

6<sup>th</sup> International Conference  
On  
**Boundary Element Techniques**

27-29<sup>th</sup> July 2005

*La Plaza, Montreal, Canada*



BeTeq 2005

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## **Programme Overview**

### **Wednesday 27<sup>th</sup> July 2005**

8 30	<b>Registration</b>	
9 45	<b>Opening address</b>	
10 00	<b>Coffee Break</b>	
10 30	<b>Session 1</b>	
12 10	<b>Buffet Lunch</b>	
14 00	<b>Session 2A</b>	<b>Session 2B</b>
15 0	<b>Coffee Break</b>	
15 30 -16 30	<b>Session 3A</b>	<b>Session 3B</b>
18 30 – 20 30	<b>Conference Reception</b>	

### **Thursday 28<sup>th</sup> July 2005**

8 30	<b>Keynote Lecture</b>	
9 00	<b>Session 4A</b>	<b>Session 4B</b>
10 00	<b>Coffee Break</b>	
10 30	<b>Sessions 5A</b>	<b>Session 5B</b>
12 10	<b>Buffet Lunch</b>	
14 00	<b>Session 6A</b>	<b>Session 6B</b>
15 00	<b>Coffee Break</b>	
15 30-16 30	<b>Session 7A</b>	<b>Session 7B</b>
19 00	<b>Boarding the Bus for the Conference Dinner</b>	

### **Friday 29<sup>th</sup> July 2005**

8 30	<b>Keynote Lecture</b>	
9 00	<b>Session 8</b>	
10 00	<b>Coffee Break</b>	
10 30	<b>Session 9</b>	
12 10 14 00	<b>Buffet Lunch &amp; End of the Conference</b>	

**Session 1: Solids and Structures**

**Chair:** *W Mansur*

10 30 Viscoelastic analysis of functionally graded materials  
by meshless local Petrov-Galerkin method  
*Sladek, J, Sladek, V, Zhang, Ch*

10 50 Fast 3D contact mechanics BEM algorithm  
*Abascal, R, Luis Rodriguez-Tembleque*

11 10 3D BEM for general anisotropic elasticity  
*Wang, C -Y, Denda, M*

11 30 A numerical Green's function and a local boundary  
integral equation approach  
*L S Miers, J C F Telles*

11 50 Domain boundary element formulation for poro-elastic  
solids  
*Botta, A S, Venturini, W S, Benallal, A*

**Session 2A: Fracture Mechanics**

**Chair:** *A Cisinio*

14 00 Fracture mechanics analysis of plane anisotropic  
bodies with concentrated heat sources using BEM  
*Shiah, Y C, Tan, C L*

14 20 An axisymmetric boundary element analysis of  
interface cracks in fiber reinforced composites  
*Mantic, V, Graciani, E, Paris, F, Varna, J*

14 40 Boundary-domain integro-differential equation of  
elastic damage mechanics model of stationary drilling  
*Mikhailov, S E*

**Session 3A: Computational & Mathematical Aspects**

**Chair:** *M Schanz*

15 30 3D numerical integration of Galerkin type integrals  
*Perez Gavilan, J J, Carrera, J*

15 50 Determination of the slow gravity-driven migration of  
arbitrary clusters of solid particles and spherical bubbles in the  
vicinity of a plane solid wall by a boundary-integral  
formulation  
*Sellier, A*

16 10 Analytic properties underlying boundary integral  
techniques  
*Baker, G*

**Session 2B: New Formulations &  
Computational Aspects**

**Chair:** *R Abascal*

14 00 Boundary element simulation for transient  
measurements in SECM  
*Traeuble, M, Sklyar, O, Wittstock, G*

14 20 Numerics of the convolution quadrature based  
poroelastodynamic BEM  
*Schanz, M, Kielhorn, L*

14 40 Green's function for viscoelastic dynamic in a 3D  
single-layer domain  
*Martinez-Castro, A E, Gallego, R*

**Session 2B: Advanced Material Modelling**

**Chair:** *J Sladek*

15 30 Some applications of FMBEM on 3D composite  
materials  
*Zhenhan Yao, Haitao Wang, Ting Lei*

15 50 Boundary element modelling and optimisation of  
structures made of functionally graded materials  
*Minutolo, V, Ruocco, E*

16 10 Modelling thin walled 3D composite structures  
using the boundary element method  
*Hoefel, S S, Sollero, P, Albuquerque, E L, Portilho, W*

**8.30 Keynote Paper** Simulation of acoustic-fluid-structure interaction with advanced boundary element method *Gaul,L., Fischer,M*

**Chair:** A P Selvadurai

**Session 4A: Fracture Mechanics II**

**Chair:** P H Wen

9 00 A 2-D hypersingular time-domain BEM for dynamic crack analysis in anisotropic solids

*Beyer,S , Zhang,Ch , Hirose,S , Sladek,J , Sladek,V*

9 20 Bond-line defects in SPF/DB structures with BEM

*Di Pisa,C , Aliabadi,M H*

9 40 Energy domain integral applied to solve three-dimensional thermoelastic crack problems using boundary elements

*Balderrama,R , Martinez,M , Cislino,A P*

**Session 5A: Acoustics and Fluid Flow**

**Chair:** B Gattmuri

10 30 Sound pressure reduction provided by an infinite elastic layer containing heterogeneities via BEM

*Pereira,A , Tadeu,A*

10 50 Boundary element acoustic analysis of perforated absorptive silencers

*Zhenlin Ji , Tianyuan Zhang*

11 10 Parameter optimisation in Ewald's method applied to shallow water acoustic wave propagation

*Santiago,J A F , Wrobel,L C*

11 30 The Trefftz method for solving Laplace eigenvalue problems

*Zi-Cai Li , Tzon-Tzer Lu , Heng-Shung Tsai*

11 50 The flux-correct Green element method for linear and nonlinear potential flows

*Taigbenu,A E*

**Session 6A: Fracture and Damage Mechanics**

**Chair:** J C F Telles

14 00 Bending of elastic plates containing internal geometric defects by the indirect boundary element method

*Ventsel,E S , Gwang Jin James Oh*

14 20 A B E M damage analysis of historical masonry walls

*Mallardo,V , Alessandri,C*

14 40 A fundamental-solution-less boundary element method in fracture mechanics

*Chongmin-Song*

**Session 7A: Nonlinear and Dynamic Problems**

**Chair:** L Gaul

15 30 Large deflection analysis of shear deformable shallow shells by the field boundary element method

*Baiz,P M , Aliabadi,M H*

15 50 Boundary elements applied to anisotropic elastoplastic media analysis

*Coda,H B , Vanalli,L , Paccola,R R*

16 10 Dynamic analysis of Mindlin plates

*Wen,P H , Aliabadi,M H*

**Session 4B: Heat and Fluid Flow**

**Chair:** A Sellier

9 00 A BEM for the propagation of non-linear free-surface waves

*Kinnas,S A , Vinayan,V*

9 20 Dual reciprocity BEM for the transient nonlinear heat conduction problem via time-stepping scheme

*Tanaka,M , Matsumoto,T , Takakuwa,S*

9 40 Application of boundary element method to modeling of hydrodynamic forces and experimental validation

*Gardano,P , Dabnichki,P , Aliabadi,M H*

**Session 5B Computational Aspects**

**Chair:** N A Dumont

10 30 Large plastic deformation analysis without use of internal cells by triple-reciprocity BEM

*Ochiai,Y*

10 50 Taguchi and BEM analyses on the productivity performance of an oil reservoir

*Mohamad Ibrahim,M N , Shuib,S*

11 10 Topology optimization of 2D potential problems using boundary elements and generic algorithms

*Anflor,C , Santanna,H , Marczak,R , Cislino,A*

11 30 How to avoid computing the nearfield in the fast multipole method

*Tausch,J*

11 50 Object-oriented modelling of field boundary element method in nonlinear solid mechanics with applications

*Sharafi,H , Gakwaya,A*

**Session 6B New Formulations**

**Chair:** A J Davies

14 00 Rapid elliptical functions based 3D mesh generation for complex surfaces

*Dabnichki,P , Zhivkov,A*

14 20 High superconvergence of combinations of Trefftz method and FEMs for Poisson's equation with singularities

*Hung-Tsai Huang , Zi-Cai Li*

14 40 Coupling techniques for Trefftz methods

*Zi-Cai Li , Hung-Tsai Huang*

**Session 7B: Computational Aspects**

**Chair:** Ochiai,Y

15 30 The Laplace transform dual reciprocity boundary element method for electromagnetic heating problems

*Crann,D , Davies,A J , Christianson,B*

15 50 Estimating the condition number of the matrices appearing in the boundary element method

*Dijkstra,W , Mattheij,R M M*

16 10 A boundary element model for drop deformation in slow viscous flows through a constriction

*Das Bhaumik,C , Wrobel,L C*



**8.30 Keynote Paper**

An advanced mode superposition technique for the general analysis of time-dependent problems

*Dumont, N.A*

**Session 8: Transient Problems**

**Chair:** *W Venturini*

9 00 Two time-domain approaches for the computation of stress and velocity at internal points for 2-D elastodynamics

*Soares, Jr, D, Mansur, W J, Carrer, J A M, Telles, J C F*

9 20 Three-dimensional time-dependent Green's function for unsaturated soils

*Gatmiri, B, Jabbari, E*

9 40 On the evaluation of damping forces in MEMS

*Frangi, A, Spinola, G*

**Session 9: Solids and Structures**

**Chair:** *C L Tan*

10 30 Boundary element analysis of tunnel construction, the challenges and proposed solutions

*Beer, G, Duenser, C, Riberio, S.A*

10 50 Stress-strain state provoked by displacement of rigid inclusions in thin plates

*Melnikov, M Y, Melnikov, Y A*

11 10 Comparison of finite and boundary element results for the stress intensity factors with analytical formulations in LEFM

*Leme, S P L, Lima, R F, Bezerra, L M, Partridge, P W*

11 30 Crack bridging in uni-directionally reinforced composites

*Selvadurai, A P S*

11 50 The boundary element method in wear simulation

*Sfantos, G K, Ahabadi, M H*

# Taguchi and BEM Analyses on the Productivity Performance of an Oil Reservoir

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**Keywords:** Taguchi method, Boundary Element Method, reservoir rock properties, reservoir fluid property, oil reservoir

**Abstract.** The application of Taguchi Robust Design Technique (TRDT) coupled with the Boundary Element Method (BEM) in analyzing the productivity performance of an oil reservoir is presented in this paper. Several reservoir rock and reservoir fluid properties, i.e. permeability, thickness, porosity and viscosity, were chosen in this study. The BEM allows the overall simulation of reservoir performance to be made, whereas the use of TRDT allows us to rank the most influencing factor (property) that affects the productivity performance of the reservoir. Numerical values obtained from the BEM analysis will be used as input data for the TRDT statistical analysis. Results indicated that oil viscosity is the most important factor that affects the productivity performance of the oil reservoir followed by the thickness of the pay zone, the rock permeability and the rock porosity. Results of this study can be used by reservoir engineer in making the right choice of Enhance Oil Recovery techniques that is the most suitable for the reservoir.

## Taguchi Method

In this study, Taguchi Robust Design Technique (TRDT) was used to rank factors that may effect the productivity of oil reservoir. The use of Taguchi orthogonal array helps to determine the minimum number of simulation runs needed to produce the most favourable output for a given set of factors. These factors are rock permeability, reservoir oil viscosity, thickness of net pay and reservoir rock porosity. The comparison between full factorial design and Taguchi design is shown in Table 1. The orthogonal array  $L_9$  was used to study the influence of these four factors. Each factor was considered at three levels. The factors involved and their levels are shown in Table 2. If full factorial experimental design were used, it would require 81 ( $3^4$ ) trials runs for all possible combinations of these factors to get the optimum result [1]. By using the Taguchi orthogonal array  $L_9$  for experimental design, the number of trials runs was reduced to 9 simple and effective experiments.

Factors	Level	Total number of experiments	
		Factorial design	Taguchi design
2	2	4 ( $2^2$ )	4
3	2	8 ( $2^3$ )	4
4	2	16 ( $2^4$ )	8
7	2	128 ( $2^7$ )	8
15	2	32,768 ( $2^{15}$ )	16
4	3	81 ( $3^4$ )	9

**Table 1** : Comparisons of factorial design and Taguchi design

Column	Factors	Level Number		
		1	2	3
1	Permeability (md)	50	100	150
2	Viscosity (cp)	0.5	1	1.5
3	Thickness (feet)	10	20	30
4	Porosity (fraction)	0.15	0.30	0.45

**Table 2** : Design factors and their levels for orthogonal experiment

Table 3 illustrates the orthogonal array  $L_9$  [1]. Since there were four of three levels factors, these factors were assigned to all four columns in the  $L_9$  array. For example in trial number 1, the value for rock permeability, oil viscosity, net pay thickness and rock porosity is 50 md, 0.5 cp, 10 feet and 0.15 (15%) respectively. For trial number 2, the value for permeability, viscosity, thickness and porosity is 50 md, 1.0 cp, 20 feet and 0.3 (30%) respectively. Nine trials simulation runs using the Boundary Element Oil Reservoir Simulation software with particular combination of factors levels in the array were carried out [2, 3, 4].

Trial Number	Column Number			
	1	2	3	4
1	1	1	1	1
2	1	2	2	2
3	1	3	3	3
4	2	1	2	3
5	2	2	3	1
6	2	3	1	2
7	3	1	3	2
8	3	2	1	3
9	3	3	2	1

**Table 3** :  $L_9$  ( $3^4$ ) Orthogonal Array [1]

## Results and Discussion

The results of the nine trial conditions are shown in Table 4. These simulation results are for the case of the following circular oil reservoir with single production well having the following properties

$Area = 314.2 \times 10^6 \text{ feet}^2 = 7,212 \text{ acre}$  (reservoir area),

$r_w = 0.25 \text{ feet}$  (well-bore radius),

$\rho = 62.4 \text{ lb/ft}^3$  (reservoir fluid density),

$p_w = 100 \text{ psi}$  (well-bore pressure),

$p_e = 2,000 \text{ psi}$  (external reservoir pressure) and

$Scale = 1:5,000$

In the Taguchi analysis, there are three of quality characteristics with respect to the target design, namely “smaller is better” and “bigger is better” [1]. In this study, the high value of oil production is desirable, therefore the “bigger is better” quality characteristic was chosen.

<b>Trial Number</b>	<b>Total Oil Production in barrel per day (bbl/d)</b>
1	1270.2
2	1270.2
3	1270.2
4	5080.9
5	3810.7
6	846.8
7	11432.0
8	1905.3
9	2450.4
<b>Grand Average</b>	<b>3259.633</b>

**Table 4 : Simulation results**

Different factors affect the wells productivities to different degrees. The relative effect of the different factors can be obtained by the decomposition of total variation into its appropriate components, which is commonly called analysis of variance (ANOVA). ANOVA is also needed for estimating the error variance. The results of ANOVA are shown in Table 5. Data generated in Table 5 especially the Sum of Squares, Variance and Percent were obtained from TRDT educational software, Qualitek-4 [5].

<b>Column</b>	<b>Factors</b>	<b>DOF</b>	<b>Sum of Squares</b>	<b>Variance</b>	<b>F</b>	<b>Percent</b>
1	Permeability (md)	2	23909295.85	11954647.925	-	26.392
2	Viscosity (cp)	2	33008700.598	16504350.299	-	36.436
3	Thickness (feet)	2	26480181.115	13240090.557	-	29.229
4	Porosity (fraction)	2	7194457.734	3597228.867	-	7.941
All others/error		0	0			0
<b>Total</b>		<b>8</b>	<b>90592640.958</b>			<b>100.00 %</b>

**Table 5 : ANOVA table**

The review of the 'Percent' column in Table 5 showed that the oil viscosity factor contributed the highest percentage (36.4%) to the factor effects, followed by the net pay thickness (29.2%), rock permeability (26.4%) and rock porosity (7.9%). Since the contribution of rock porosity was the smallest and less than 10% therefore it was considered insignificant. Thus, this factor was pooled (combined) with the error term. This process of disregarding the contribution of a selected factor and subsequently adjusting the contribution of the other factor is known as pooling. The new ANOVA after pooling is shown in Table 6. It was observed that as the smallest factor effect (porosity) was pooled, the percentage contributions of the remaining factors decreased slightly, but the ranking of factor effects still remained the same. In estimating the performance at optimum condition, only the significant factors were used. An examination of the average effects as shown in Table 7 indicates that level 1 of viscosity and level 3 of both permeability and thickness factors will be included in the optimum condition (after excluding the porosity factor). This is due to the highest value of average effects for each factor. With this levels combination, one should get the total oil production as 11,432 bbl/d.

Column	Factors	DOF	Sum of Squares	Variance	F	Percent
1	Permeability (md)	2	23909205.85	11954647.925	3.323	18.45
2	Viscosity (cp)	2	33008700.598	16504350.299	4.588	28.494
3	Thickness (feet)	2	26480181.115	13240090.557	3.68	21.288
4	Porosity (fraction)	(2)	(7194457.734)		POOLED	
All others/Error		2	7194463.392	3597231.696		31.768
<b>Total</b>		<b>8</b>	<b>31.19</b>			<b>100.00 %</b>

**Table 6 : Pooled ANOVA table**

Column	Factors	Level Number		
		1	2	3
1	Permeability (md)	1270.199	3246.133	5262.566
2	Viscosity (cp)	5927.699	2328.733	1522.466
3	Thickness (feet)	1340.766	2933.833	5504.3
4	Porosity (fraction)	2510.433	4516.333	2752.133

**Table 7 : The Average Effects of Factor for Each Level**

Most data generated in Table 6 and Table 7 especially were obtained from TRDT educational software, Qualitek-4 [5].

## Conclusions

Among four factors considered in this study, reservoir oil viscosity found to be the most influenced factor in producing oil from the reservoir. It's followed by the net pay thickness, rock permeability and rock porosity. Designing an Enhance Oil Recovery technique that can improve the oil viscosity such as steam flooding would be a good idea in order to improve the productivity of the reservoir.

Further analysis shows that (by keeping the viscosity, thickness and permeability at their optimum levels), regardless of any rock porosity value use in the simulation runs, the oil productivity values are still the same. This proves that porosity has very small contribution towards the productivity of the reservoir.

## Acknowledgements

The authors would like to express their appreciation to Universiti Sains Malaysia and the Malaysian Ministry of Science, Technology and Innovation for their financial support of this project through a research grant.

## References

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