5 tahun. Adakah dakwaan penyelidik tersebut betul? Gunakan $\alpha = 0.05$. Jika terdapat perbezaan, berikan alasan untuk perbezaan tersebut.
- (25 markah)

5. (a) Kadar pelajar yang menghadiri sekolah persendirian adalah sekitar 11%. Sampel rawak 450 pelajar dari kawasan geografi yang luas menunjukkan bahawa 55 pelajar menghadiri sekolah persendirian. Anggarkan kadar sebenar pelajar yang menghadiri sekolah persendirian dengan keyakinan 95%. Bagaimana hasil anggaran anda dibandingkan dengan 11%.

(30 markah)

- (b) Dapatkan selang keyakinan 95% bagi varians dan sisihan piawai untuk masa yang diperlukan oleh pelanggan membuat tempahan barang melalui telefon dari katalog sebuah syarikat besar jika satu sampel 23 tempahan mempunyai sisihan piawai 3.8 minit. Anggap pembolehubah bertaburan secara normal.

(20 markah)

- (c) Seorang pengurus menyatakan bahawa purata ketidak hadiran para pekerja dalam setahun adalah kurang daripada purata nasional sebanyak 10 hari. Data berikut menunjukkan bilangan hari ketidak hadiran 40 orang pekerja pada tahun lepas. Adakah cukup bukti untuk mempercayai pernyataan pengurus tersebut pada $\alpha = 0.05$? (gunakan s untuk menganggar σ). Gunakan kaedah nilai- P .

0	6	12	3	3	5	4	1
3	9	6	0	7	6	3	4
7	4	7	1	0	8	12	3
2	5	10	5	15	3	2	5
3	11	8	2	2	4	1	9

(30 markah)

- (d) Dua kumpulan pelajar diberikan ujian soal jawab dan keputusannya dibandingkan. Dapatkan selang keyakinan 90% perbezaan min sebenar.

Major Matematik	Major Sains Komputer
$\bar{x}_1 = 83.6$	$\bar{x}_2 = 79.2$
$s_1 = 4.3$	$s_2 = 3.8$
$n_1 = 36$	$n_2 = 36$

(20 markah)

Important Formulas

Chapter 3 Data Description

Mean for individual data: $\bar{X} = \frac{\sum X}{n}$

Mean for grouped data: $\bar{X} = \frac{\sum f \cdot X_m}{n}$

Standard deviation for a sample:

$$s = \sqrt{\frac{\sum X^2 - [(\sum X)^2 / n]}{n-1}}$$

Standard deviation for grouped data:

$$s = \sqrt{\frac{\sum f \cdot X_m^2 - [(\sum f \cdot X_m)^2 / n]}{n-1}}$$

Range rule of thumb: $s \approx \frac{\text{range}}{4}$

Median for grouped data:

$$MD = \frac{(n/2) - cf}{f} (w) + L_m$$

where

n = sum of frequencies

cf = cumulative frequency of class immediately preceding the median class

w = width of median class

f = frequency of median class

L_m = lower boundary of median class

Chapter 4 Probability of Counting Rules

Addition rule 1 (mutually exclusive events):

$$P(A \text{ or } B) = P(A) + P(B)$$

Addition rule 2 (events not mutually exclusive):

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

Multiplication rule 1 (independent events):

$$P(A \text{ and } B) = P(A) \cdot P(B)$$

Multiplication rule 2 (dependent events):

$$P(A \text{ and } B) = P(A) \cdot P(B|A)$$

Conditional probability: $P(B|A) = \frac{P(A \text{ and } B)}{P(A)}$

Complementary events: $P(\bar{E}) = 1 - P(E)$

Fundamental counting rule: Total number of outcomes of a sequence when each event has a different number of possibilities: $k_1 \cdot k_2 \cdot k_3 \cdots k_n$

Permutation rule: Number of permutations of n objects taking r at a time is

$${}_n P_r = \frac{n!}{(n-r)!}$$

Combination rule: Number of combinations of r objects selected from n objects is

$${}_n C_r = \frac{n!}{(n-r)!r!}$$

Chapter 5 Discrete Probability Distributions

Mean for a probability distribution: $\mu = \sum [X \cdot P(X)]$

Variance and standard deviation for a probability distribution:

$$\sigma^2 = \sum [X^2 \cdot P(X)] - \mu^2$$

$$\sigma = \sqrt{\sum [X^2 \cdot P(X)] - \mu^2}$$

Expectation: $E(X) = \sum [X \cdot P(X)]$

Binomial probability: $P(X) = \frac{n!}{(n-X)!X!} \cdot p^X \cdot q^{n-X}$

Mean for binomial distribution: $\mu = n \cdot p$

Variance and standard deviation for the binomial distribution:

$$\sigma^2 = n \cdot p \cdot q \quad \sigma = \sqrt{n \cdot p \cdot q}$$

Multinomial probability:

$$P(X) = \frac{n!}{X_1! X_2! X_3! \cdots X_k!} \cdot p_1^{X_1} \cdot p_2^{X_2} \cdot p_3^{X_3} \cdots p_k^{X_k}$$

Poisson probability: $P(X; \lambda) = \frac{e^{-\lambda} \lambda^X}{X!}$ where $X = 0, 1, 2, \dots$

Hypergeometric probability: $P(X) = \frac{{}_a C_X \cdot {}_b C_{n-X}}{{}_{a+b} C_n}$

Chapter 6 The Normal Distribution

Standard score: $z = \frac{X - \mu}{\sigma}$ or $\frac{X - \bar{X}}{s}$

Mean of sample means: $\mu_{\bar{X}} = \mu$

Standard error of the mean: $\sigma_{\bar{X}} = \frac{\sigma}{\sqrt{n}}$

Central limit theorem formula: $z = \frac{\bar{X} - \mu}{\sigma/\sqrt{n}}$

Chapter 7 Confidence Intervals and Sample Size

z confidence interval for means:

$$\bar{X} - z_{\alpha/2} \left(\frac{\sigma}{\sqrt{n}} \right) < \mu < \bar{X} + z_{\alpha/2} \left(\frac{\sigma}{\sqrt{n}} \right)$$

t confidence interval for means:

$$\bar{X} - t_{\alpha/2} \left(\frac{s}{\sqrt{n}} \right) < \mu < \bar{X} + t_{\alpha/2} \left(\frac{s}{\sqrt{n}} \right)$$

Sample size for means: $n = \left(\frac{z_{\alpha/2} \cdot \sigma}{E} \right)^2$ where E is the maximum error of estimate

Confidence interval for a proportion:

$$\hat{p} - (z_{\alpha/2}) \sqrt{\frac{\hat{p}\hat{q}}{n}} < p < \hat{p} + (z_{\alpha/2}) \sqrt{\frac{\hat{p}\hat{q}}{n}}$$

Sample size for a proportion: $n = \hat{p}\hat{q} \left(\frac{z_{\alpha/2}}{E} \right)^2$

where $\hat{p} = \frac{X}{n}$ and $\hat{q} = 1 - \hat{p}$

Confidence interval for variance:

$$\frac{(n-1)s^2}{\chi^2_{\text{right}}} < \sigma^2 < \frac{(n-1)s^2}{\chi^2_{\text{left}}}$$

Confidence interval for standard deviation:

$$\sqrt{\frac{(n-1)s^2}{\chi^2_{\text{right}}}} < \sigma < \sqrt{\frac{(n-1)s^2}{\chi^2_{\text{left}}}}$$

Chapter 8 Hypothesis Testing

z test: $z = \frac{\bar{X} - \mu}{\sigma/\sqrt{n}}$ for any value n. If $n < 30$, population must be normally distributed.

$z = \frac{\bar{X} - \mu}{s/\sqrt{n}}$ for σ unknown and $n \geq 30$

t test: $t = \frac{\bar{X} - \mu}{s/\sqrt{n}}$ for $n < 30$ (d.f. = $n - 1$)

z test for proportions: $z = \frac{\hat{p} - p}{\sqrt{pq/n}}$

Chi-square test for a single variance: $\chi^2 = \frac{(n-1)s^2}{\sigma^2}$
(d.f. = $n - 1$)

Chapter 9 Testing the Difference Between Two Means, Two Variances and Two Proportions

Z test for comparing two means (independent samples);

$$z = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$$

Formula for the confidence interval for difference of two means (large samples):

$$(\bar{X}_1 - \bar{X}_2) - z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}} < \mu_1 - \mu_2 < (\bar{X}_1 - \bar{X}_2) + z_{\alpha/2} \sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}$$

Note: s_1^2 and s_2^2 can be used when $n_1 \geq 30$ and $n_2 \geq 30$.

F test for comparing two variances: $F = \frac{s_1^2}{s_2^2}$

where s_1^2 is the larger variance and

$$\text{d.f.N.} = n_1 - 1, \text{ d.f.D} = n_2 - 1$$

t test for comparing two means (independent samples, variances not equal):

$$t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$$

(d.f. = the smaller of $n_1 - 1$ or $n_2 - 1$)

Formula for the confidence interval for difference of two means (small independent samples, variance unequal):

$$(\bar{X}_1 - \bar{X}_2) - t_{\alpha/2} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}} < \mu_1 - \mu_2 < (\bar{X}_1 - \bar{X}_2) + t_{\alpha/2} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$$

(d.f. = smaller of $n_1 - 1$ and $n_2 - 1$)

t test for comparing two means (independent samples, variances equal):

$$t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{(n_1 + n_2 - 2)}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$$

(d.f. = $n_1 + n_2 - 2$)

Formula for the confidence interval for difference of two means (small independent samples, variances equal):

$$(\bar{X}_1 - \bar{X}_2) - t_{\alpha/2} \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

$$(\bar{X}_1 - \bar{X}_2) + t_{\alpha/2} \sqrt{\frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}} \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}$$

and d.f. = $n_1 + n_2 - 2$.

t test for comparing two means for dependent samples:

$$t = \frac{\bar{D} - \mu_D}{s_D / \sqrt{n}} \quad \text{where } \bar{D} = \frac{\sum D}{n} \quad \text{and}$$

$$s_D = \sqrt{\frac{\sum D^2 - [(\sum D)^2 / n]}{n-1}} \quad (\text{d.f.} = n-1)$$

Formula for confidence interval for the mean of the difference for dependent samples:

$$\bar{D} - t_{\alpha/2} \frac{S_D}{\sqrt{n}} < \mu_D < \bar{D} + t_{\alpha/2} \frac{S_D}{\sqrt{n}}$$

(d.f. = $n - 1$)

t test for comparing two proportions:

$$z = \frac{(\hat{p}_1 - \hat{p}_2) - (p_1 - p_2)}{\sqrt{pq \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

$$\text{where } \bar{p} = \frac{X_1 + X_2}{n_1 + n_2} \quad \hat{p}_1 = \frac{X_1}{n_1}$$

$$\bar{q} = 1 - \bar{p} \quad \hat{p}_2 = \frac{X_2}{n_2}$$

Formula for the confidence interval for the difference of two proportions:

$$(\hat{p}_1 - \hat{p}_2) - z_{\alpha/2} \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}} < p_1 - p_2 < (\hat{p}_1 - \hat{p}_2) + z_{\alpha/2} \sqrt{\frac{\hat{p}_1 \hat{q}_1}{n_1} + \frac{\hat{p}_2 \hat{q}_2}{n_2}}$$

n	x	p									
		0.05	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
2	0	0.902	0.810	0.640	0.490	0.360	0.250	0.160	0.090	0.040	0.010
	1	0.095	0.180	0.320	0.420	0.480	0.500	0.480	0.420	0.320	0.180
	2	0.002	0.010	0.040	0.090	0.160	0.250	0.360	0.490	0.640	0.810
3	0	0.857	0.729	0.512	0.343	0.216	0.125	0.064	0.027	0.008	0.001
	1	0.135	0.243	0.384	0.441	0.432	0.375	0.288	0.189	0.096	0.027
	2	0.007	0.027	0.096	0.189	0.288	0.375	0.432	0.441	0.384	0.243
	3		0.001	0.008	0.027	0.064	0.125	0.216	0.343	0.512	0.729
4	0	0.815	0.656	0.410	0.240	0.130	0.062	0.026	0.008	0.002	
	1	0.171	0.292	0.410	0.412	0.346	0.250	0.154	0.076	0.026	0.004
	2	0.014	0.049	0.154	0.265	0.346	0.375	0.346	0.265	0.154	0.049
	3		0.004	0.026	0.076	0.154	0.250	0.346	0.412	0.410	0.292
	4			0.002	0.008	0.026	0.062	0.130	0.240	0.410	0.656
5	0	0.774	0.590	0.328	0.168	0.078	0.031	0.010	0.002		
	1	0.204	0.328	0.410	0.360	0.259	0.156	0.077	0.028	0.006	
	2	0.021	0.073	0.205	0.309	0.346	0.312	0.230	0.132	0.051	0.008
	3	0.001	0.008	0.051	0.132	0.230	0.312	0.346	0.309	0.205	0.073
	4			0.006	0.028	0.077	0.156	0.259	0.360	0.410	0.328
	5				0.002	0.010	0.031	0.078	0.168	0.328	0.590
6	0	0.735	0.531	0.262	0.118	0.047	0.016	0.004	0.001		
	1	0.232	0.354	0.393	0.303	0.187	0.094	0.037	0.010	0.002	
	2	0.031	0.098	0.246	0.324	0.311	0.234	0.138	0.060	0.015	0.001
	3	0.002	0.015	0.082	0.185	0.276	0.312	0.276	0.185	0.082	0.015
	4			0.001	0.015	0.060	0.138	0.234	0.311	0.324	0.246
	5				0.002	0.010	0.037	0.094	0.187	0.303	0.393
	6					0.001	0.004	0.016	0.047	0.118	0.262
7	0	0.698	0.478	0.210	0.082	0.028	0.008	0.002			
	1	0.257	0.372	0.367	0.247	0.131	0.055	0.017	0.004		
	2	0.041	0.124	0.275	0.318	0.261	0.164	0.077	0.025	0.004	
	3	0.004	0.023	0.115	0.227	0.290	0.273	0.194	0.097	0.029	0.003
	4			0.003	0.029	0.097	0.194	0.273	0.290	0.227	0.115
	5				0.004	0.025	0.077	0.164	0.261	0.318	0.275
	6					0.004	0.017	0.055	0.131	0.247	0.367
	7						0.002	0.008	0.028	0.082	0.210
8	0	0.663	0.430	0.168	0.058	0.017	0.004	0.001			
	1	0.279	0.383	0.336	0.198	0.090	0.031	0.008	0.001		
	2	0.051	0.149	0.294	0.296	0.209	0.109	0.041	0.010	0.001	
	3	0.005	0.033	0.147	0.254	0.279	0.219	0.124	0.047	0.009	
	4			0.005	0.046	0.136	0.232	0.273	0.232	0.136	0.046
	5				0.009	0.047	0.124	0.219	0.279	0.254	0.147
	6					0.001	0.010	0.041	0.109	0.209	0.296
	7						0.001	0.008	0.031	0.090	0.198
	8							0.001	0.004	0.017	0.058

Table B-5 (continued)

n	x	p									
		0.05	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
9	0	0.630	0.387	0.134	0.040	0.010	0.002				
	1	0.299	0.387	0.302	0.156	0.060	0.018	0.004			
	2	0.063	0.172	0.302	0.267	0.161	0.070	0.021	0.004		
	3	0.008	0.045	0.176	0.267	0.251	0.164	0.074	0.021	0.003	
	4	0.001	0.007	0.066	0.172	0.251	0.246	0.167	0.074	0.017	0.001
	5		0.001	0.017	0.074	0.167	0.246	0.251	0.172	0.066	0.007
	6			0.003	0.021	0.074	0.164	0.251	0.267	0.176	0.045
	7				0.004	0.021	0.070	0.161	0.267	0.302	0.172
	8					0.004	0.018	0.060	0.156	0.302	0.387
	9						0.002	0.010	0.040	0.134	0.387
10	0	0.599	0.349	0.107	0.028	0.006	0.001				
	1	0.315	0.387	0.268	0.121	0.040	0.010	0.002			
	2	0.075	0.194	0.302	0.233	0.121	0.044	0.011	0.001		
	3	0.010	0.057	0.201	0.267	0.215	0.117	0.042	0.009	0.001	
	4	0.001	0.011	0.088	0.200	0.251	0.205	0.111	0.037	0.006	
	5		0.001	0.026	0.103	0.201	0.246	0.201	0.103	0.026	0.001
	6			0.006	0.037	0.111	0.205	0.251	0.200	0.088	0.011
	7				0.001	0.009	0.042	0.117	0.215	0.267	0.201
	8					0.001	0.011	0.044	0.121	0.233	0.302
	9						0.002	0.010	0.040	0.121	0.268
	10							0.001	0.006	0.028	0.107
11	0	0.569	0.314	0.086	0.020	0.004					
	1	0.329	0.384	0.236	0.093	0.027	0.005	0.001			
	2	0.087	0.213	0.295	0.200	0.089	0.027	0.005	0.001		
	3	0.014	0.071	0.221	0.257	0.177	0.081	0.023	0.004		
	4	0.001	0.016	0.111	0.220	0.236	0.161	0.070	0.017	0.002	
	5		0.002	0.039	0.132	0.221	0.226	0.147	0.057	0.010	
	6			0.010	0.057	0.147	0.226	0.221	0.132	0.039	0.002
	7				0.002	0.017	0.070	0.161	0.236	0.220	0.111
	8					0.004	0.023	0.081	0.177	0.257	0.221
	9						0.001	0.005	0.027	0.089	0.200
	10							0.001	0.005	0.027	0.093
	11								0.004	0.020	0.086
12	0	0.540	0.282	0.069	0.014	0.002					
	1	0.341	0.377	0.206	0.071	0.017	0.003				
	2	0.099	0.230	0.283	0.168	0.064	0.016	0.002			
	3	0.017	0.085	0.236	0.240	0.142	0.054	0.012	0.001		
	4	0.002	0.021	0.133	0.231	0.213	0.121	0.042	0.008	0.001	
	5		0.004	0.053	0.158	0.227	0.193	0.101	0.029	0.003	
	6			0.016	0.079	0.177	0.226	0.177	0.079	0.016	
	7				0.003	0.029	0.101	0.193	0.227	0.158	0.053
	8					0.001	0.008	0.042	0.121	0.213	0.133
	9						0.001	0.012	0.054	0.142	0.240
	10							0.002	0.016	0.064	0.168
	11								0.003	0.017	0.071
	12									0.002	0.014

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Table B (*continued*)

n	x	P									
		0.05	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
13	0	0.513	0.254	0.055	0.010	0.001					
	1	0.351	0.367	0.179	0.054	0.011	0.002				
	2	0.111	0.245	0.268	0.139	0.045	0.010	0.001			
	3	0.021	0.100	0.246	0.218	0.111	0.035	0.006	0.001		
	4	0.003	0.028	0.154	0.234	0.184	0.087	0.024	0.003		
	5		0.006	0.069	0.180	0.221	0.157	0.066	0.014	0.001	
	6		0.001	0.023	0.103	0.197	0.209	0.131	0.044	0.006	
	7			0.006	0.044	0.131	0.209	0.197	0.103	0.023	0.001
	8				0.001	0.014	0.066	0.157	0.221	0.180	0.069
	9					0.003	0.024	0.087	0.184	0.234	0.154
	10						0.001	0.006	0.035	0.111	0.218
	11							0.001	0.010	0.045	0.139
	12								0.002	0.011	0.054
	13									0.001	0.010
14	0	0.488	0.229	0.044	0.007	0.001					
	1	0.359	0.356	0.154	0.041	0.007	0.001				
	2	0.123	0.257	0.250	0.113	0.032	0.006	0.001			
	3	0.026	0.114	0.250	0.194	0.085	0.022	0.003			
	4	0.004	0.035	0.172	0.229	0.155	0.061	0.014	0.001		
	5		0.008	0.086	0.196	0.207	0.122	0.041	0.007		
	6		0.001	0.032	0.126	0.207	0.183	0.092	0.023	0.002	
	7			0.009	0.062	0.157	0.209	0.157	0.062	0.009	
	8				0.002	0.023	0.092	0.183	0.207	0.126	0.032
	9					0.007	0.041	0.122	0.207	0.196	0.086
	10						0.001	0.014	0.061	0.155	0.229
	11							0.003	0.022	0.085	0.194
	12								0.001	0.006	0.032
	13									0.001	0.007
	14										0.001
15	0	0.463	0.206	0.035	0.005						
	1	0.366	0.343	0.132	0.031	0.005					
	2	0.135	0.267	0.231	0.092	0.022	0.003				
	3	0.031	0.129	0.250	0.170	0.063	0.014	0.002			
	4	0.005	0.043	0.188	0.219	0.127	0.042	0.007	0.001		
	5	0.001	0.010	0.103	0.206	0.186	0.092	0.024	0.003		
	6		0.002	0.043	0.147	0.207	0.153	0.061	0.012	0.001	
	7			0.014	0.081	0.177	0.196	0.118	0.035	0.003	
	8				0.003	0.035	0.118	0.196	0.177	0.081	0.014
	9					0.001	0.012	0.061	0.153	0.207	0.147
	10						0.003	0.024	0.092	0.186	0.206
	11							0.001	0.007	0.042	0.127
	12								0.002	0.014	0.063
	13									0.003	0.022
	14										0.005
	15										0.005

Table B (continued)

n	x	P										
		0.05	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	0.95
16	0	0.440	0.185	0.028	0.003							
	1	0.371	0.329	0.113	0.023	0.003						
	2	0.146	0.275	0.211	0.073	0.015	0.002					
	3	0.036	0.142	0.246	0.146	0.047	0.009	0.001				
	4	0.006	0.051	0.200	0.204	0.101	0.028	0.004				
	5	0.001	0.014	0.120	0.210	0.162	0.067	0.014	0.001			
	6		0.003	0.055	0.165	0.198	0.122	0.039	0.006			
	7			0.020	0.101	0.189	0.175	0.084	0.019	0.001		
	8				0.006	0.049	0.142	0.196	0.142	0.049	0.006	
	9					0.001	0.019	0.084	0.175	0.189	0.101	0.020
	10						0.006	0.039	0.122	0.198	0.165	0.055
	11							0.001	0.014	0.067	0.162	0.210
	12								0.004	0.028	0.101	0.204
	13									0.001	0.009	0.047
	14										0.002	0.015
	15											0.003
	16											0.003
17	0	0.418	0.167	0.023	0.002							
	1	0.374	0.315	0.096	0.017	0.002						
	2	0.158	0.280	0.191	0.058	0.010	0.001					
	3	0.041	0.156	0.239	0.125	0.034	0.005					
	4	0.008	0.060	0.209	0.187	0.080	0.018	0.002				
	5	0.001	0.017	0.136	0.208	0.138	0.047	0.008	0.001			
	6		0.004	0.068	0.178	0.184	0.094	0.024	0.003			
	7			0.001	0.027	0.120	0.193	0.148	0.057	0.009		
	8				0.008	0.064	0.161	0.185	0.107	0.028	0.002	
	9					0.002	0.028	0.107	0.185	0.161	0.064	0.008
	10						0.009	0.057	0.148	0.193	0.120	0.027
	11							0.003	0.024	0.094	0.184	0.178
	12								0.001	0.008	0.047	0.138
	13									0.002	0.018	0.080
	14										0.005	0.034
	15										0.001	0.010
	16											0.002
	17											0.002

Table B (continued)

n	x	p									
		0.05	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
18	0	0.397	0.150	0.018	0.002						
	1	0.376	0.300	0.081	0.013	0.001					
	2	0.168	0.284	0.172	0.046	0.007	0.001				
	3	0.047	0.168	0.230	0.105	0.025	0.003				
	4	0.009	0.070	0.215	0.168	0.061	0.012	0.001			
	5	0.001	0.022	0.151	0.202	0.115	0.033	0.004			
	6		0.005	0.082	0.187	0.166	0.071	0.015	0.001		
	7		0.001	0.035	0.138	0.189	0.121	0.037	0.005		
	8			0.012	0.081	0.173	0.167	0.077	0.015	0.001	
	9				0.003	0.039	0.128	0.185	0.128	0.039	0.003
	10					0.001	0.015	0.077	0.167	0.173	0.081
	11						0.005	0.037	0.121	0.189	0.138
	12							0.015	0.071	0.166	0.187
	13								0.004	0.033	0.115
	14									0.012	0.061
	15										0.003
	16										0.025
	17										0.105
	18										0.230
19	0	0.377	0.135	0.014	0.001						
	1	0.377	0.285	0.068	0.009	0.001					
	2	0.179	0.285	0.154	0.036	0.005					
	3	0.053	0.180	0.218	0.087	0.017	0.002				
	4	0.011	0.080	0.218	0.149	0.047	0.007	0.001			
	5	0.002	0.027	0.164	0.192	0.093	0.022	0.002			
	6		0.007	0.095	0.192	0.145	0.052	0.008	0.001		
	7		0.001	0.044	0.153	0.180	0.096	0.024	0.002		
	8			0.017	0.098	0.180	0.144	0.053	0.008		
	9				0.005	0.051	0.146	0.176	0.098	0.022	0.001
	10					0.001	0.022	0.098	0.176	0.146	0.051
	11						0.008	0.053	0.144	0.180	0.098
	12							0.002	0.024	0.096	0.153
	13								0.001	0.008	0.052
	14									0.002	0.022
	15										0.001
	16										0.007
	17										0.005
	18										0.005
	19										0.001

Table B (concluded)

n	x	P									
		0.05	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.95
20	0	0.358	0.122	0.012	0.001						
	1	0.377	0.270	0.058	0.007						
	2	0.189	0.285	0.137	0.028	0.003					
	3	0.060	0.190	0.205	0.072	0.012	0.001				
	4	0.013	0.090	0.218	0.130	0.035	0.005				
	5	0.002	0.032	0.175	0.179	0.075	0.015	0.001			
	6		0.009	0.109	0.192	0.124	0.037	0.005			
	7		0.002	0.055	0.164	0.166	0.074	0.015	0.001		
	8			0.022	0.114	0.180	0.120	0.035	0.004		
	9				0.007	0.065	0.160	0.160	0.071	0.012	
	10				0.002	0.031	0.117	0.176	0.117	0.031	0.002
	11					0.012	0.071	0.160	0.160	0.065	0.007
	12					0.004	0.035	0.120	0.180	0.114	0.022
	13					0.001	0.015	0.074	0.166	0.164	0.055 0.002
	14						0.005	0.037	0.124	0.192	0.109 0.009
	15						0.001	0.015	0.075	0.179	0.175 0.032 0.002
	16							0.005	0.035	0.130	0.218 0.090 0.013
	17							0.001	0.012	0.072	0.205 0.190 0.060
	18								0.003	0.028	0.137 0.285 0.189
	19									0.007	0.058 0.270 0.377
	20									0.001	0.012 0.122 0.358

Note: All values of 0.0005 or less are omitted.

Source: John E. Freund, *Modern Elementary Statistics*, 8th ed., © 1992. Reprinted by permission of Prentice-Hall, Inc., Upper Saddle River, N.J.

Table C The Poisson Distribution

x	λ									
	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
0	.9048	.8187	.7408	.6703	.6065	.5488	.4966	.4493	.4066	.3679
1	.0905	.1637	.2222	.2681	.3033	.3293	.3476	.3595	.3659	.3679
2	.0045	.0164	.0333	.0536	.0758	.0988	.1217	.1438	.1647	.1839
3	.0002	.0011	.0033	.0072	.0126	.0198	.0284	.0383	.0494	.0613
4	.0000	.0001	.0003	.0007	.0016	.0030	.0050	.0077	.0111	.0153
5	.0000	.0000	.0000	.0001	.0002	.0004	.0007	.0012	.0020	.0031
6	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0003	.0005	
7	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
x	λ									
	1.1	1.2	1.3	1.4	1.5	1.6	1.7	1.8	1.9	2.0
0	.3329	.3012	.2725	.2466	.2231	.2019	.1827	.1653	.1496	.1353
1	.3662	.3614	.3543	.3452	.3347	.3230	.3106	.2975	.2842	.2707
2	.2014	.2169	.2303	.2417	.2510	.2584	.2640	.2678	.2700	.2707
3	.0738	.0867	.0998	.1128	.1255	.1378	.1496	.1607	.1710	.1804
4	.0203	.0260	.0324	.0395	.0471	.0551	.0636	.0723	.0812	.0902
5	.0045	.0062	.0084	.0111	.0141	.0176	.0216	.0260	.0309	.0361
6	.0008	.0012	.0018	.0026	.0035	.0047	.0061	.0078	.0098	.0120
7	.0001	.0002	.0003	.0005	.0008	.0011	.0015	.0020	.0027	.0034
8	.0000	.0000	.0001	.0001	.0001	.0002	.0003	.0005	.0006	.0009
9	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002
x	λ									
	2.1	2.2	2.3	2.4	2.5	2.6	2.7	2.8	2.9	3.0
0	.1225	.1108	.1003	.0907	.0821	.0743	.0672	.0608	.0550	.0498
1	.2572	.2438	.2306	.2177	.2052	.1931	.1815	.1703	.1596	.1494
2	.2700	.2681	.2652	.2613	.2565	.2510	.2450	.2384	.2314	.2240
3	.1890	.1966	.2033	.2090	.2138	.2176	.2205	.2225	.2237	.2240
4	.0992	.1082	.1169	.1254	.1336	.1414	.1488	.1557	.1622	.1680
5	.0417	.0476	.0538	.0602	.0668	.0735	.0804	.0872	.0940	.1008
6	.0146	.0174	.0206	.0241	.0278	.0319	.0362	.0407	.0455	.0504
7	.0044	.0055	.0068	.0083	.0099	.0118	.0139	.0163	.0188	.0216
8	.0011	.0015	.0019	.0025	.0031	.0038	.0047	.0057	.0068	.0081
9	.0003	.0004	.0005	.0007	.0009	.0011	.0014	.0018	.0022	.0027
10	.0001	.0001	.0001	.0002	.0002	.0003	.0004	.0005	.0006	.0008
11	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0002	.0002
12	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
x	λ									
	3.1	3.2	3.3	3.4	3.5	3.6	3.7	3.8	3.9	4.0
0	.0450	.0408	.0369	.0334	.0302	.0273	.0247	.0224	.0202	.0183
1	.1397	.1304	.1217	.1135	.1057	.0984	.0915	.0850	.0789	.0733
2	.2165	.2087	.2008	.1929	.1850	.1771	.1692	.1615	.1539	.1465
3	.2237	.2226	.2209	.2186	.2158	.2125	.2087	.2046	.2001	.1954
4	.1734	.1781	.1823	.1858	.1888	.1912	.1931	.1944	.1951	.1954

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Table C (continued)

x	λ									
	3.1	3.2	3.3	3.4	3.5	3.6	3.7	3.8	3.9	4.0
5	.1075	.1140	.1203	.1264	.1322	.1377	.1429	.1477	.1522	.1563
6	.0555	.0608	.0662	.0716	.0771	.0826	.0881	.0936	.0989	.1042
7	.0246	.0278	.0312	.0348	.0385	.0425	.0466	.0508	.0551	.0595
8	.0095	.0111	.0129	.0148	.0169	.0191	.0215	.0241	.0269	.0298
9	.0033	.0040	.0047	.0056	.0066	.0076	.0089	.0102	.0116	.0132
10	.0010	.0013	.0016	.0019	.0023	.0028	.0033	.0039	.0045	.0053
11	.0003	.0004	.0005	.0006	.0007	.0009	.0011	.0013	.0016	.0019
12	.0001	.0001	.0001	.0002	.0002	.0003	.0003	.0004	.0005	.0006
13	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0002	.0002
14	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
x	λ									
	4.1	4.2	4.3	4.4	4.5	4.6	4.7	4.8	4.9	5.0
0	.0166	.0150	.0136	.0123	.0111	.0101	.0091	.0082	.0074	.0067
1	.0679	.0630	.0583	.0540	.0500	.0462	.0427	.0395	.0365	.0337
2	.1393	.1323	.1254	.1188	.1125	.1063	.1005	.0948	.0894	.0842
3	.1904	.1852	.1798	.1743	.1687	.1631	.1574	.1517	.1460	.1404
4	.1951	.1944	.1933	.1917	.1898	.1875	.1849	.1820	.1789	.1755
5	.1600	.1633	.1662	.1687	.1708	.1725	.1738	.1747	.1753	.1755
6	.1093	.1143	.1191	.1237	.1281	.1323	.1362	.1398	.1432	.1462
7	.0640	.0686	.0732	.0778	.0824	.0869	.0914	.0959	.1002	.1044
8	.0328	.0360	.0393	.0428	.0463	.0500	.0537	.0575	.0614	.0653
9	.0150	.0168	.0188	.0209	.0232	.0255	.0280	.0307	.0334	.0363
10	.0061	.0071	.0081	.0092	.0104	.0118	.0132	.0147	.0164	.0181
11	.0023	.0027	.0032	.0037	.0043	.0049	.0056	.0064	.0073	.0082
12	.0008	.0009	.0011	.0014	.0016	.0019	.0022	.0026	.0030	.0034
13	.0002	.0003	.0004	.0005	.0006	.0007	.0008	.0009	.0011	.0013
14	.0001	.0001	.0001	.0001	.0002	.0002	.0003	.0003	.0004	.0005
15	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0002
x	λ									
	5.1	5.2	5.3	5.4	5.5	5.6	5.7	5.8	5.9	6.0
0	.0061	.0055	.0050	.0045	.0041	.0037	.0033	.0030	.0027	.0025
1	.0311	.0287	.0265	.0244	.0225	.0207	.0191	.0176	.0162	.0149
2	.0793	.0746	.0701	.0659	.0618	.0580	.0544	.0509	.0477	.0446
3	.1348	.1293	.1239	.1185	.1133	.1082	.1033	.0985	.0938	.0892
4	.1719	.1681	.1641	.1600	.1558	.1515	.1472	.1428	.1383	.1339

(continued)

x	λ									
	5.1	5.2	5.3	5.4	5.5	5.6	5.7	5.8	5.9	6.0
5	.1753	.1748	.1740	.1728	.1714	.1697	.1678	.1656	.1632	.1606
6	.1490	.1515	.1537	.1555	.1571	.1584	.1594	.1601	.1605	.1606
7	.1086	.1125	.1163	.1200	.1234	.1267	.1298	.1326	.1353	.1377
8	.0692	.0731	.0771	.0810	.0849	.0887	.0925	.0962	.0998	.1033
9	.0392	.0423	.0454	.0486	.0519	.0552	.0586	.0620	.0654	.0688
10	.0200	.0220	.0241	.0262	.0285	.0309	.0334	.0359	.0386	.0413
11	.0093	.0104	.0116	.0129	.0143	.0157	.0173	.0190	.0207	.0225
12	.0039	.0045	.0051	.0058	.0065	.0073	.0082	.0092	.0102	.0113
13	.0015	.0018	.0021	.0024	.0028	.0032	.0036	.0041	.0046	.0052
14	.0006	.0007	.0008	.0009	.0011	.0013	.0015	.0017	.0019	.0022
15	.0002	.0002	.0003	.0003	.0004	.0005	.0006	.0007	.0008	.0009
16	.0001	.0001	.0001	.0001	.0001	.0002	.0002	.0002	.0003	.0003
17	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001
x	λ									
	6.1	6.2	6.3	6.4	6.5	6.6	6.7	6.8	6.9	7.0
0	.0022	.0020	.0018	.0017	.0015	.0014	.0012	.0011	.0010	.0009
1	.0137	.0126	.0116	.0106	.0098	.0090	.0082	.0076	.0070	.0064
2	.0417	.0390	.0364	.0340	.0318	.0296	.0276	.0258	.0240	.0223
3	.0848	.0806	.0765	.0726	.0688	.0652	.0617	.0584	.0552	.0521
4	.1294	.1249	.1205	.1162	.1118	.1076	.1034	.0992	.0952	.0912
5	.1579	.1549	.1519	.1487	.1454	.1420	.1385	.1349	.1314	.1277
6	.1605	.1601	.1595	.1586	.1575	.1562	.1546	.1529	.1511	.1490
7	.1399	.1418	.1435	.1450	.1462	.1472	.1480	.1486	.1489	.1490
8	.1066	.1099	.1130	.1160	.1188	.1215	.1240	.1263	.1284	.1304
9	.0723	.0757	.0791	.0825	.0858	.0891	.0923	.0954	.0985	.1014
10	.0441	.0469	.0498	.0528	.0558	.0588	.0618	.0649	.0679	.0710
11	.0245	.0265	.0285	.0307	.0330	.0353	.0377	.0401	.0426	.0452
12	.0124	.0137	.0150	.0164	.0179	.0194	.0210	.0227	.0245	.0264
13	.0058	.0065	.0073	.0081	.0089	.0098	.0108	.0119	.0130	.0142
14	.0025	.0029	.0033	.0037	.0041	.0046	.0052	.0058	.0064	.0071
15	.0010	.0012	.0014	.0016	.0018	.0020	.0023	.0026	.0029	.0033
16	.0004	.0005	.0005	.0006	.0007	.0008	.0010	.0011	.0013	.0014
17	.0001	.0002	.0002	.0002	.0003	.0003	.0004	.0004	.0005	.0006
18	.0000	.0001	.0001	.0001	.0001	.0001	.0001	.0002	.0002	.0002
19	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001

...26/-

Table C (continued)

x	λ									
	7.1	7.2	7.3	7.4	7.5	7.6	7.7	7.8	7.9	8.0
0	.0008	.0007	.0007	.0006	.0006	.0005	.0005	.0004	.0004	.0003
1	.0059	.0054	.0049	.0045	.0041	.0038	.0035	.0032	.0029	.0027
2	.0208	.0194	.0180	.0167	.0156	.0145	.0134	.0125	.0116	.0107
3	.0492	.0464	.0438	.0413	.0389	.0366	.0345	.0324	.0305	.0286
4	.0874	.0836	.0799	.0764	.0729	.0696	.0663	.0632	.0602	.0573
5	.1241	.1204	.1167	.1130	.1094	.1057	.1021	.0986	.0951	.0916
6	.1468	.1445	.1420	.1394	.1367	.1339	.1311	.1282	.1252	.1221
7	.1489	.1486	.1481	.1474	.1465	.1454	.1442	.1428	.1413	.1396
8	.1321	.1337	.1351	.1363	.1373	.1382	.1388	.1392	.1395	.1396
9	.1042	.1070	.1096	.1121	.1144	.1167	.1187	.1207	.1224	.1241
10	.0740	.0770	.0800	.0829	.0858	.0887	.0914	.0941	.0967	.0993
11	.0478	.0504	.0531	.0558	.0585	.0613	.0640	.0667	.0695	.0722
12	.0283	.0303	.0323	.0344	.0366	.0388	.0411	.0434	.0457	.0481
13	.0154	.0168	.0181	.0196	.0211	.0227	.0243	.0260	.0278	.0296
14	.0078	.0086	.0095	.0104	.0113	.0123	.0134	.0145	.0157	.0169
15	.0037	.0041	.0046	.0051	.0057	.0062	.0069	.0075	.0083	.0090
16	.0016	.0019	.0021	.0024	.0026	.0030	.0033	.0037	.0041	.0045
17	.0007	.0008	.0009	.0010	.0012	.0013	.0015	.0017	.0019	.0021
18	.0003	.0003	.0004	.0004	.0005	.0006	.0006	.0007	.0008	.0009
19	.0001	.0001	.0001	.0002	.0002	.0002	.0003	.0003	.0003	.0004
20	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0002
21	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001
x	λ									
	8.1	8.2	8.3	8.4	8.5	8.6	8.7	8.8	8.9	9.0
0	.0003	.0003	.0002	.0002	.0002	.0002	.0002	.0002	.0001	.0001
1	.0025	.0023	.0021	.0019	.0017	.0016	.0014	.0013	.0012	.0011
2	.0100	.0092	.0086	.0079	.0074	.0068	.0063	.0058	.0054	.0050
3	.0269	.0252	.0237	.0222	.0208	.0195	.0183	.0171	.0160	.0150
4	.0544	.0517	.0491	.0466	.0443	.0420	.0398	.0377	.0357	.0337
5	.0882	.0849	.0816	.0784	.0752	.0722	.0692	.0663	.0635	.0607
6	.1191	.1160	.1128	.1097	.1066	.1034	.1003	.0972	.0941	.0911
7	.1378	.1358	.1338	.1317	.1294	.1271	.1247	.1222	.1197	.1171
8	.1395	.1392	.1388	.1382	.1375	.1366	.1356	.1344	.1332	.1318
9	.1256	.1269	.1280	.1290	.1299	.1306	.1311	.1315	.1317	.1318

Table C (continued)

x	λ									
	8.1	8.2	8.3	8.4	8.5	8.6	8.7	8.8	8.9	9.0
10	.1017	.1040	.1063	.1084	.1104	.1123	.1140	.1157	.1172	.1186
11	.0749	.0776	.0802	.0828	.0853	.0878	.0902	.0925	.0948	.0970
12	.0505	.0530	.0555	.0579	.0604	.0629	.0654	.0679	.0703	.0728
13	.0315	.0334	.0354	.0374	.0395	.0416	.0438	.0459	.0481	.0504
14	.0182	.0196	.0210	.0225	.0240	.0256	.0272	.0289	.0306	.0324
15	.0098	.0107	.0116	.0126	.0136	.0147	.0158	.0169	.0182	.0194
16	.0050	.0055	.0060	.0066	.0072	.0079	.0086	.0093	.0101	.0109
17	.0024	.0026	.0029	.0033	.0036	.0040	.0044	.0048	.0053	.0058
18	.0011	.0012	.0014	.0015	.0017	.0019	.0021	.0024	.0026	.0029
19	.0005	.0005	.0006	.0007	.0008	.0009	.0010	.0011	.0012	.0014
20	.0002	.0002	.0002	.0003	.0003	.0004	.0004	.0005	.0005	.0006
21	.0001	.0001	.0001	.0001	.0001	.0002	.0002	.0002	.0002	.0003
22	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001	.0001	.0001
x	λ									
	9.1	9.2	9.3	9.4	9.5	9.6	9.7	9.8	9.9	10.0
0	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0000
1	.0010	.0009	.0009	.0008	.0007	.0007	.0006	.0005	.0005	.0005
2	.0046	.0043	.0040	.0037	.0034	.0031	.0029	.0027	.0025	.0023
3	.0140	.0131	.0123	.0115	.0107	.0100	.0093	.0087	.0081	.0076
4	.0319	.0302	.0285	.0269	.0254	.0240	.0226	.0213	.0201	.0189
5	.0581	.0555	.0530	.0506	.0483	.0460	.0439	.0418	.0398	.0378
6	.0881	.0851	.0822	.0793	.0764	.0736	.0709	.0682	.0656	.0631
7	.1145	.1118	.1091	.1064	.1037	.1010	.0982	.0955	.0928	.0901
8	.1302	.1286	.1269	.1251	.1232	.1212	.1191	.1170	.1148	.1126
9	.1317	.1315	.1311	.1306	.1300	.1293	.1284	.1274	.1263	.1251
10	.1198	.1210	.1219	.1228	.1235	.1241	.1245	.1249	.1250	.1251
11	.0991	.1012	.1031	.1049	.1067	.1083	.1098	.1112	.1125	.1137
12	.0752	.0776	.0799	.0822	.0844	.0866	.0888	.0908	.0928	.0948
13	.0526	.0549	.0572	.0594	.0617	.0640	.0662	.0685	.0707	.0729
14	.0342	.0361	.0380	.0399	.0419	.0439	.0459	.0479	.0500	.0521
15	.0208	.0221	.0235	.0250	.0265	.0281	.0297	.0313	.0330	.0347
16	.0118	.0127	.0137	.0147	.0157	.0168	.0180	.0192	.0204	.0217
17	.0063	.0069	.0075	.0081	.0088	.0095	.0103	.0114	.0119	.0128
18	.0032	.0035	.0039	.0042	.0046	.0051	.0055	.0060	.0065	.0071
19	.0015	.0017	.0019	.0021	.0023	.0026	.0028	.0031	.0034	.0037

Table C (continued)

x	λ									
	9.1	9.2	9.3	9.4	9.5	9.6	9.7	9.8	9.9	10.0
20	.0007	.0008	.0009	.0010	.0011	.0012	.0014	.0015	.0017	.0019
21	.0003	.0003	.0004	.0004	.0005	.0006	.0006	.0007	.0008	.0009
22	.0001	.0001	.0002	.0002	.0002	.0002	.0003	.0003	.0004	.0004
23	.0000	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0002	.0002
24	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0001	.0001	.0001
x	λ									
	11	12	13	14	15	16	17	18	19	20
0	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
1	.0002	.0001	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000
2	.0010	.0004	.0002	.0001	.0000	.0000	.0000	.0000	.0000	.0000
3	.0037	.0018	.0008	.0004	.0002	.0001	.0000	.0000	.0000	.0000
4	.0102	.0053	.0027	.0013	.0006	.0003	.0001	.0001	.0000	.0000
5	.0224	.0127	.0070	.0037	.0019	.0010	.0005	.0002	.0001	.0001
6	.0411	.0255	.0152	.0087	.0048	.0026	.0014	.0007	.0004	.0002
7	.0646	.0437	.0281	.0174	.0104	.0060	.0034	.0018	.0010	.0005
8	.0888	.0655	.0457	.0304	.0194	.0120	.0072	.0042	.0024	.0013
9	.1085	.0874	.0661	.0473	.0324	.0213	.0135	.0083	.0050	.0029
10	.1194	.1048	.0859	.0663	.0486	.0341	.0230	.0150	.0095	.0058
11	.1194	.1144	.1015	.0844	.0663	.0496	.0355	.0245	.0164	.0106
12	.1094	.1144	.1099	.0984	.0829	.0661	.0504	.0368	.0259	.0176
13	.0926	.1056	.1099	.1060	.0956	.0814	.0658	.0509	.0378	.0271
14	.0728	.0905	.1021	.1060	.1024	.0930	.0800	.0655	.0514	.0387
15	.0534	.0724	.0885	.0989	.1024	.0992	.0906	.0786	.0650	.0516
16	.0367	.0543	.0719	.0866	.0960	.0992	.0963	.0884	.0772	.0646
17	.0237	.0383	.0550	.0713	.0847	.0934	.0963	.0936	.0863	.0760
18	.0145	.0256	.0397	.0554	.0706	.0830	.0909	.0936	.0911	.0844
19	.0084	.0161	.0272	.0409	.0557	.0699	.0814	.0887	.0911	.0888
20	.0046	.0097	.0177	.0286	.0418	.0559	.0692	.0798	.0866	.0888
21	.0024	.0055	.0109	.0191	.0299	.0426	.0560	.0684	.0783	.0846
22	.0012	.0030	.0065	.0121	.0204	.0310	.0433	.0560	.0676	.0769
23	.0006	.0016	.0037	.0074	.0133	.0216	.0320	.0438	.0559	.0669
24	.0003	.0008	.0020	.0043	.0083	.0144	.0226	.0328	.0442	.0557
25	.0001	.0004	.0010	.0024	.0050	.0092	.0154	.0237	.0336	.0446
26	.0000	.0002	.0005	.0013	.0029	.0057	.0101	.0164	.0246	.0343
27	.0000	.0001	.0002	.0007	.0016	.0034	.0063	.0109	.0173	.0254
28	.0000	.0000	.0001	.0003	.0009	.0019	.0038	.0070	.0117	.0181
29	.0000	.0000	.0001	.0002	.0004	.0011	.0023	.0044	.0077	.0125

Table C (concluded)

x	λ									
	11	12	13	14	15	16	17	18	19	20
30	.0000	.0000	.0000	.0001	.0002	.0006	.0013	.0026	.0049	.0083
31	.0000	.0000	.0000	.0000	.0001	.0003	.0007	.0015	.0030	.0054
32	.0000	.0000	.0000	.0000	.0001	.0001	.0004	.0009	.0018	.0034
33	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0005	.0010	.0020
34	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	<u>.0006</u>	.0012
35	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0003	.0007
36	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002	.0004
37	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001	.0002
38	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001
39	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0001

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Table E The Standard Normal Distribution

<i>z</i>	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.0000	.0040	.0080	.0120	.0160	.0199	.0239	.0279	.0319	.0359
0.1	.0398	.0438	.0478	.0517	.0557	.0596	.0636	.0675	.0714	.0753
0.2	.0793	.0832	.0871	.0910	.0948	.0987	.1026	.1064	.1103	.1141
0.3	.1179	.1217	.1255	.1293	.1331	.1368	.1406	.1443	.1480	.1517
0.4	.1554	.1591	.1628	.1664	.1700	.1736	.1772	.1808	.1844	.1879
0.5	.1915	.1950	.1985	.2019	.2054	.2088	.2123	.2157	.2190	.2224
0.6	.2257	.2291	.2324	.2357	.2389	.2422	.2454	.2486	.2517	.2549
0.7	.2580	.2611	.2642	.2673	.2704	.2734	.2764	.2794	.2823	.2852
0.8	.2881	.2910	.2939	.2967	.2995	.3023	.3051	.3078	.3106	.3133
0.9	.3159	.3186	.3212	.3238	.3264	.3289	.3315	.3340	.3365	.3389
1.0	.3413	.3438	.3461	.3485	.3508	.3531	.3554	.3577	.3599	.3621
1.1	.3643	.3665	.3686	.3708	.3729	.3749	.3770	.3790	.3810	.3830
1.2	.3849	.3869	.3888	.3907	.3925	.3944	.3962	.3980	.3997	.4015
1.3	.4032	.4049	.4066	.4082	.4099	.4115	.4131	.4147	.4162	.4177
1.4	.4192	.4207	.4222	.4236	.4251	.4265	.4279	.4292	.4306	.4319
1.5	.4332	.4345	.4357	.4370	.4382	.4394	.4406	.4418	.4429	.4441
1.6	.4452	.4463	.4474	.4484	.4495	.4505	.4515	.4525	.4535	.4545
1.7	.4554	.4564	.4573	.4582	.4591	.4599	.4608	.4616	.4625	.4633
1.8	.4641	.4649	.4656	.4664	.4671	.4678	.4686	.4693	.4699	.4706
1.9	.4713	.4719	.4726	.4732	.4738	.4744	.4750	.4756	.4761	.4767
2.0	.4772	.4778	.4783	.4788	.4793	.4798	.4803	.4808	.4812	.4817
2.1	.4821	.4826	.4830	.4834	.4838	.4842	.4846	.4850	.4854	.4857
2.2	.4861	.4864	.4868	.4871	.4875	.4878	.4881	.4884	.4887	.4890
2.3	.4893	.4896	.4898	.4901	.4904	.4906	.4909	.4911	.4913	.4916
2.4	.4918	.4920	.4922	.4925	.4927	.4929	.4931	.4932	.4934	.4936
2.5	.4938	.4940	.4941	.4943	.4945	.4946	.4948	.4949	.4951	.4952
2.6	.4953	.4955	.4956	.4957	.4959	.4960	.4961	.4962	.4963	.4964
2.7	.4965	.4966	.4967	.4968	.4969	.4970	.4971	.4972	.4973	.4974
2.8	.4974	.4975	.4976	.4977	.4977	.4978	.4979	.4979	.4980	.4981
2.9	.4981	.4982	.4982	.4983	.4984	.4984	.4985	.4985	.4986	.4986
3.0	.4987	.4987	.4987	.4988	.4988	.4989	.4989	.4989	.4990	.4990

Note: Use 0.4999 for *z* values above 3.09.

Source: Frederick Mosteller and Robert E. K. Rourke. *Sturdy Statistics*. Table A-1 (Reading, Mass.: Addison-Wesley, 1973). Reprinted with permission of the copyright owners.

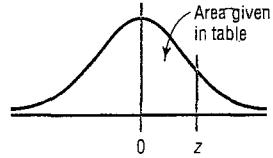
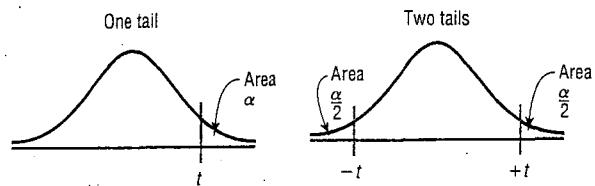


Table F The *t* Distribution

	Confidence intervals	50%	80%	90%	95%	98%	99%
d.f.	One tail, α	0.25	0.10	0.05	0.025	0.01	0.005
	Two tails, α	0.50	0.20	0.10	0.05	0.02	0.01
1		1.000	3.078	6.314	12.706	31.821	63.657
2		.816	1.886	2.920	4.303	6.965	9.925
3		.765	1.638	2.353	3.182	4.541	5.841
4		.741	1.533	2.132	2.776	3.747	4.604
5		.727	1.476	2.015	2.571	3.365	4.032
6		.718	1.440	1.943	2.447	3.143	3.707
7		.711	1.415	1.895	2.365	2.998	3.499
8		.706	1.397	1.860	2.306	2.896	3.355
9		.703	1.383	1.833	2.262	2.821	3.250
10		.700	1.372	1.812	2.228	2.764	3.169
11		.697	1.363	1.796	2.201	2.718	3.106
12		.695	1.356	1.782	2.179	2.681	3.055
13		.694	1.350	1.771	2.160	2.650	3.012
14		.692	1.345	1.761	2.145	2.624	2.977
15		.691	1.341	1.753	2.131	2.602	2.947
16		.690	1.337	1.746	2.120	2.583	2.921
17		.689	1.333	1.740	2.110	2.567	2.898
18		.688	1.330	1.734	2.101	2.552	2.878
19		.688	1.328	1.729	2.093	2.539	2.861
20		.687	1.325	1.725	2.086	2.528	2.845
21		.686	1.323	1.721	2.080	2.518	2.831
22		.686	1.321	1.717	2.074	2.508	2.819
23		.685	1.319	1.714	2.069	2.500	2.807
24		.685	1.318	1.711	2.064	2.492	2.797
25		.684	1.316	1.708	2.060	2.485	2.787
26		.684	1.315	1.706	2.056	2.479	2.779
27		.684	1.314	1.703	2.052	2.473	2.771
28		.683	1.313	1.701	2.048	2.467	2.763
(z) ∞		.674	1.282 ^a	1.645 ^b	1.960	2.326 ^c	2.576 ^d

^aThis value has been rounded to 1.28 in the textbook.^bThis value has been rounded to 1.65 in the textbook.^cThis value has been rounded to 2.33 in the textbook.^dThis value has been rounded to 2.58 in the textbook.Source: Adapted from W. H. Beyer. *Handbook of Tables for Probability and Statistics*, 2nd ed., CRC Press, Boca Raton, Fla., 1986. Reprinted with permission.

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Table G The Chi-Square Distribution

Degrees of freedom	α									
	0.995	0.99	0.975	0.95	0.90	0.10	0.05	0.025	0.01	0.005
1	—	—	0.001	0.004	0.016	2.706	3.841	5.024	6.635	7.879
2	0.010	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210	10.597
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345	12.838
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860
5	0.412	0.554	0.831	1.145	1.610	9.236	11.071	12.833	15.086	16.750
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	23.589
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	26.757
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.299
13	3.565	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688	29.819
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	32.801
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	34.267
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	35.718
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	38.582
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	41.401
22	8.643	9.542	10.982	12.338	14.042	30.813	33.924	36.781	40.289	42.796
23	9.262	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	44.181
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.559
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	46.928
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.194	46.963	49.645
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.993
29	13.121	14.257	16.047	17.708	19.768	39.087	42.557	45.722	49.588	52.336
30	13.787	14.954	16.791	18.493	20.599	40.256	43.773	46.979	50.892	53.672
40	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	66.766
50	27.991	29.707	32.357	34.764	37.689	63.167	67.505	71.420	76.154	79.490
60	35.534	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379	91.952
70	43.275	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425	104.215
80	51.172	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329	116.321
90	59.196	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116	128.299
100	67.328	70.065	74.222	77.929	82.358	118.498	124.342	129.561	135.807	140.169

Source: Donald B. Owen. *Handbook of Statistics Tables*. The Chi-Square Distribution Table. © 1962 by Addison-Wesley Publishing Company, Inc. Copyright renewal © 1990. Reprinted by permission of Pearson Education, Inc.

